

# Thermal modelling for the implementation of an energetic efficiency control system in a room of meetings of singular geometry

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Instituto Tecnológico de la Energía



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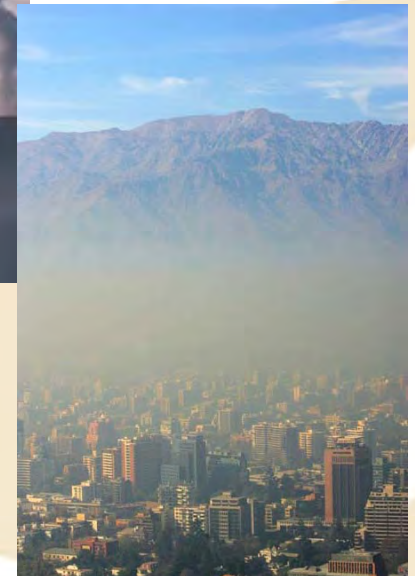
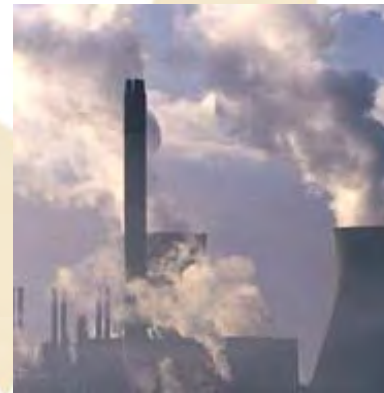
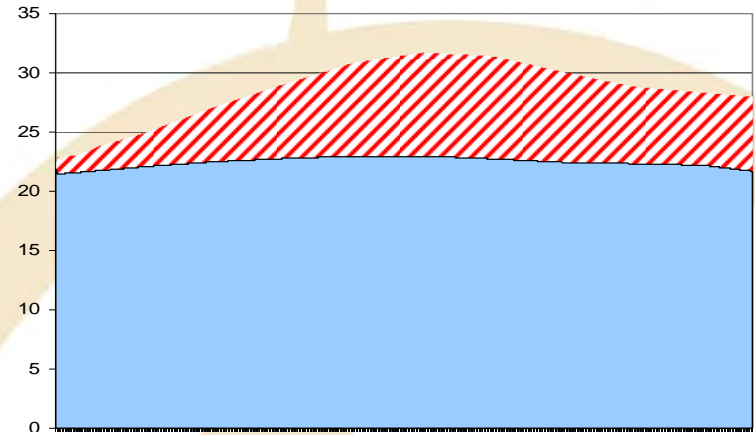
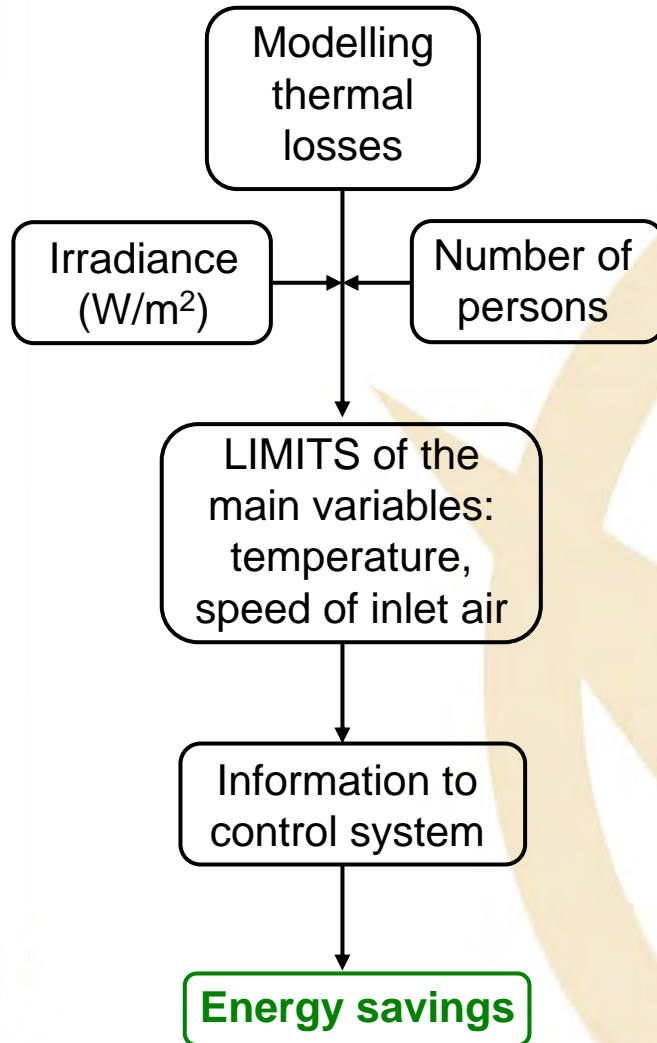
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# Introduction & objectives

- **Introduction & objectives.**

- Construction details.
- Irradiance data.
- Simulation scenarios.
- Irradiance curve fitting.
- Restrictions and b. c. approach.
- Finite Element mesh.
- Results.
- Conclusions



## Introduction & objectives

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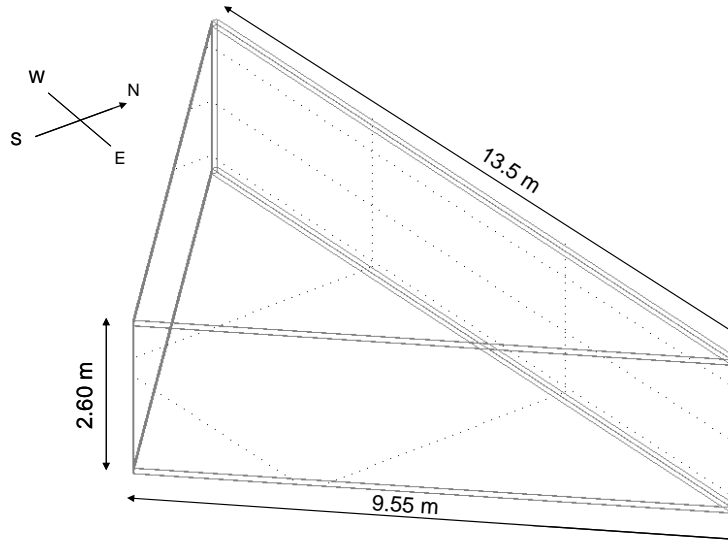
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- ❑ Collect irradiance data from weather station for 1 year.
- ❑ Fit the irradiance data to a mathematical model.
- ❑ Approach the Finite Element model and impose the corresponding boundary conditions.
- ❑ Estimate the spatial and temporary temperature evolution of the model and analyze different scenarios.

# Enclosure construction details

## ▣ Enclosure features

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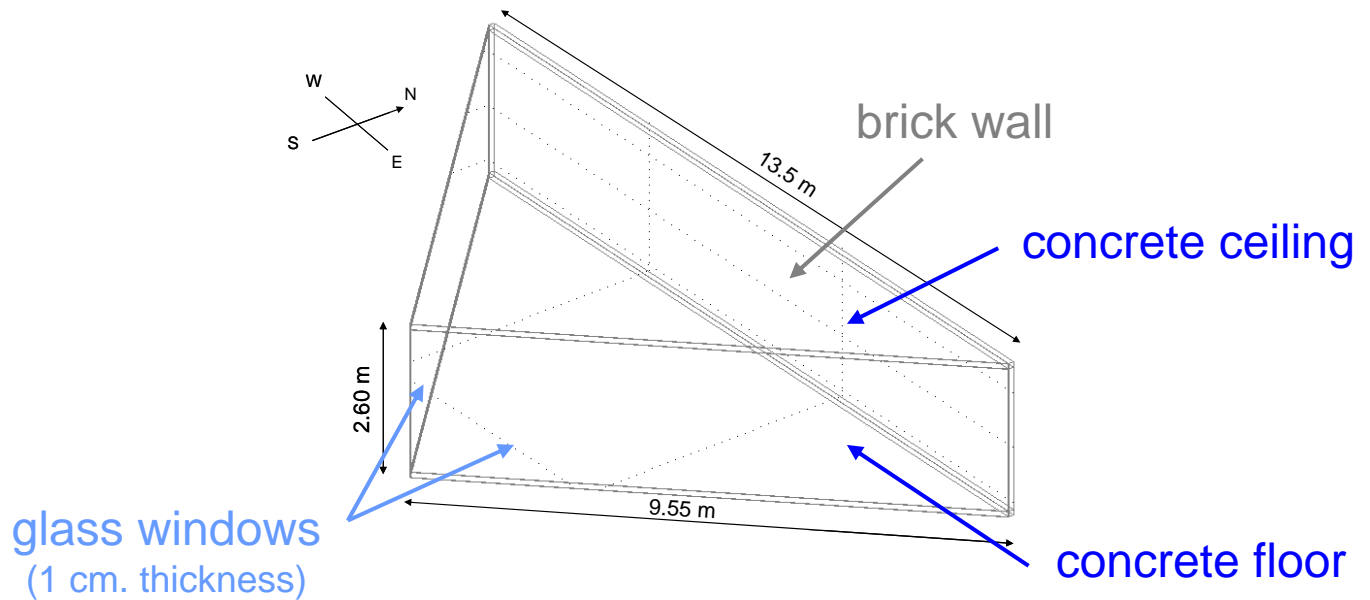


Enclosure volume:  
118.46 m<sup>3</sup>

# Enclosure construction details

## Enclosure features

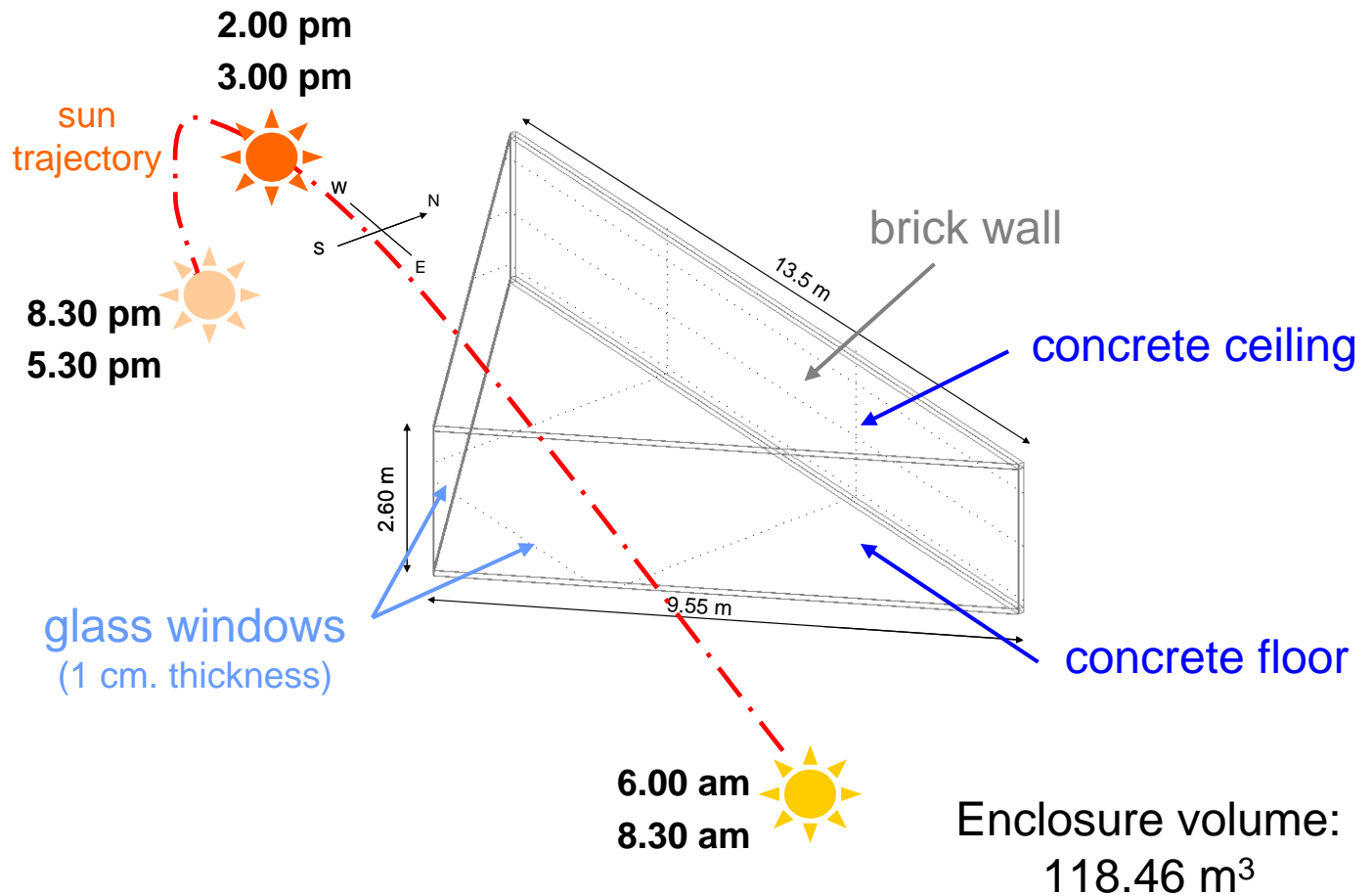
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Enclosure volume:  
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# Enclosure construction details

## Enclosure features and sun trajectory



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# Irradiance data

## ☐ Irradiance data from weather station

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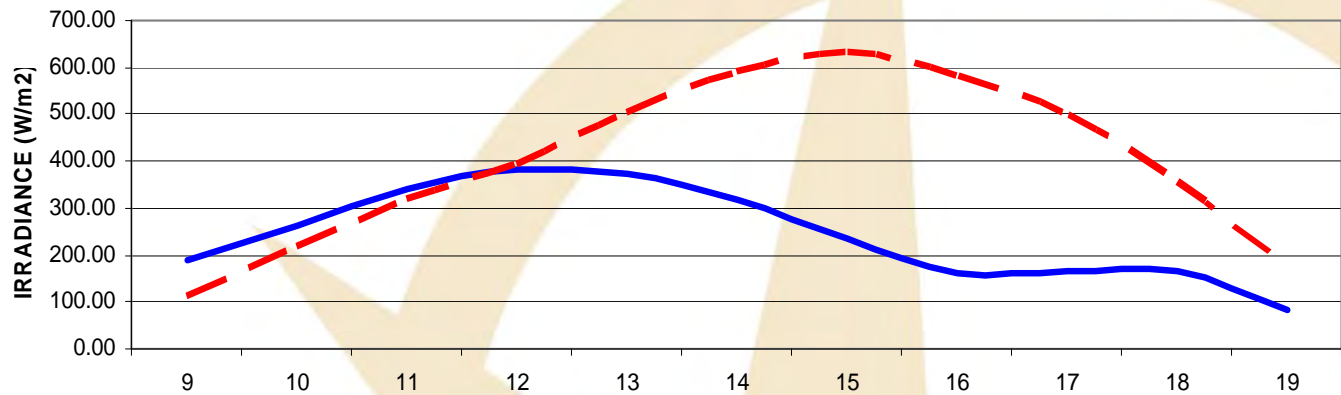
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# Irradiance data

## Irradiance data from weather station

### Summer irradiance



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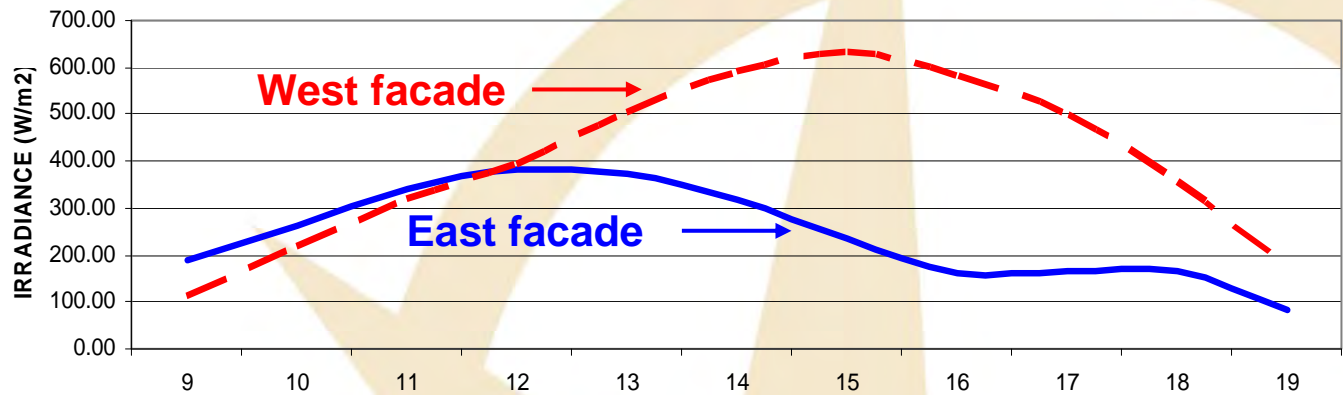




# Irradiance data

## Irradiance data from weather station

### Summer irradiance



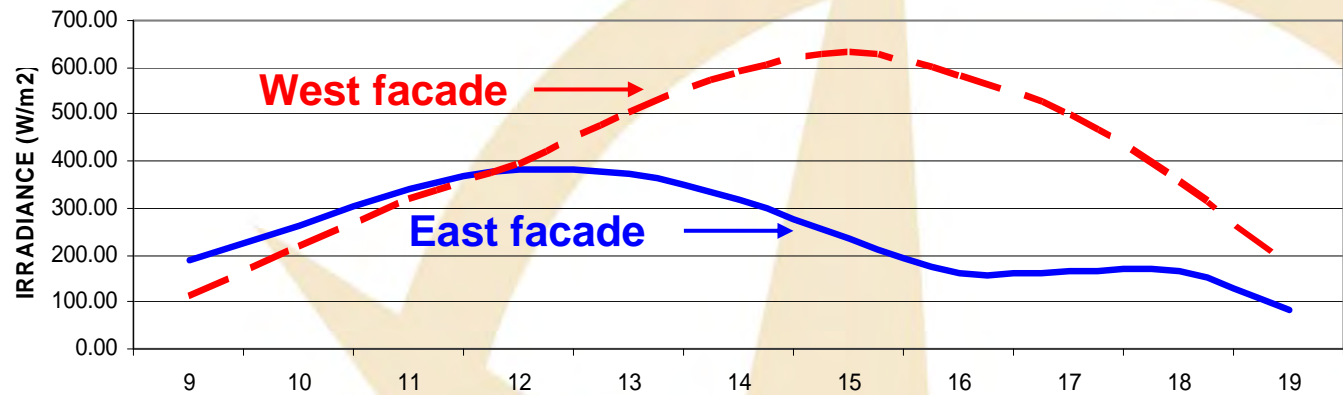
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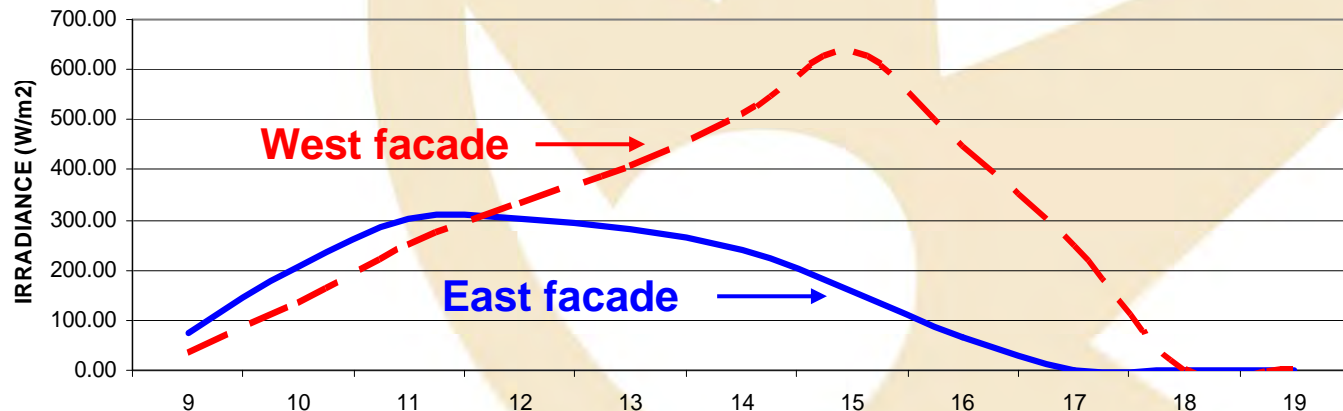
# Irradiance data

## Irradiance data from weather station

### Summer irradiance



### Winter irradiance



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# Simulation scenarios

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## ▣ Modelling taking into account:



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## ▣ Modelling taking into account:

- Time of the day
  - Morning (9.00 am to 12.00 m)
  - Noon (12.00 m to 4.00 pm)
  - Later (4.00 pm to 7.00 pm)

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- Weather season
  - Summer
  - Winter
- Existence or not of air conditioning
- Number of persons
  - 1,2,5 and 10 persons.

# Irradiance curve fitting

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- ❑ Mathematical model fitted to the initial data in order to be introduced in Comsol.
- ❑ Polynomial curves.



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## Summer irradiance

### East facade

$$5.74 \cdot 10^{-5} x^9 - 2.11 \cdot 10^{-3} x^8 + 0.027 x^7 - 0.13 x^6 - 0.0894 x^5 + 2.8178 x^4 - 11.4836 x^3 + 19.675 x^2 + 68.0458 x + 106.835$$

### West facade

$$2.467 \cdot 10^{-4} x^9 - 0.0115 x^8 + 0.219 x^7 - 2.146 x^6 + 11.227 x^5 - 28.553 x^4 + 18.761 x^3 + 44.859 x^2 + 38.910 x + 23.081$$

# Irradiance curve fitting

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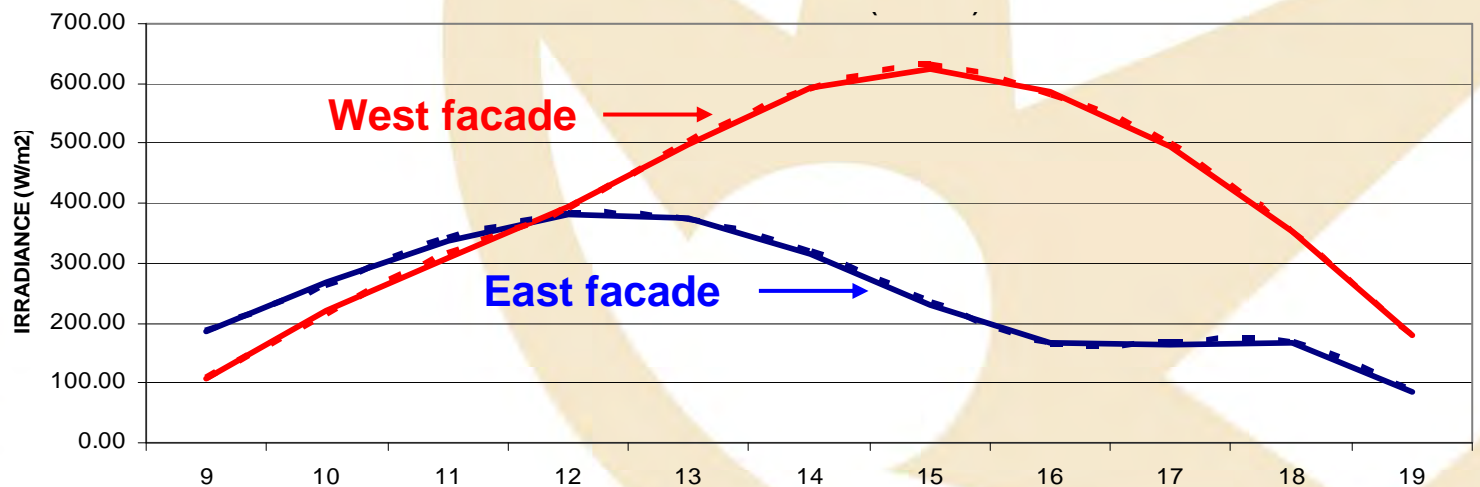
## Summer irradiance

### East facade

$$5.74 \cdot 10^{-5} x^9 - 2.11 \cdot 10^{-3} x^8 + 0.027 x^7 - 0.13 x^6 - 0.0894 x^5 + 2.8178 x^4 - 11.4836 x^3 + 19.675 x^2 + 68.0458 x + 106.835$$

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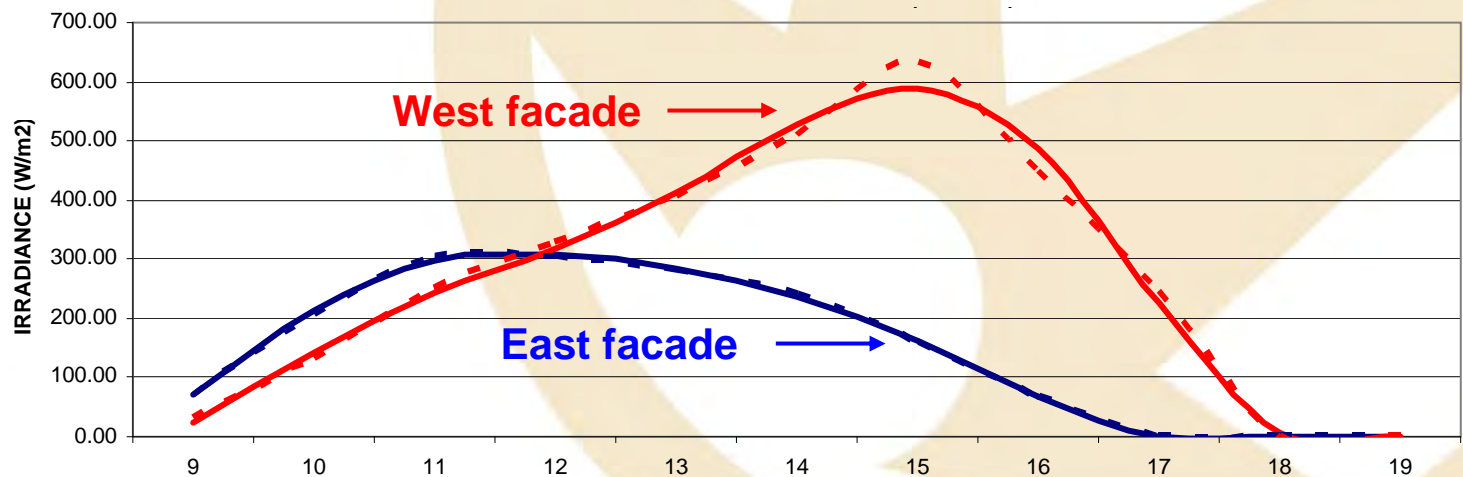
## Winter irradiance

### East facade

$$1.598 \cdot 10^{-4} x^9 - 0.008 x^8 + 0.177 x^7 - 1.965 x^6 + 11.912 x^5 - 36.571 x^4 + 33.981 x^3 + 54.017 x^2 + 23.841 x - 14.832$$

### West facade

$$-6.39 \cdot 10^{-5} x^9 + 8.99 \cdot 10^{-4} x^8 + 0.026 x^7 - 0.762 x^6 + 6.463 x^5 - 24.772 x^4 + 30.239 x^3 + 37.999 x^2 - 5.974 x - 30.031$$



# Restrictions and boundary conditions approach

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- **Restrictions and b. c. approach.**
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## ☐ Comsol approach

- Heat transfer module (3D)
  - Fluid-thermal interaction
    - Turbulent Non-isothermal Flow,  $k - \epsilon$ 
      - General heat transfer (htgh)
      - $k - \epsilon$  Turbulence Model (chns)

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- Subdomain settings, (chns and htgh)

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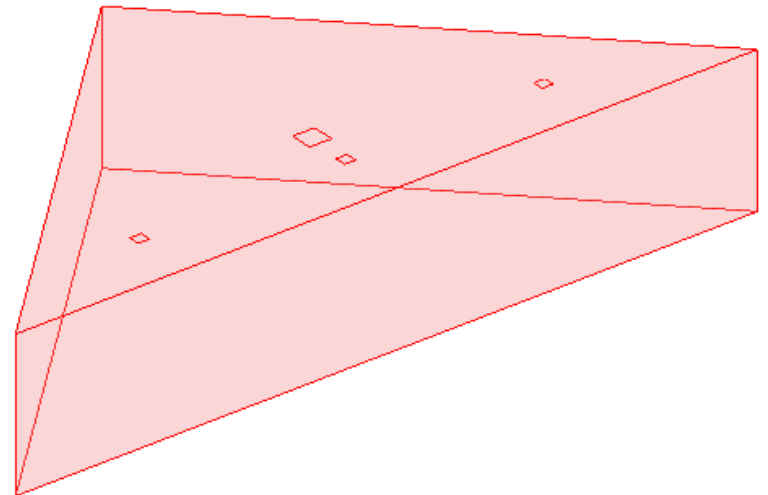
## ☐ Comsol approach

- Subdomain settings, (chns and htgh)

Air (**library material**)

$\rho$  ( $p_0[1/\text{Pa}]$ ,  $T_f[1/\text{K}]$ ) [ $\text{kg}/\text{m}^3$ ] (**density**)

$\eta$  ( $T_f[1/\text{K}]$ ) [ $\text{Pa}\cdot\text{s}$ ] (**dynamic viscosity**)



# Restrictions and boundary conditions approach

## Comsol approach

- Subdomain settings, (chns and htgh)

Air (**library material**)

rho (p0[1/Pa], Tf[1/K]) [kg/m<sup>3</sup>] (**density**)

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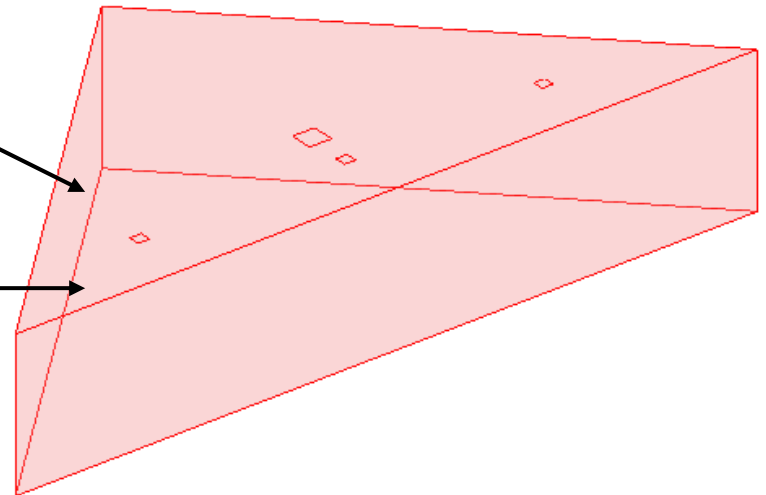
**chns**

Stabilization

**htgh**

Convection

Init. Value Tf(t<sub>0</sub>)



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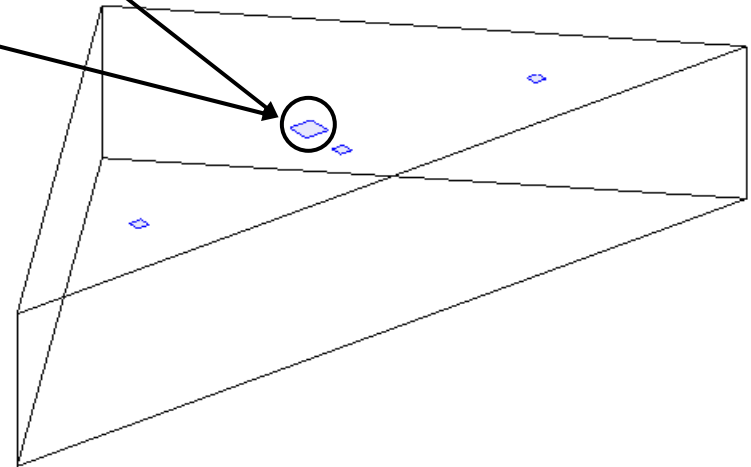
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## ☐ Comsol approach

- Boundary settings, **chns**

**Boundary type:**  
Inlet

**Boundary cond.:**  
Velocity  
 $U_0, L_T, I_T$



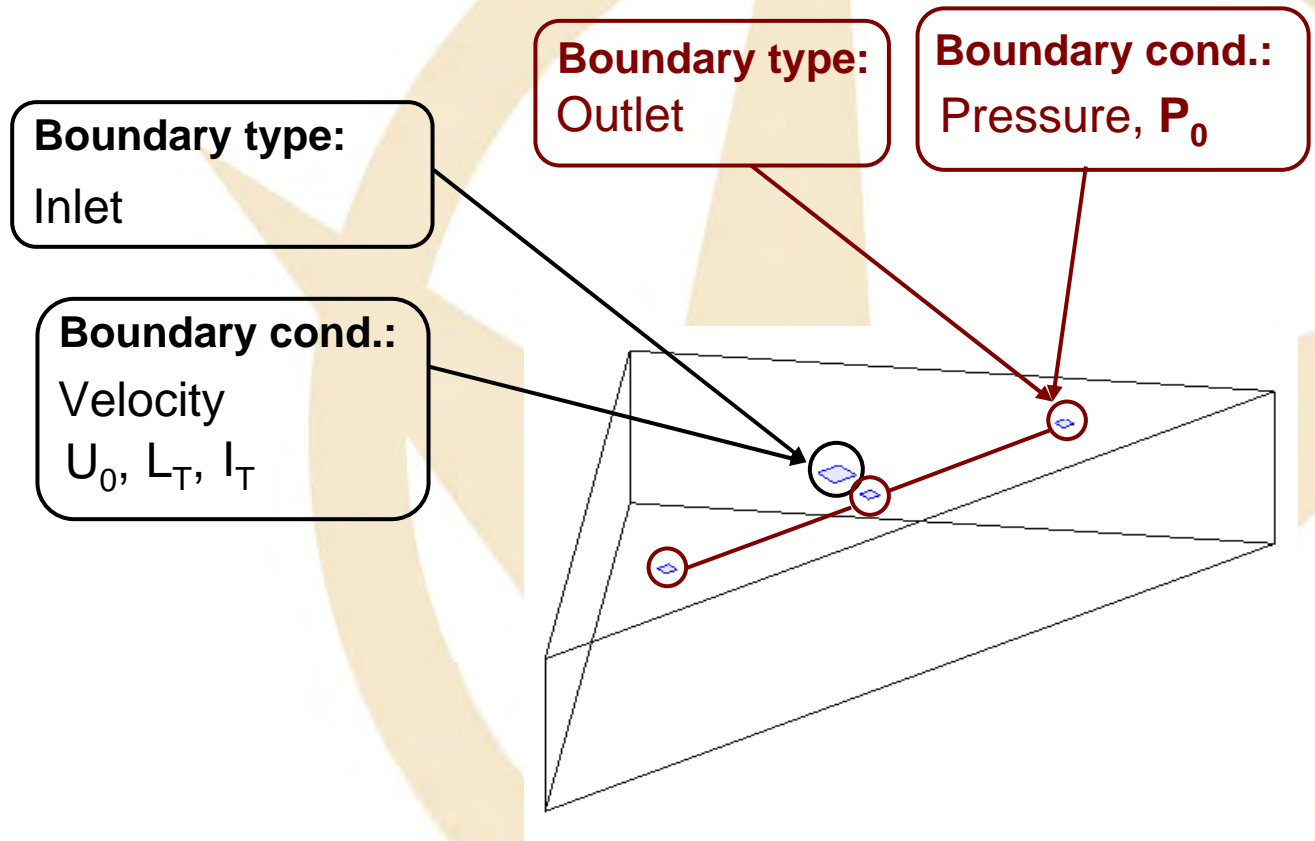


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- Boundary settings, **chns**

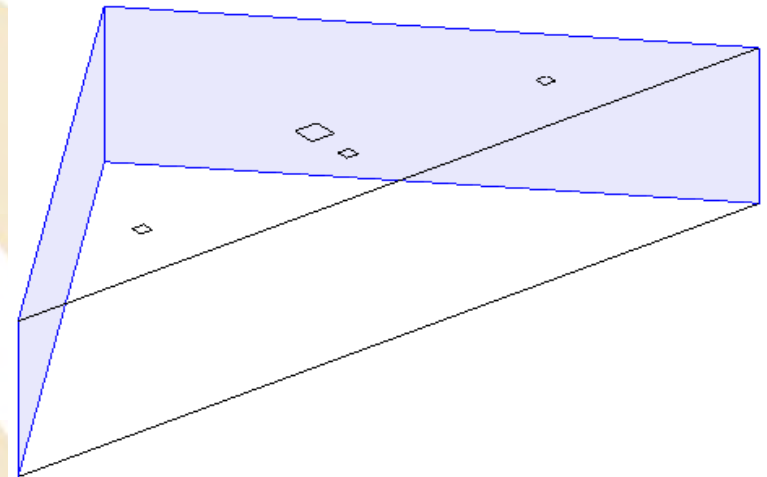


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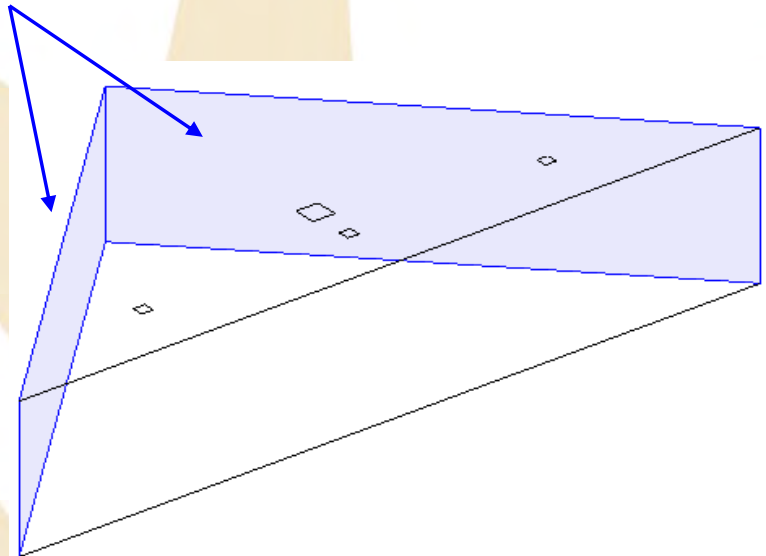
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## ☐ Comsol approach

- Boundary settings, **htgh**

**Boundary cond.:**  
Heat flux  
 $q_0 = \text{fitted curves}$

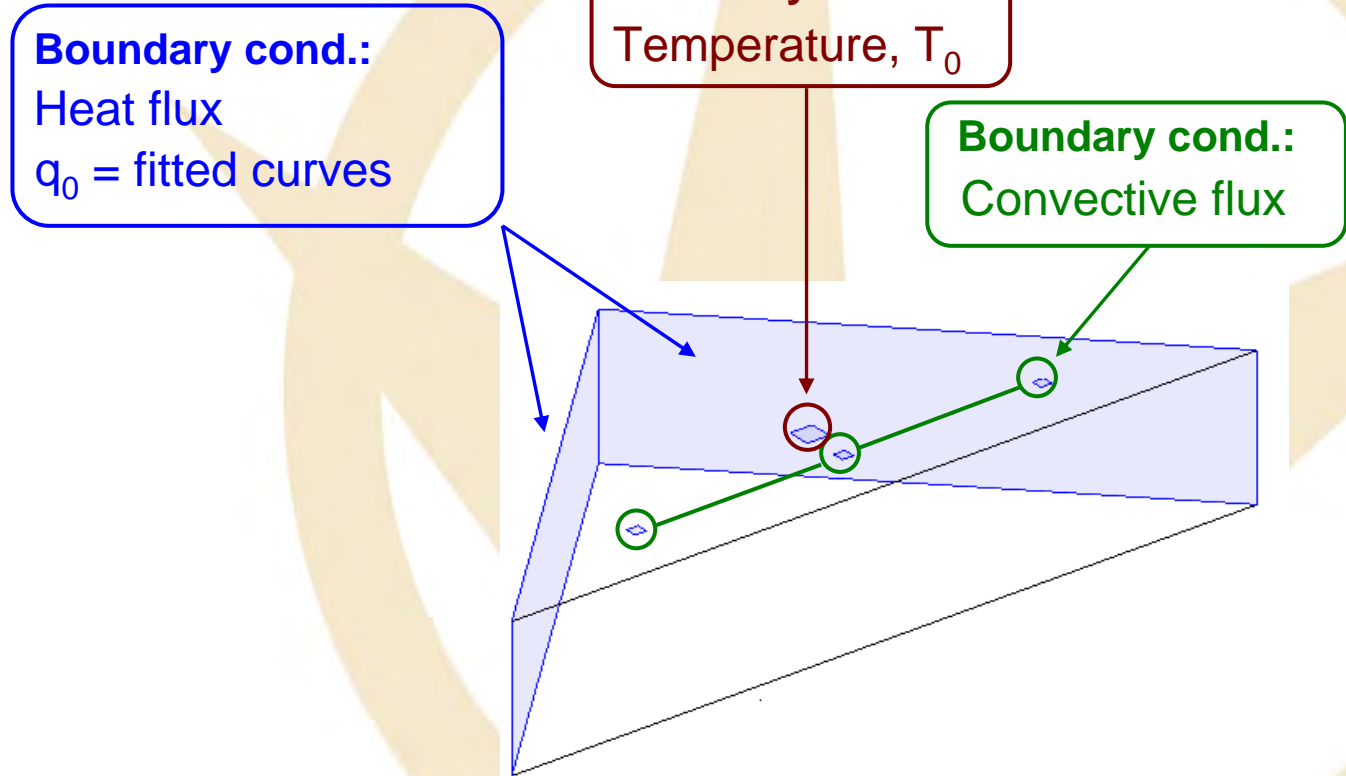


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# Restrictions and boundary conditions approach

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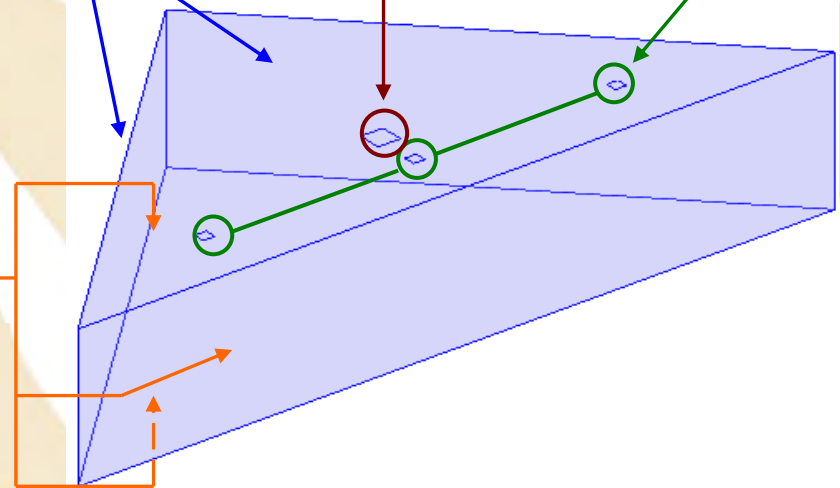
- Boundary settings, **htgh**

**Boundary cond.:**  
Heat flux  
 $q_0 = \text{fitted curves}$

**Boundary cond.:**  
Temperature,  $T_0$

**Boundary cond.:**  
Convective flux

**Boundary cond.:**  
 $q_0, T_0$



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# Restrictions and boundary conditions approach

## Comsol approach

### Differential equations

$$\frac{\partial \rho}{\partial t} + \frac{\partial(\rho u)}{\partial x} + \frac{\partial(\rho v)}{\partial y} + \frac{\partial(\rho w)}{\partial z}$$

$$\rho a_y = \rho F_y - \frac{\partial p}{\partial y} + \frac{\partial}{\partial y} \left( 2\mu \frac{\partial v}{\partial y} + \left( \zeta - \frac{2}{3} \mu \right) \nabla^T \bar{\mathbf{u}} \right) + \frac{\partial}{\partial z} \left( \mu \left( \frac{\partial v}{\partial z} + \frac{\partial w}{\partial y} \right) \right) + \frac{\partial}{\partial x} \left( \mu \left( \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y} \right) \right)$$

$$\rho a_x = \rho F_x - \frac{\partial p}{\partial x} + \frac{\partial}{\partial x} \left( 2\mu \frac{\partial u}{\partial x} + \left( \zeta - \frac{2}{3} \mu \right) \nabla^T \bar{\mathbf{u}} \right) + \frac{\partial}{\partial y} \left( \mu \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) \right) + \frac{\partial}{\partial z} \left( \mu \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right) \right)$$

$$\rho a_z = \rho F_z - \frac{\partial p}{\partial z} + \frac{\partial}{\partial z} \left( 2\mu \frac{\partial w}{\partial z} + \left( \zeta - \frac{2}{3} \mu \right) \nabla^T \bar{\mathbf{u}} \right) + \frac{\partial}{\partial x} \left( \mu \left( \frac{\partial w}{\partial x} + \frac{\partial u}{\partial z} \right) \right) + \frac{\partial}{\partial y} \left( \mu \left( \frac{\partial w}{\partial y} + \frac{\partial v}{\partial z} \right) \right)$$

$$\frac{\partial}{\partial x} \left( k \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left( k \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z} \left( k \frac{\partial T}{\partial z} \right) + \frac{\partial Q}{\partial t} + \Phi_d - \nabla^T \bar{\mathbf{q}}_r =$$

$$\frac{\partial}{\partial x} (\rho u) + \frac{\partial}{\partial y} (\rho v) + \frac{\partial}{\partial z} (\rho w) + \frac{\rho}{2} \frac{D}{Dt} (u^2 + v^2 + w^2) + \rho \frac{DE}{Dt}$$

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# Finite Element mesh

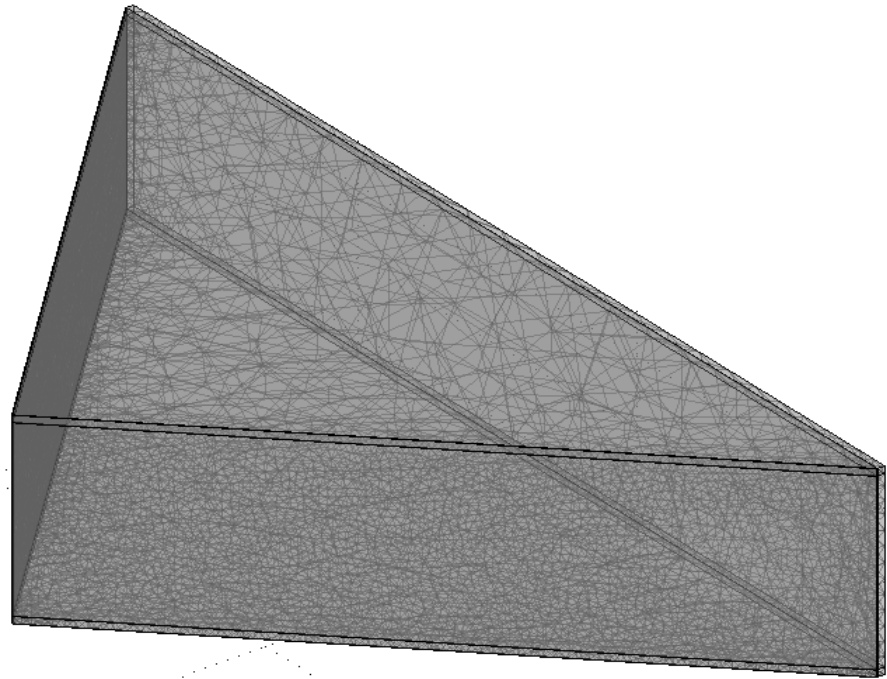
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## ▣ Enclosure's Finite Elements mesh

Tetrahedral elements

60883 elements

99069 dof



## Results. Experimental validation

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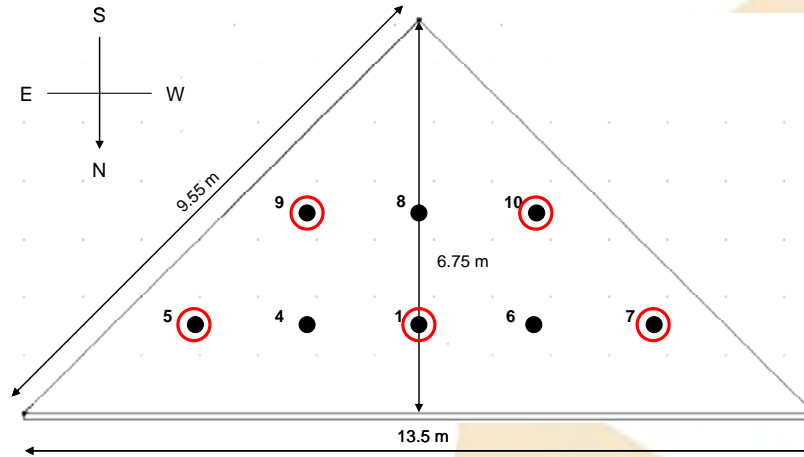
- ▣ Temperature comparissons at reference points.



## Results. Experimental validation

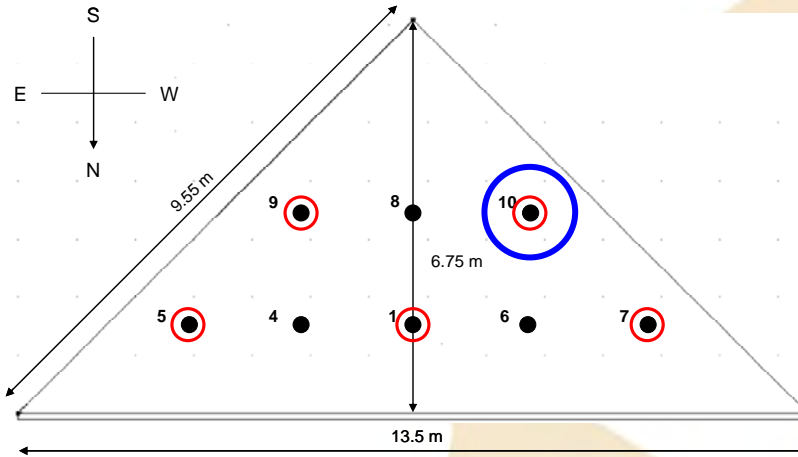
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### ☐ Temperature comparisons at reference points.

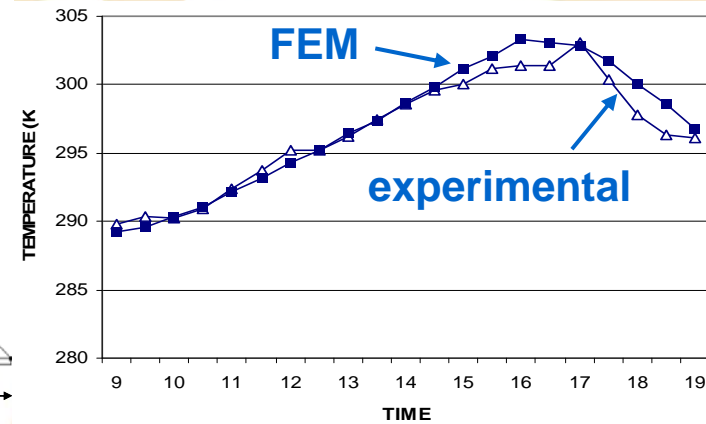


# Results. Experimental validation

## Temperature comparisons at reference points.



### point 10

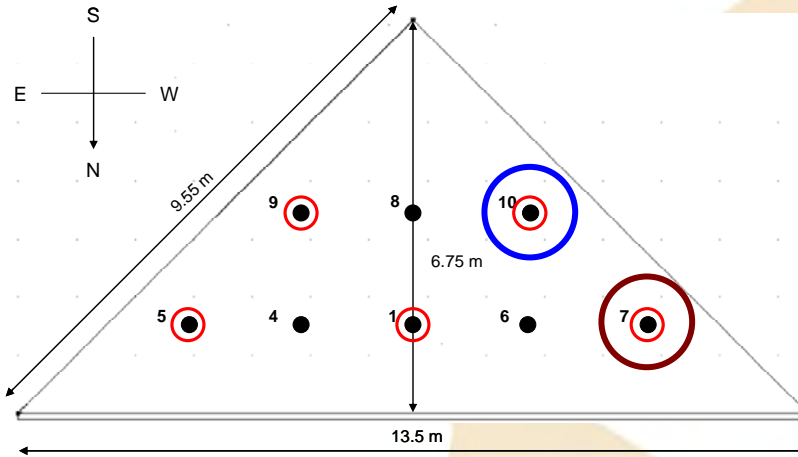


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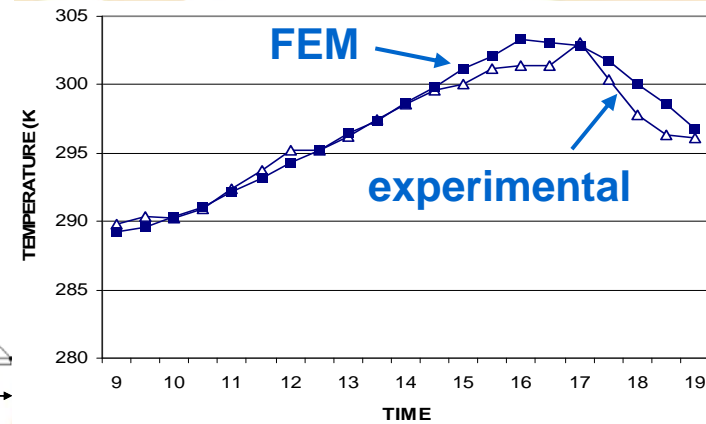
# Results. Experimental validation

## Temperature comparisons at reference points.

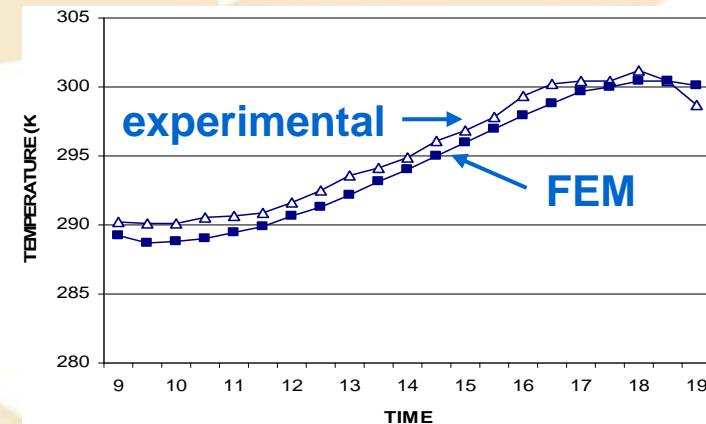


Good approximation between experimental results and FEM

### point 10



### point 7

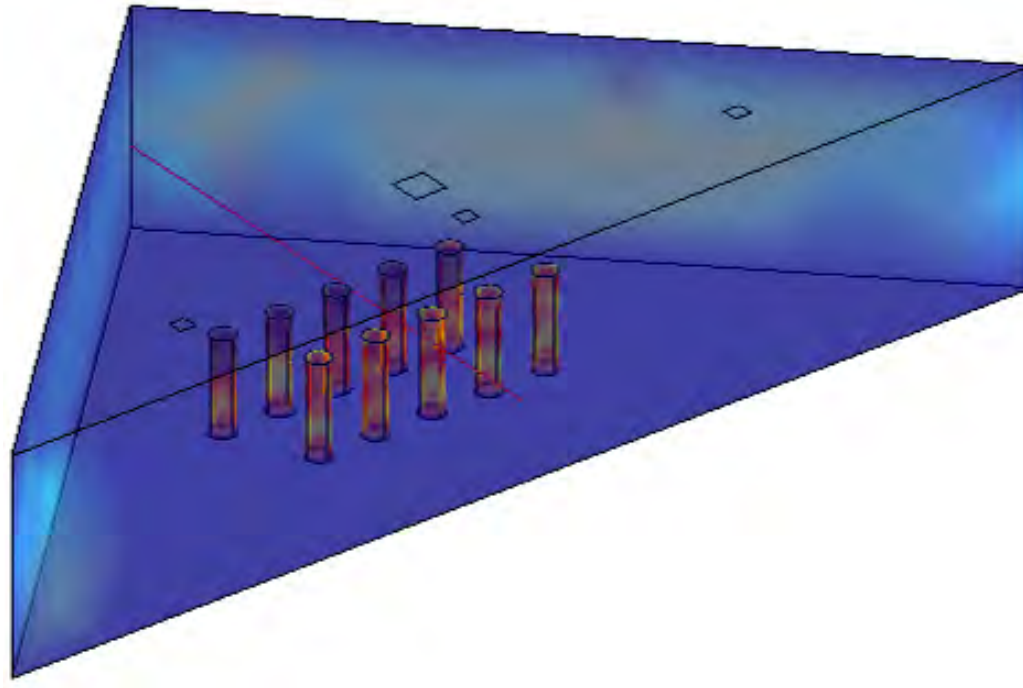


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## Results. Temperature evolution

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- ▣ Temperature distribution of the enclosure. Ten people



# Results. Temperature evolution

## ▣ Temperature evolution. Summer.

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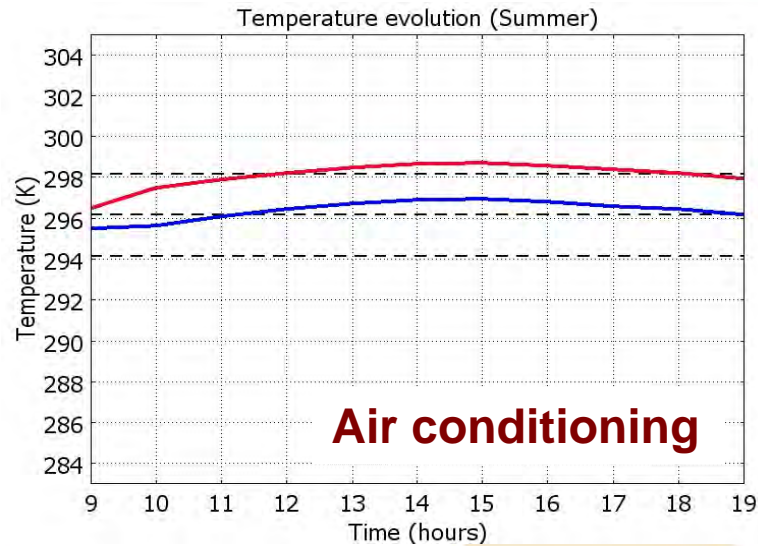
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## Results. Temperature evolution

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- Simulation scenarios.
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- Restrictions and b. c. approach.
- Finite Element mesh.
- **Results.**
- Conclusions

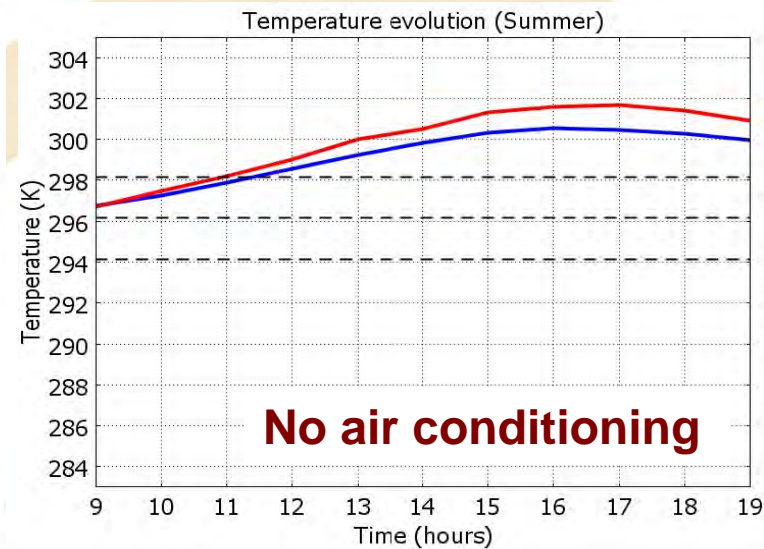
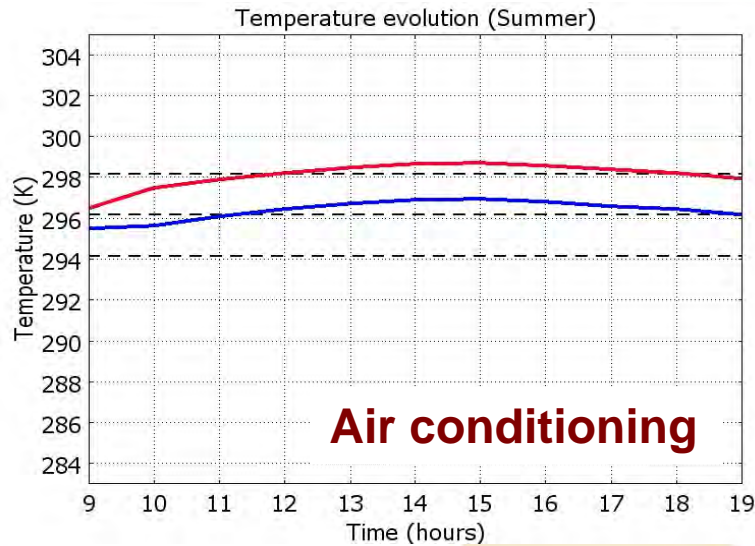
### ☐ Temperature evolution. Summer.



# Results. Temperature evolution

## Temperature evolution. Summer.

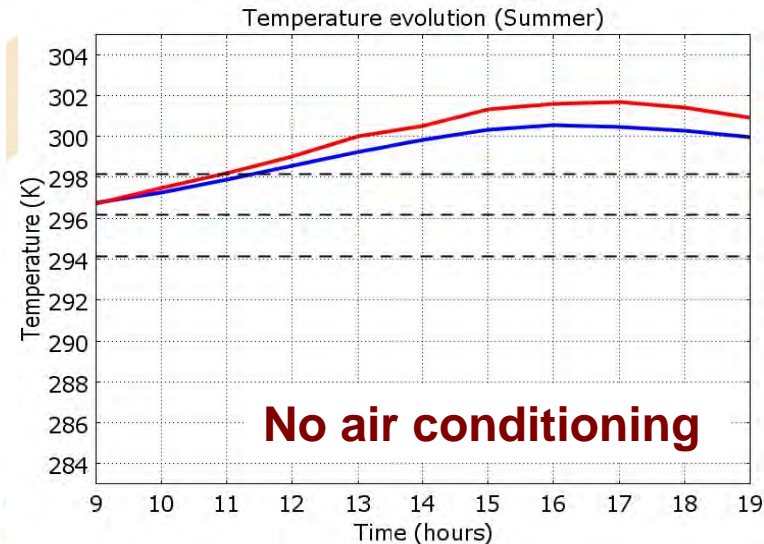
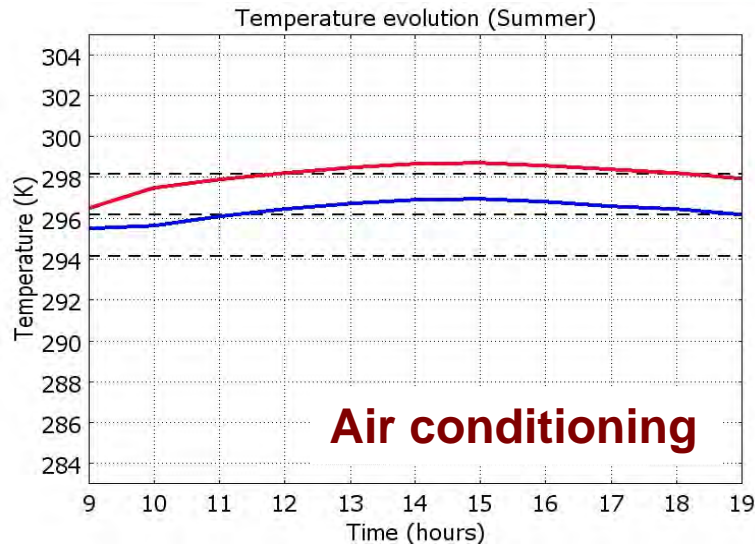
- Introduction & objectives.
- Construction details.
- Irradiance data.
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- Finite Element mesh.
- **Results.**
- Conclusions



— 0 people — 10 people

## Results. Temperature evolution

### Temperature evolution. Summer.



— 0 people — 10 people

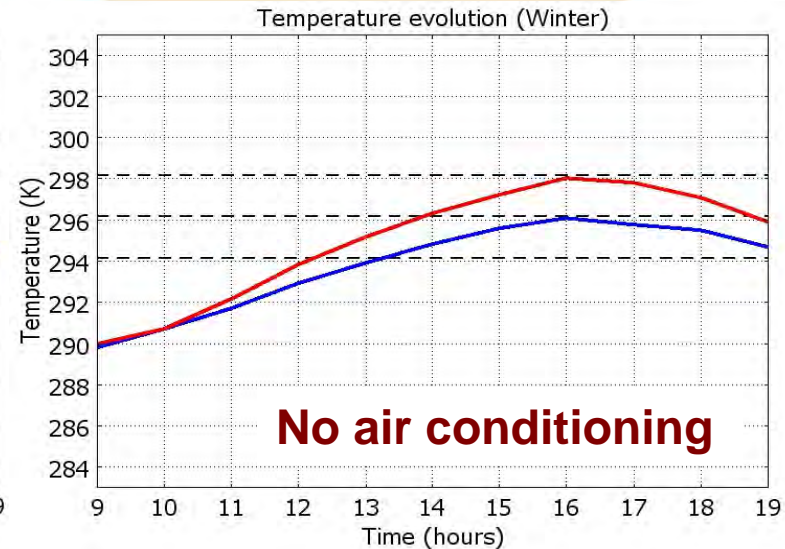
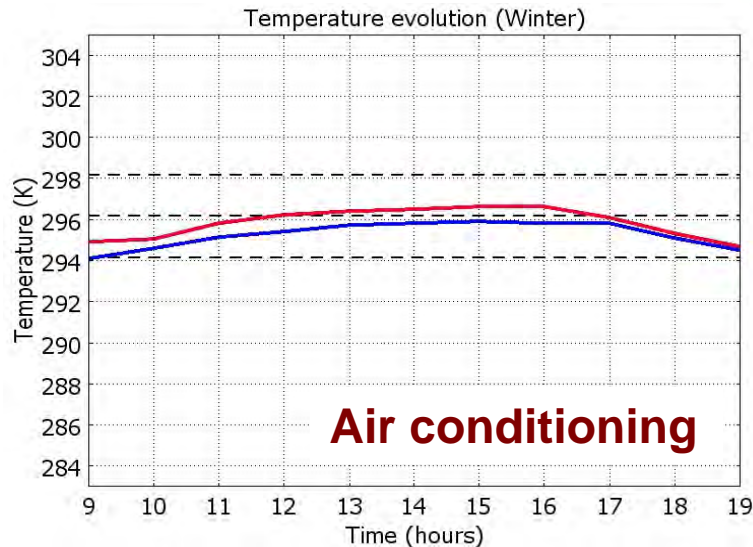
- Enclosure's temperature 10 people > enclosure's temp. 0 people
- The trend of the temperature evolution is similar to the irradiance curve.
- With air conditioning the temperature remains within the comfort range.

- Introduction & objectives.
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## Results. Temperature evolution

### Temperature evolution. Winter.



— 0 people — 10 people

- The trend of the temperature evolution is similar to the irradiance curve.
- With air conditioning the temperature remains within the comfort range.

- Introduction & objectives.
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## Conclusions

- Introduction & objectives.
- Construction details.
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- Results.
- **Conclusions**

- ❑ Influence of the irradiance in the temperature evolution into the enclosure.
- ❑ Setting the irradiance curves to assign a heat source to modelling in Comsol.
- ❑ Good approximation between experimental and numerical results.
- ❑ Trend of the temperature evolution similar to the irradiance curve.

# Thermal modelling for the implementation of an energetic efficiency control system in a room of meetings of singular geometry

Thanks !



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