



# Calculation of HF Eigenmodes in Liquid Rocket Combustion Chambers

COMSOL Application  
R. Kaess, J. Braun, S. Koeglmeier

**1**

**Thermo-Acoustic Combustion Instability in Rocket Engines**

**2**

**Comsol Calculation**

**3**

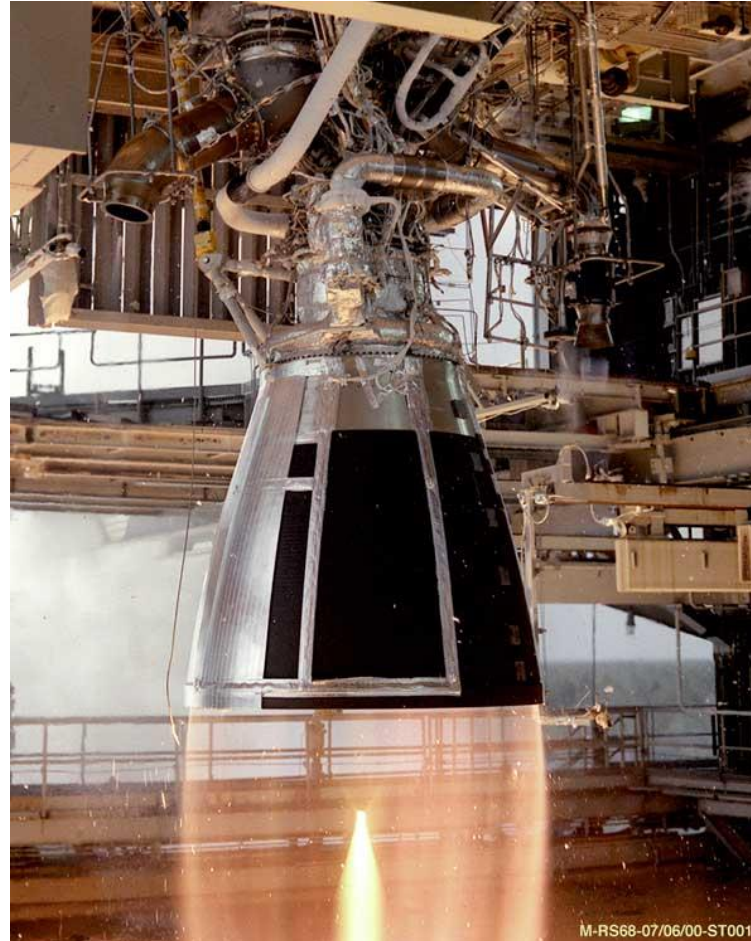
**Summary**



# 1 Thermo-Acoustic Combustion Instability in Rocket Engines

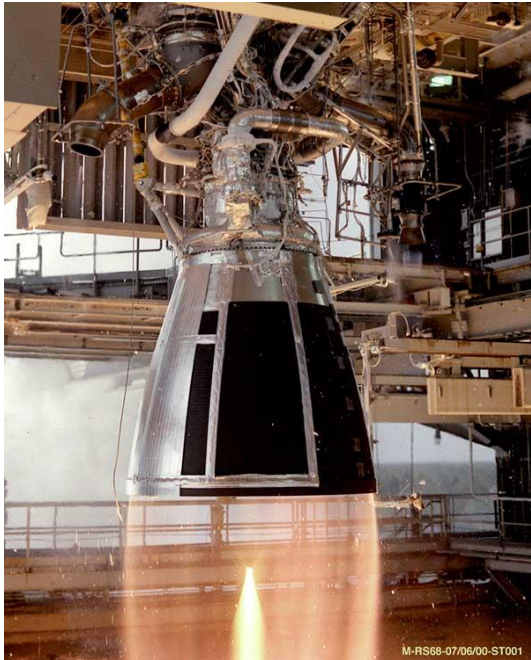


How does it work?



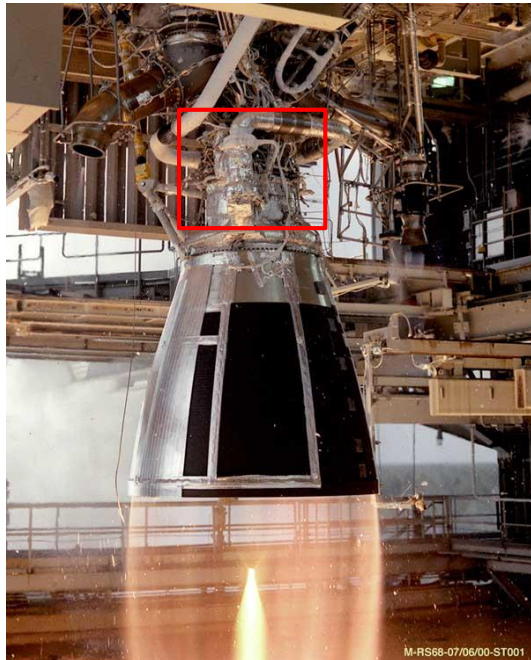
[http://www.nasa.gov/images/content/148709main\\_d4\\_testing\\_08.jpg](http://www.nasa.gov/images/content/148709main_d4_testing_08.jpg), (accessed on 07.09.2016)

# Rocket Engines



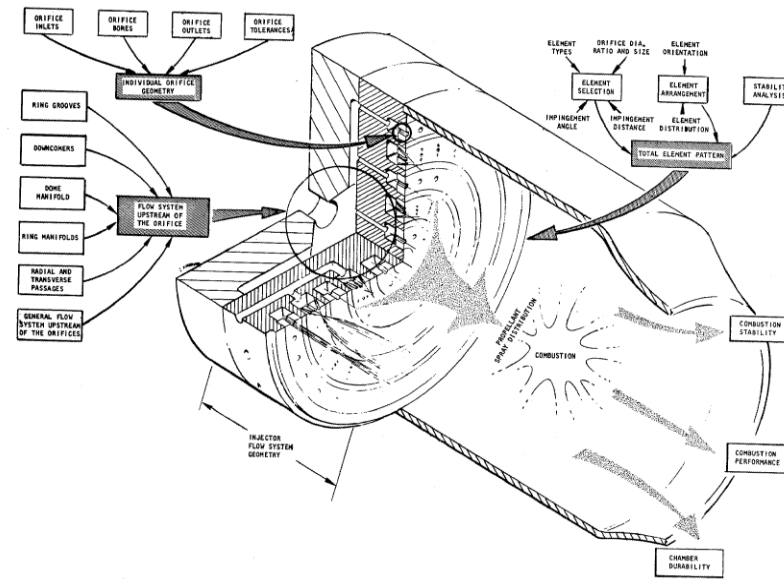
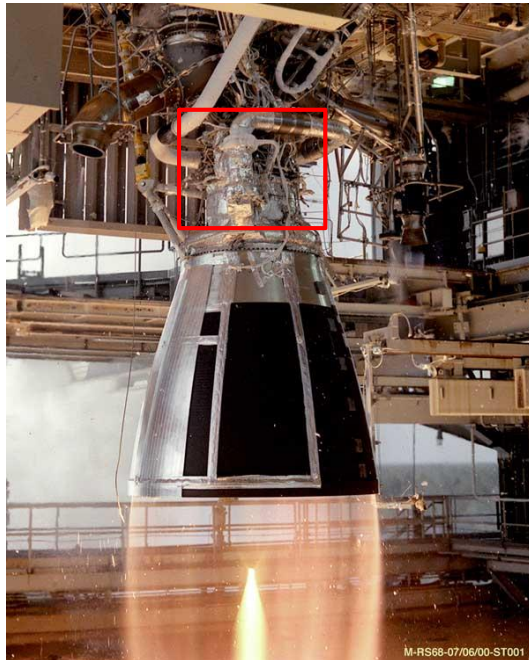
[http://www.nasa.gov/images/content/148709main\\_d4\\_testing\\_08.jpg](http://www.nasa.gov/images/content/148709main_d4_testing_08.jpg), (accessed on 07.09.2016)

# Rocket Engines



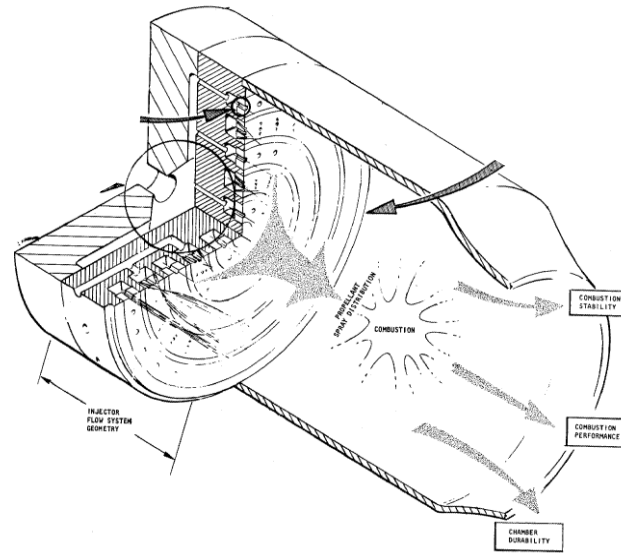
[http://www.nasa.gov/images/content/148709main\\_d4\\_testing\\_08.jpg](http://www.nasa.gov/images/content/148709main_d4_testing_08.jpg), (accessed on 07.09.2016)

# Rocket Engines



[http://www.nasa.gov/images/content/148709main\\_d4\\_testing\\_08.jpg](http://www.nasa.gov/images/content/148709main_d4_testing_08.jpg), (accessed on 07.09.2016)



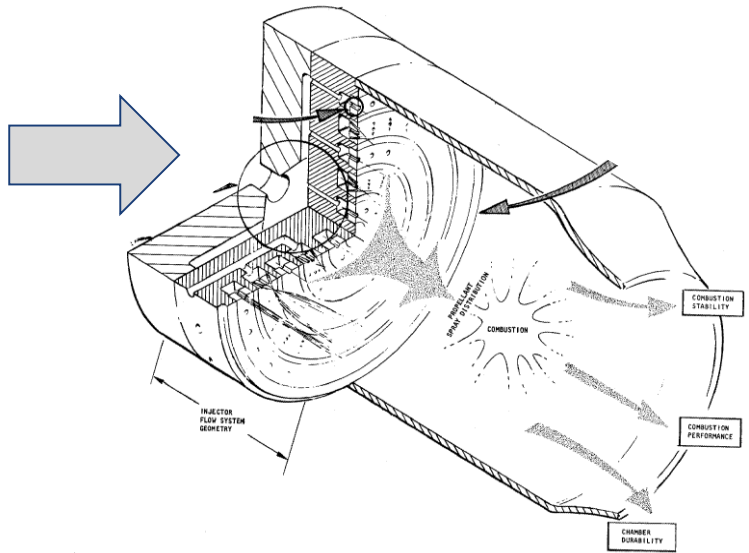


[http://www.nasa.gov/images/content/148709main\\_d4\\_testing\\_08.jpg](http://www.nasa.gov/images/content/148709main_d4_testing_08.jpg), (accessed on 07.09.2016)





## Flowrates and Pressure Levels



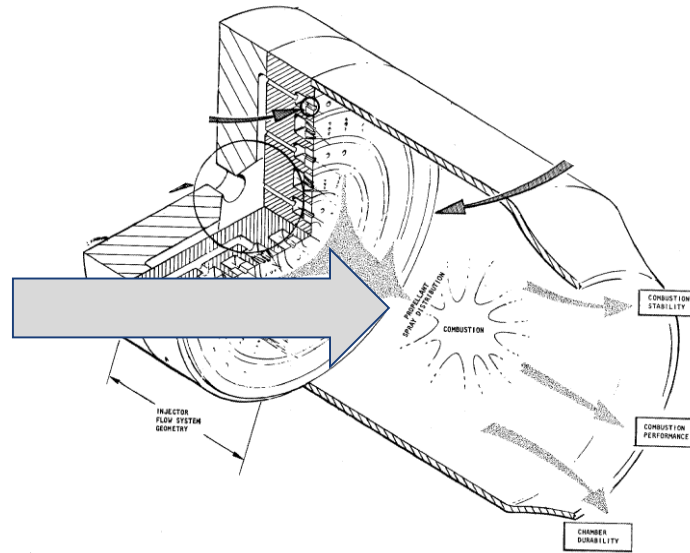
Jet d'eau, Geneve: 500l/s, 16bar, 140m



## Thermal Power

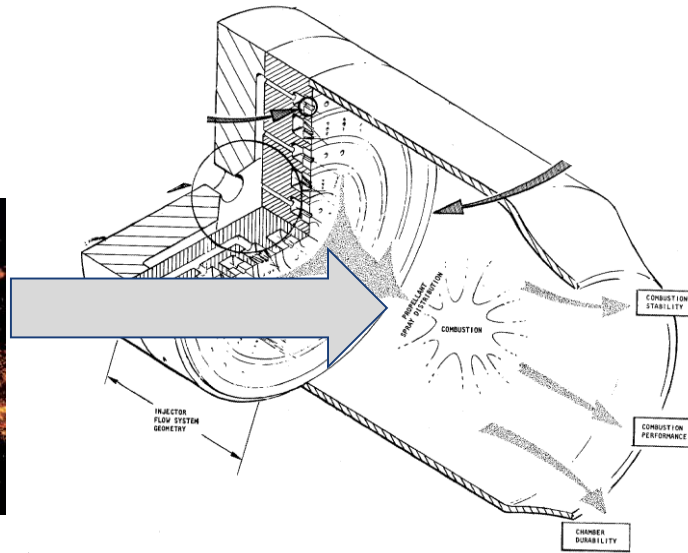


Neckarwestheim: 1400 MW





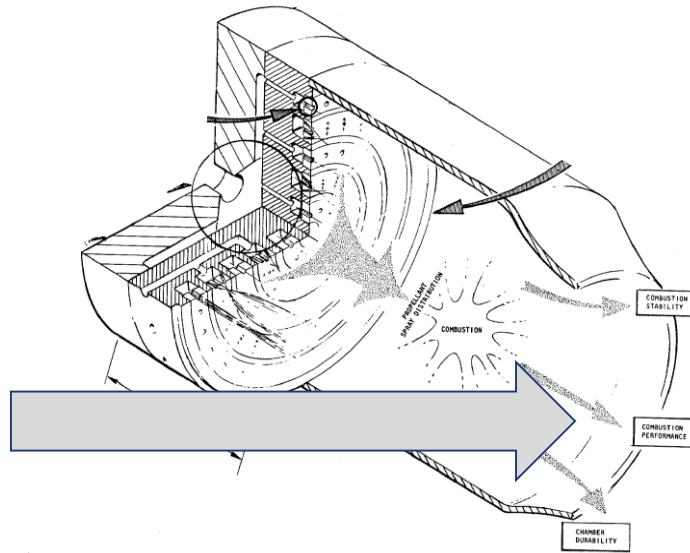
## Temperatures



2 x Melting Point of Steel



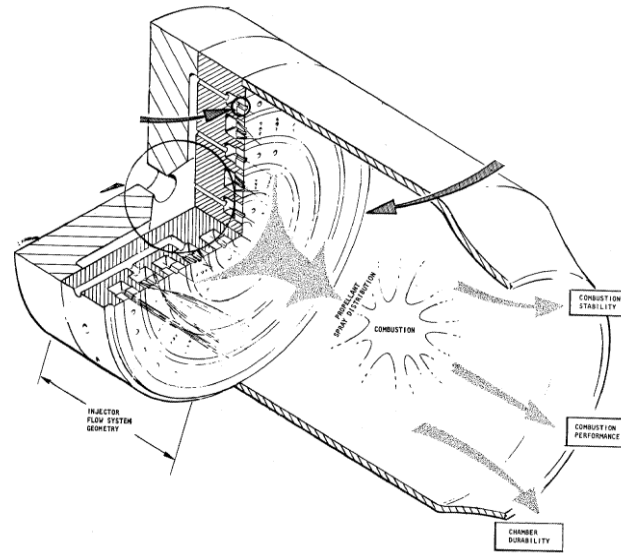
## Velocities



Approx. 4000m/s → 4 x A12 maximum speed



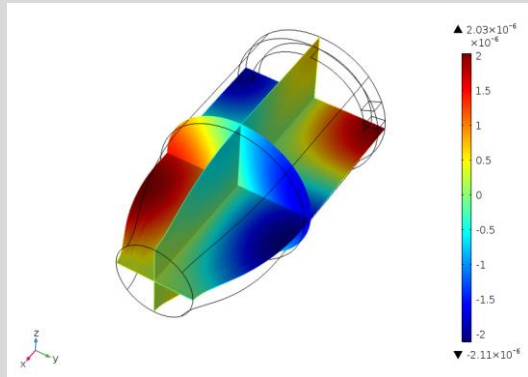
- Application at the physical limits
- Large quantities of energy present
- Limited margins against failures
- Small deviations can have catastrophic effects



➔ Need for a safe, smooth, robust mode of operation

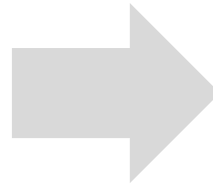
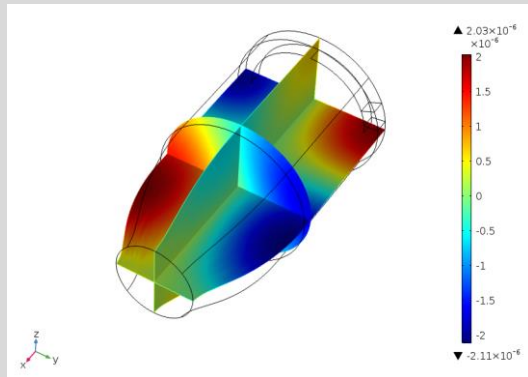


Combustion chamber  
acoustics conserve  
pressure and velocity  
fluctuations

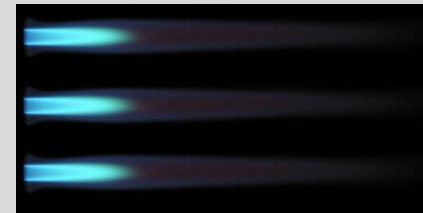




Combustion chamber acoustics conserve pressure and velocity fluctuations



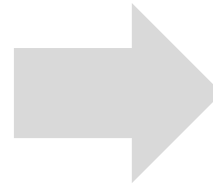
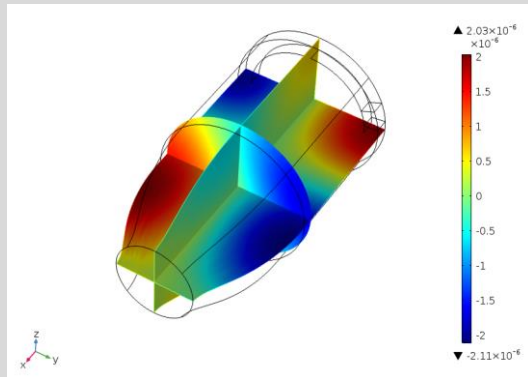
Combustion process is sensitive to pressure and velocity fluctuations



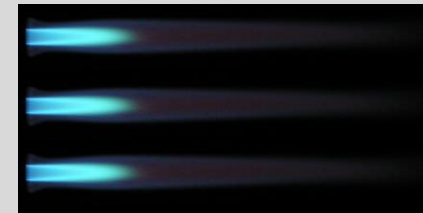




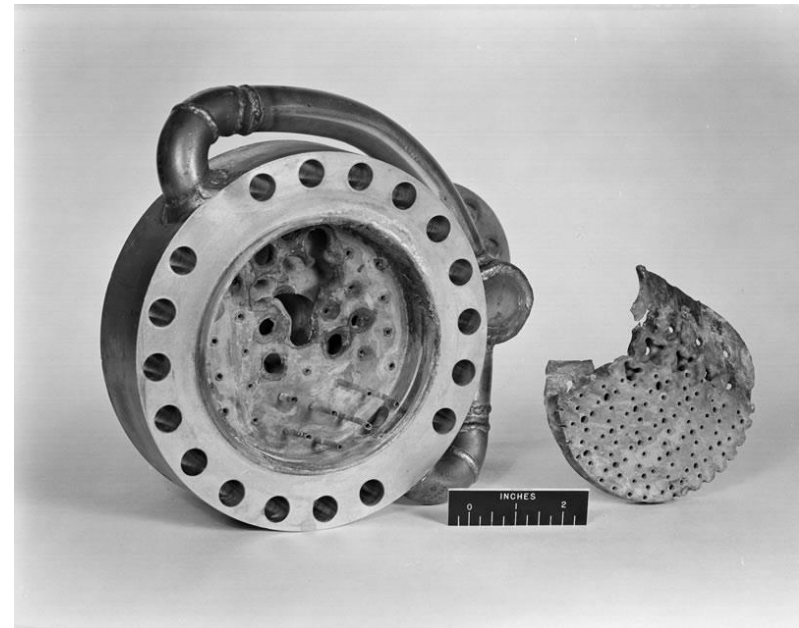
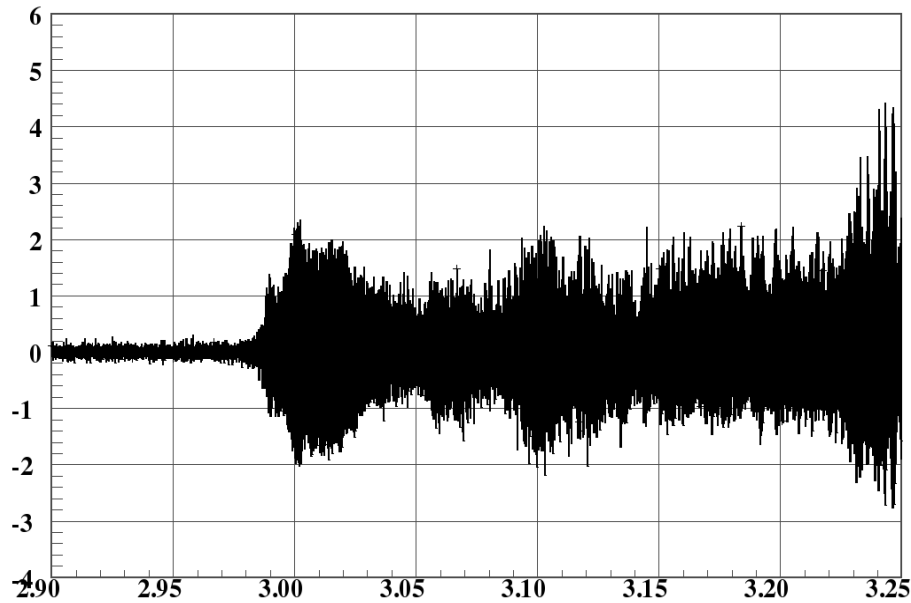
Combustion chamber acoustics conserve pressure and velocity fluctuations



Combustion process is sensitive to pressure and velocity fluctuations



Fluctuating combustion induces heat release fluctuations and pressure fluctuations



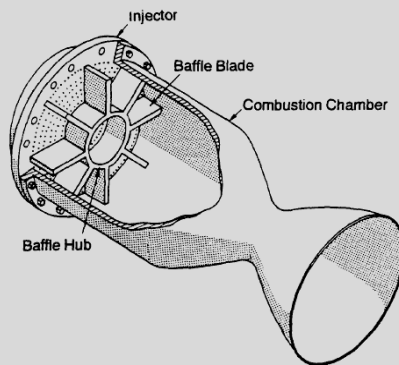
Combustion instability oscillating in the combustion chambers acoustic eigenmodes



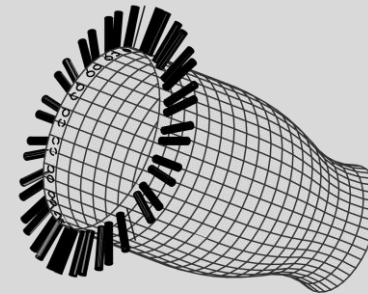
Influence parameters and counter-measures:

- Combustion chamber geometry and hot gas determine the eigenfrequencies
- Propellant combination has tremendous influence on the risk of instabilities
- Proper design of Injection system reduces risk
- Stabilization devices can be used

Baffles:  
protect the flame and provide damping



Acoustic absorbers/liners:  
provide damping at their tuning frequency



Knowledge of the acoustic eigenfrequencies is required

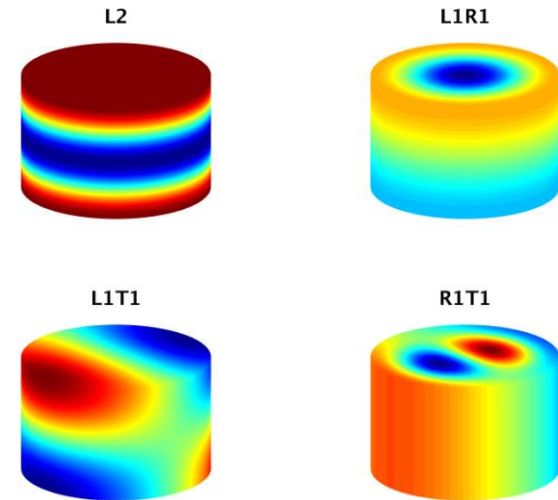
# 1 / Can COMSOL predict the combustion chamber eigenfrequencies?



Evaluation of off-the-shelf-COMSOL modules w/o modifications

Features to be considered

- Presence of mean flow (non-negligible Ma-Number)
- Presence of gradients
- (Presence of absorbers or baffles)



Stepwise approach with increasing complexity

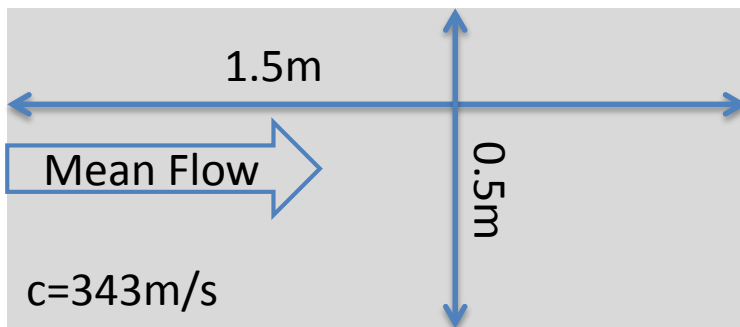
The results have been de-dimensionalized for confidentiality reasons



# 2 Comsol Calculations



### Eigenfrequencies of a 2D Duct with and w/o mean flow



Analytic solution:

$$\omega_{lm} = c\pi \sqrt{\left(\frac{l}{L}\right)^2 + \left(\frac{m}{H}\right)^2} = c\sqrt{\alpha_l^2 + \beta_m^2}$$

| Eigen mode | Analytic solution |       |
|------------|-------------------|-------|
| Mach       | 0                 | 0.2   |
| L1         | 114.3             | 109.8 |
| L2         | 228.7             | 219.5 |
| L3         | 343.0             | 329.3 |
| T1L1       | 361.6             |       |
| T1L2       | 412.2             |       |



### Eigenfrequencies of a 2D Duct with and w/o mean flow

Physics module:

*Linear Euler, Frequency Domain*

Acoustic source:

*Domain Source*

Study:

*Frequency Domain*

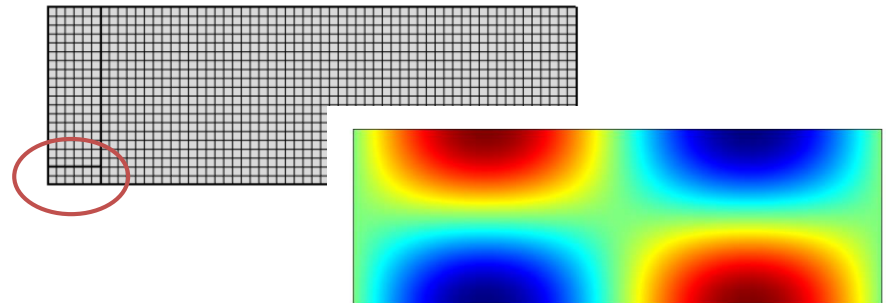
Direct solver: MUMPS

Mesh:

Quadrilateral mapped mesh

Max. element length: 0.025m

| Eigen mode | Analytic solution |       | COMSOL<br>(Step: 0.25Hz) |       |
|------------|-------------------|-------|--------------------------|-------|
|            | 0                 | 0.2   | 0                        | 0.2   |
| Mach       | 0                 | 0.2   | 0                        | 0.2   |
| L1         | 114.3             | 109.8 | 114.3                    | 109.8 |
| L2         | 228.7             | 219.5 | 228.8                    | 219.5 |
| L3         | 343.0             | 329.3 | 343.3                    | 329.5 |
| T1L1       | 361.6             |       | 361.8                    | 353.5 |
| T1L2       | 412.2             |       | 412.5                    | 401.5 |



➔ Set up is correct

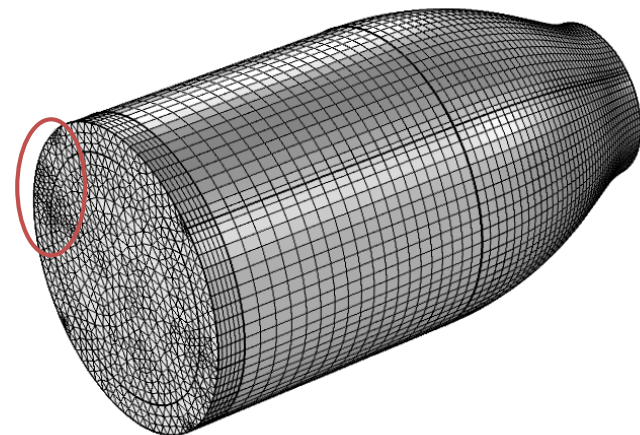
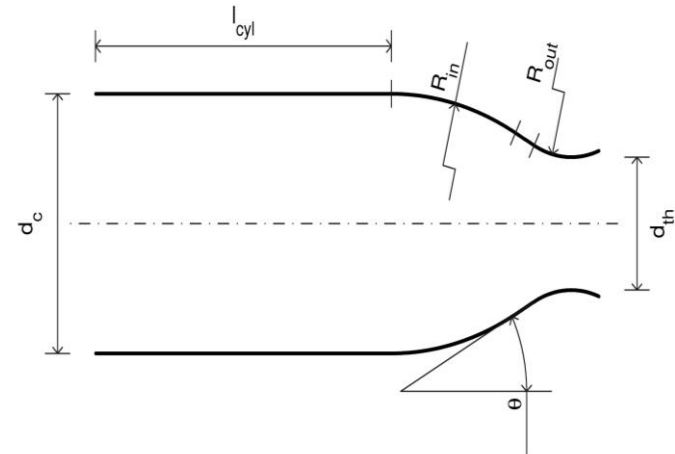




Physics module:  
*Linear Euler, Frequency Domain*

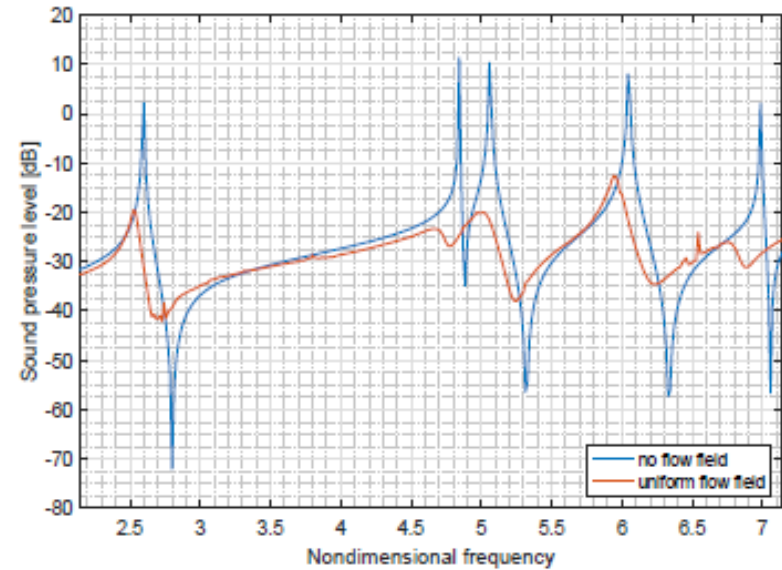
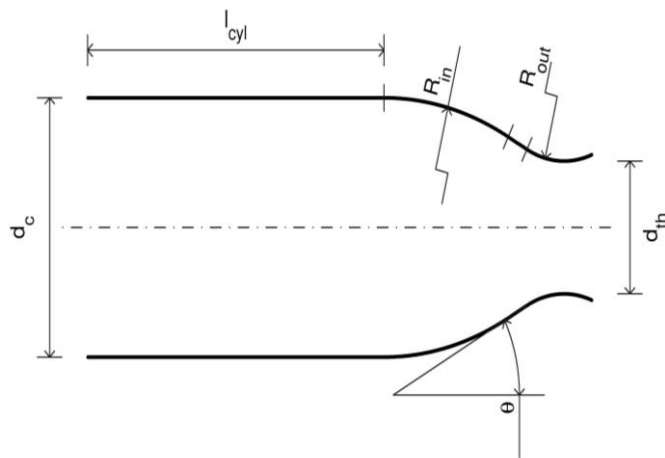
Boundary Conditions:  
Chamber wall and inlet: *Rigid wall*  
Chamber outlet: *Asymptotic far-field radiation + Outflow boundary*

Acoustic source:  
*Domain Source*





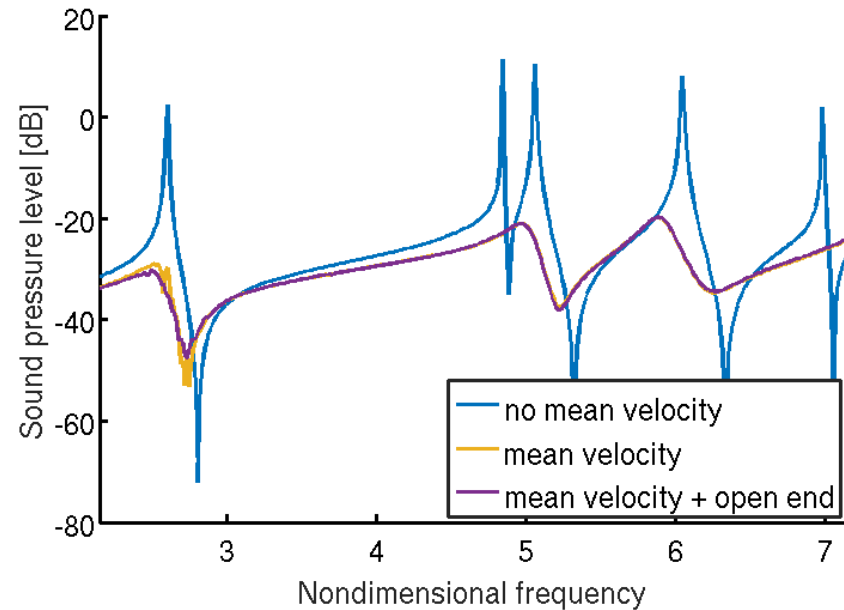
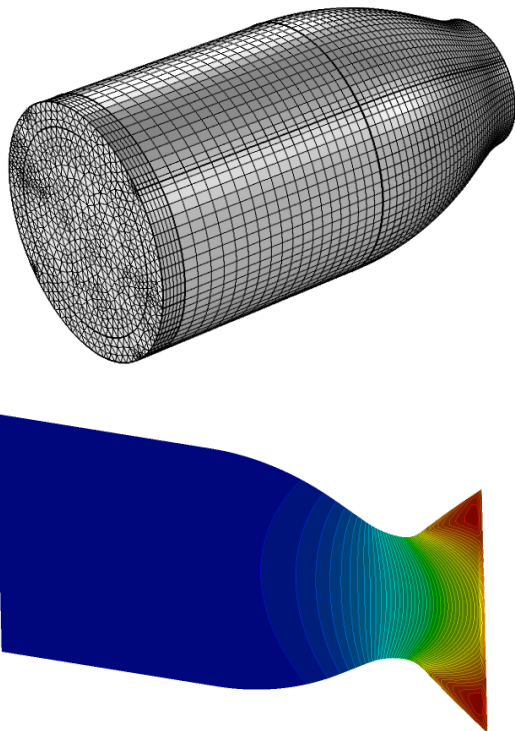
- Zero Mach number and homogeneous medium
- Simple, constant axial velocity (unphysical at nozzle)



Frequency shift and additional damping when mean flow is present



- COMSOL domain is truncated to keep Ma number below 1



→ Damping increases, double peak reduces to single peak, some spurious oscillations



# 3 Summary



- COMSOL has been applied to calculate the acoustic properties of confined domains
- Cases with and without mean flow have been chosen
- The eigenfrequencies can be calculated using a domain source and a frequency sweep
- Mean flow increases damping and promotes spurious oscillations
- Frequency shift for mean flow can be observed