

# Spatiotemporal Study of Thrombosis incorporating Recent Rheological Findings

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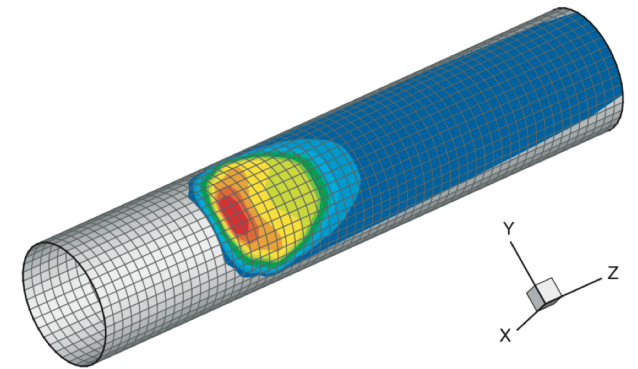
# Motivation

- Hemostasis stops internal bleeding
- Clinical Relevance
  - Under-active -> hemorrhage
  - Over-active -> thrombosis (blood vessel occlusion)
  - Unaddressed thrombosis can lead to heart attack or stroke

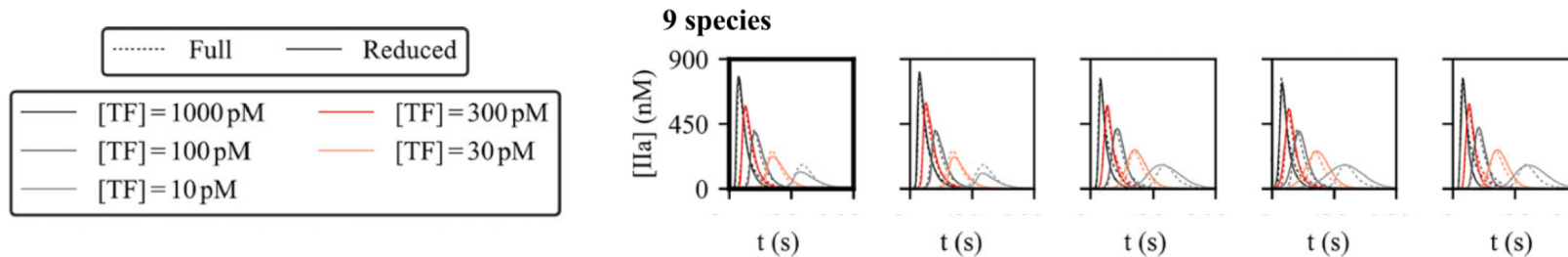


# Background

- Few thrombosis models include rheological feedback
- Variable Viscosity Constitutive Equation
  - Dependence on shear rate and chemical concentration
- Reduced blood coagulation model
  - Optimizes computational cost while capturing kinetics



[2] Bodnár T, Sequeira A. Numerical simulation of the coagulation dynamics of blood. *Computational and Mathematical Methods in Medicine*. 2008 Jun 1;9(2):83-104.

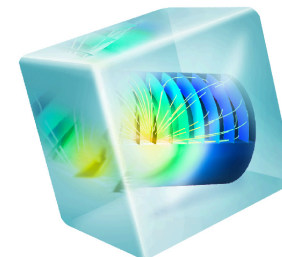


[3] Hansen KB, Shadden SC. Automated reduction of blood coagulation models. *International Journal for Numerical Methods in Biomedical Engineering*. 2019 Oct;35(10):e3220.

# Project Scope

- Build a COMSOL Simulation App to Evaluate Thrombosis Formation
  - Computationally efficient
  - Easy to Manipulate
- Apply to Test Coagulation Respond to Injury and Device Insertion
- This App will use the “Reacting Flow” library

COMSOL  
MULTIPHYSICS®



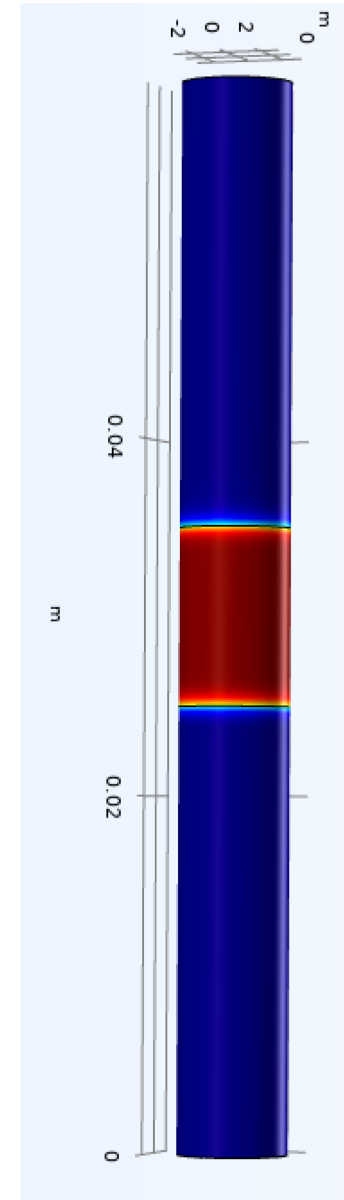
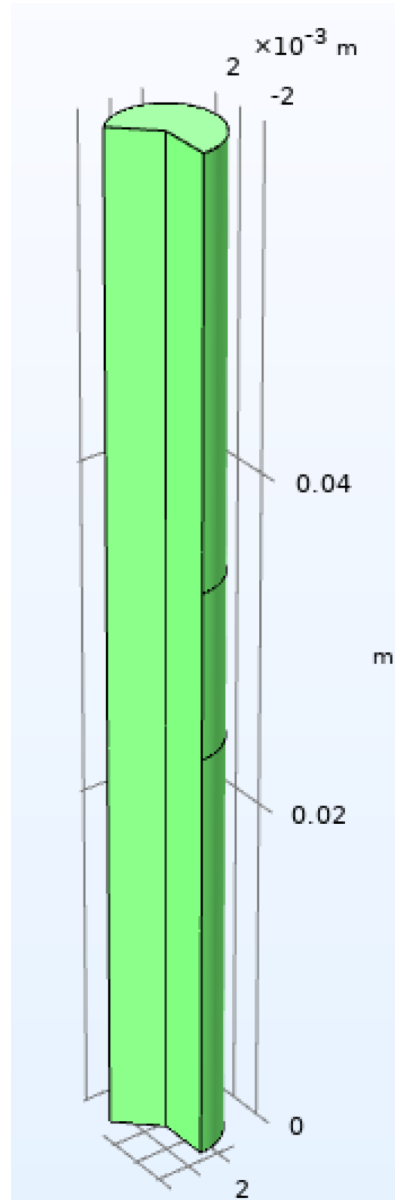
# Geometry

## Artery

- 0.06 m length
- 0.0031 m radius

## Wound Site

- 2D Axis Symmetry
- 0.025 - 0.035 m



# Chemokinetic implantation

- Using Reaction Engineering Module to generate space-dependent model with Chemistry and Transport of Dilute Species Modules

- Chemistry 1 (*chem*)
  - ▶ 1:  $TF + ten \Rightarrow XaVa$
  - ▶ Species: TF
  - ▶ Species: ten
  - ▶ Species: XaVa
  - ▶ 2:  $TF + ten + II \Rightarrow TF + ten + IIa$
  - ▶ Species: II
  - ▶ Species: IIa
  - ▶ 3:  $XaVa + II \Rightarrow XaVall$
  - ▶ Species: XaVall
  - ▶ 4:  $XaVall \Rightarrow XaVa + mlla$
  - ▶ Species: mlla
  - ▶ 5:  $XaVa + mlla \Rightarrow XaVa + IIa$
  - ▶ 6:  $mlla \Rightarrow mllaATIII$
  - ▶ Species: mllaATIII
  - ▶ 7:  $IIa \Rightarrow IIaATIII$
  - ▶ Species: IIaATIII

Parameter	Value	Unit
TF Wall Flux	1e-6	mol / (m <sup>2</sup> s)
Initial X Concen.	1.6e-4	M
Initial V Concen.	2e-5	M
Initial II Concen.	1.4e-3	M
Diffusivities	1e-7	m <sup>2</sup> / s
Reaction Rates	See [3]	varies

[3] Hansen KB, Shadden SC. Automated reduction of blood coagulation models. International journal for numerical methods in biomedical engineering. 2019 Oct;35(10):e3220.

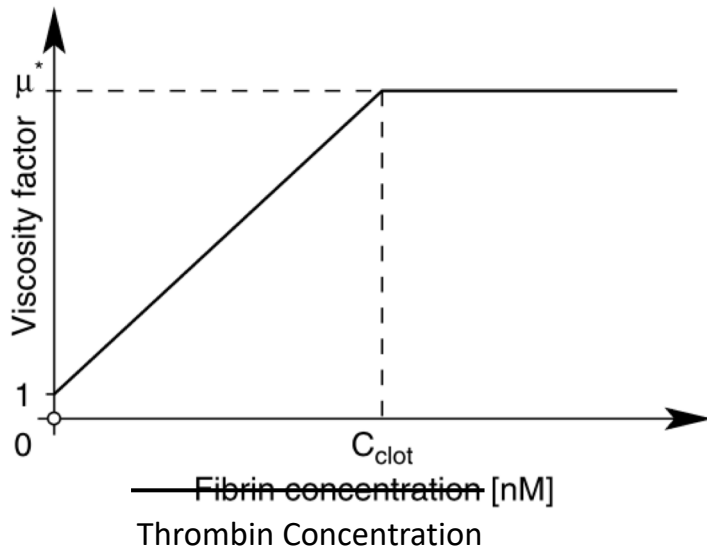
# Flow Implementation

- Laminar Flow Module with Fully developed inlet
- User defined viscosity

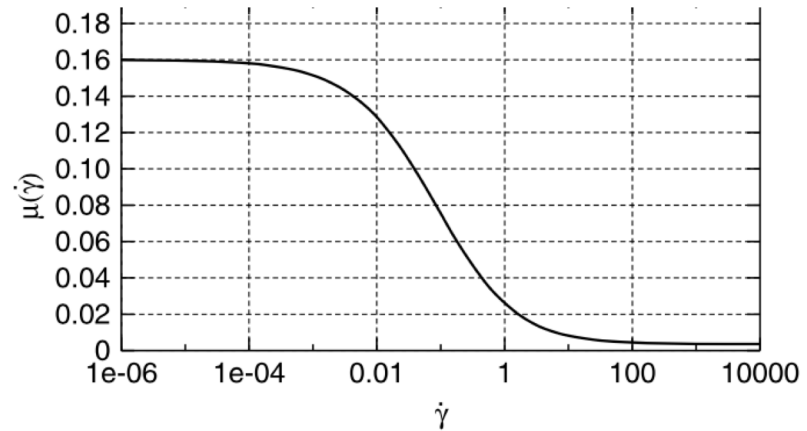
Concentration Dependent Pre-factor

X

Generalized Cross Model for Shear-thinning

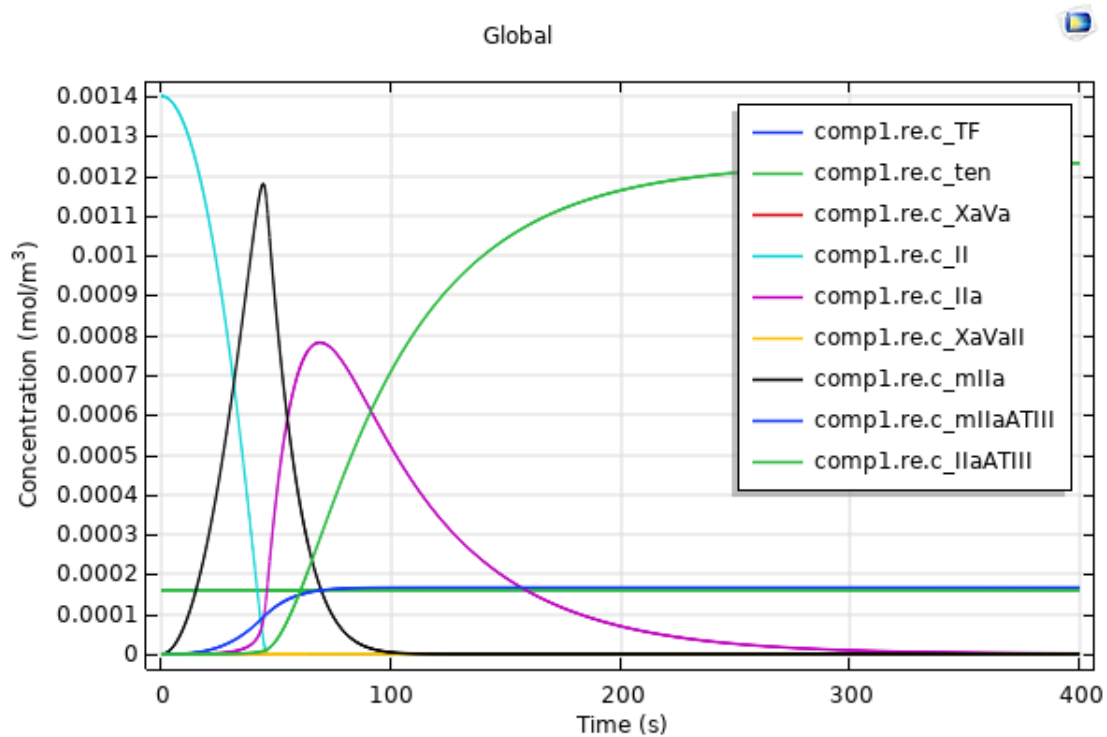


X

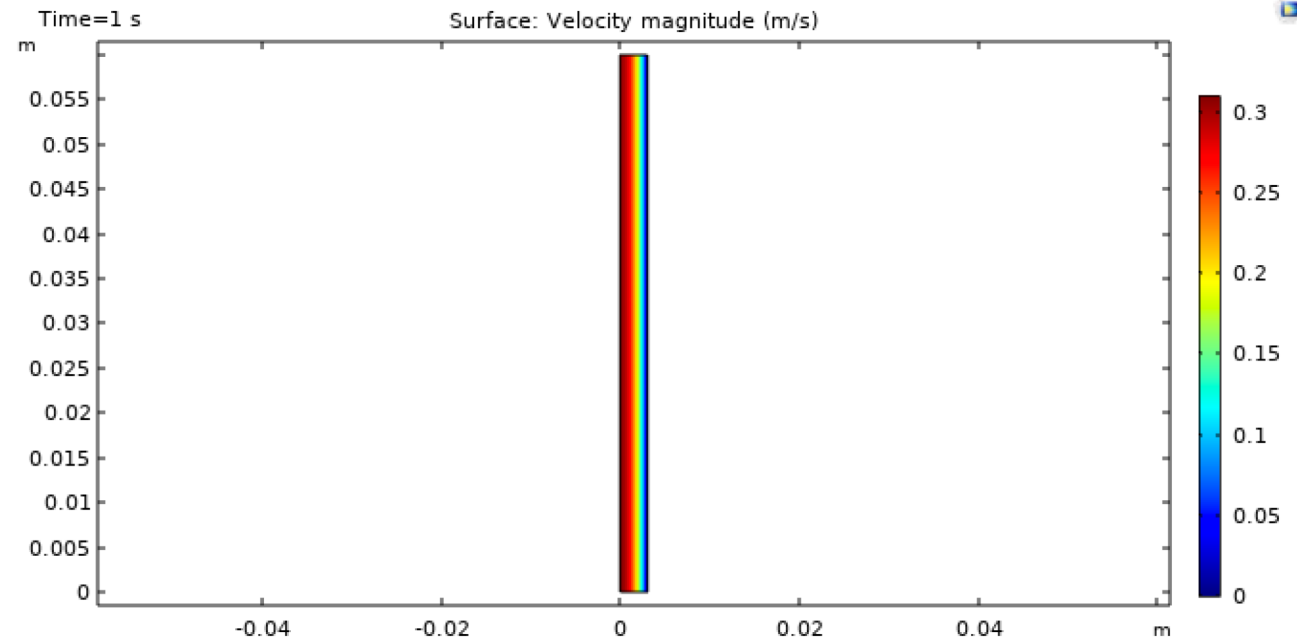


$$\frac{\mu(\dot{\gamma}) - \mu_{\infty}}{\mu_0 - \mu_{\infty}} = \frac{1}{(1 + (\lambda\dot{\gamma})^b)^a}$$

# Independent Tests



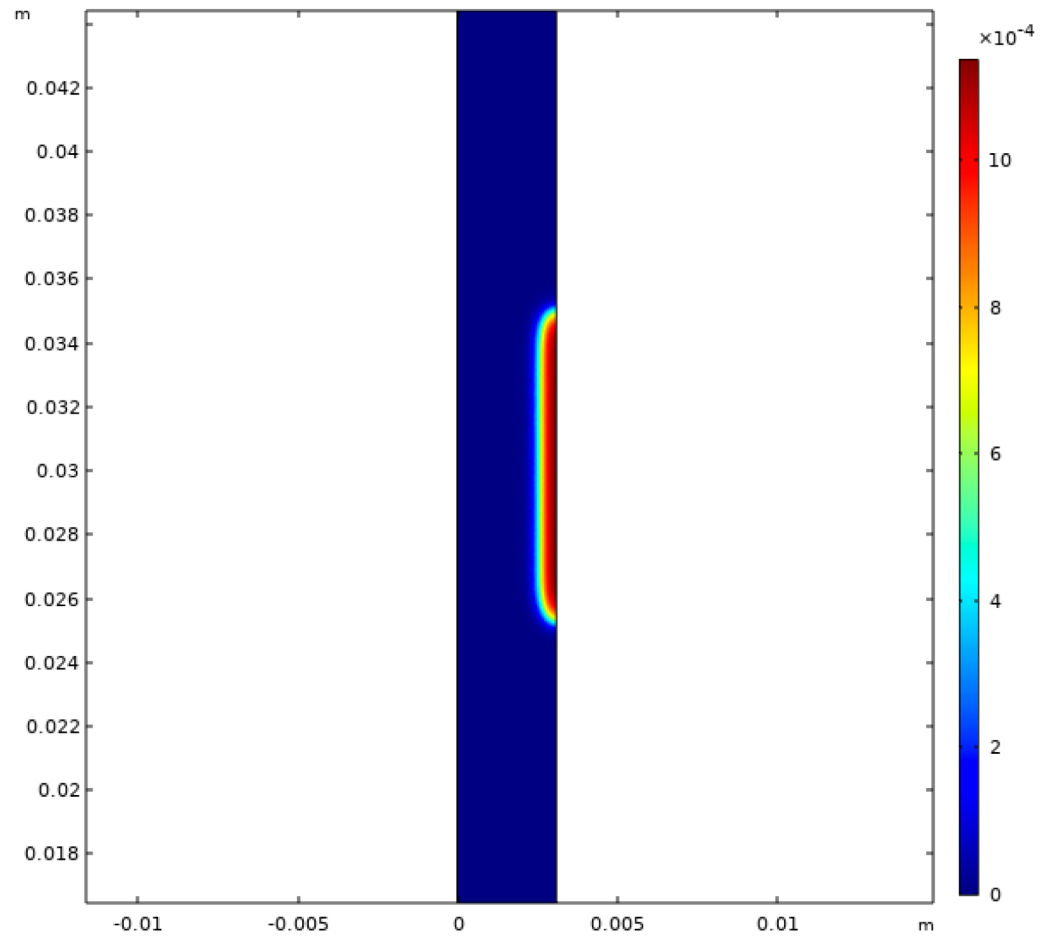
OD Batch Reactor



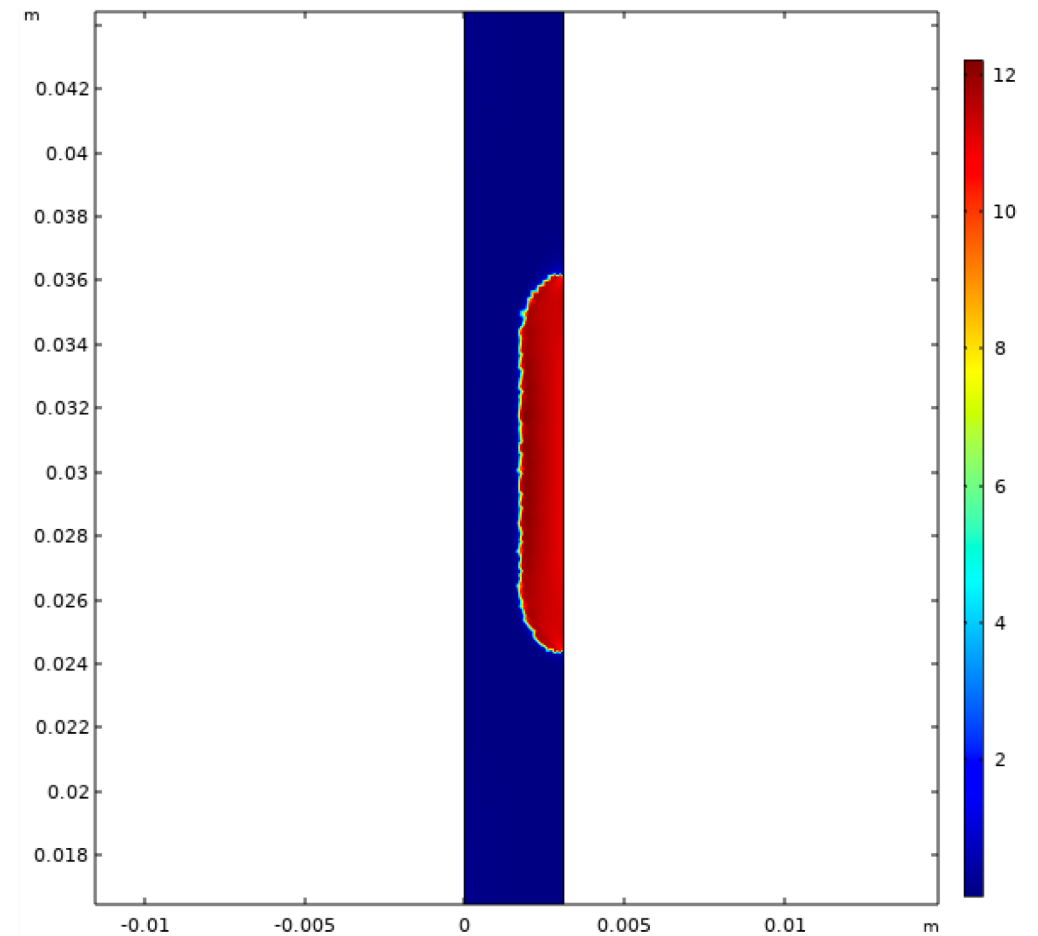
Test of Pipe Flow to Verify Centerline Velocity



# Fully Coupled Reacting Flow

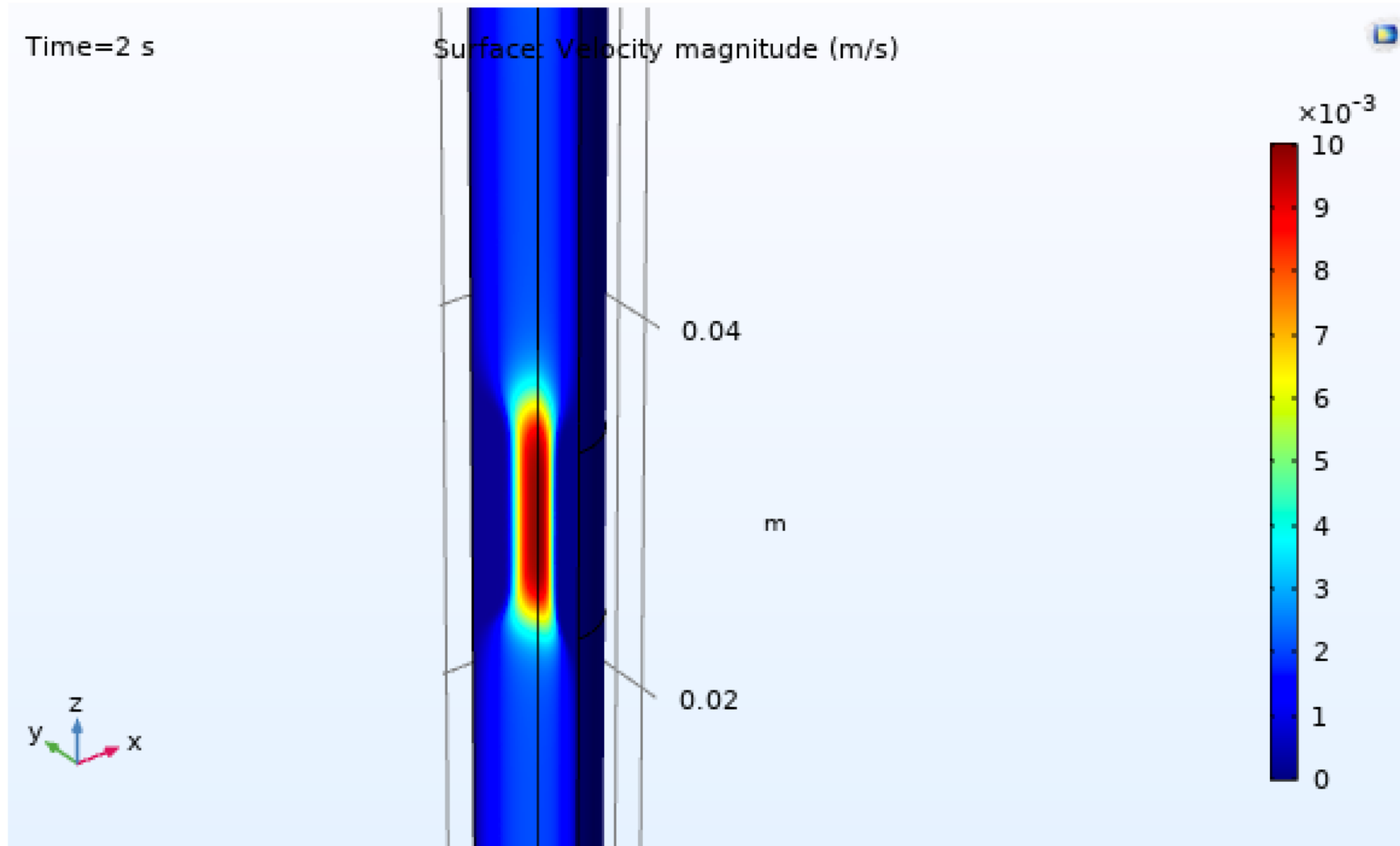


Thrombin Concentration ( $\text{mol/m}^3$ ),  $t = 2 \text{ s}$

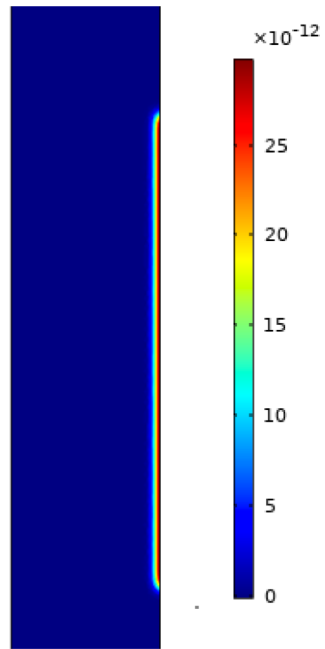


Dynamic Viscosity ( $\text{Pa}\cdot\text{s}$ ),  $t = 2 \text{ s}$

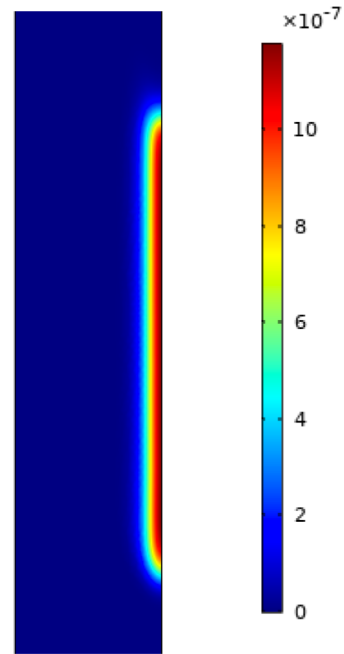
# Velocity Around the Thrombosis



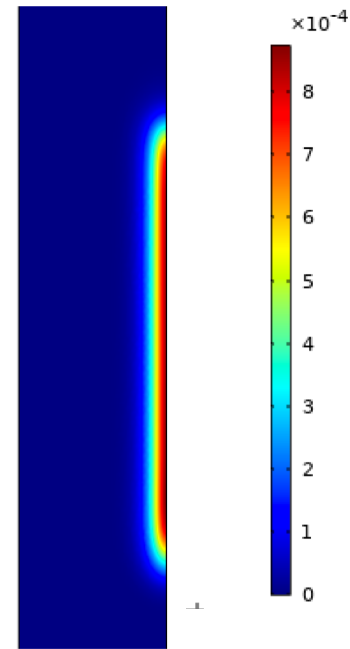
# Thrombin Concentration ( $\text{mol}/\text{m}^3$ )



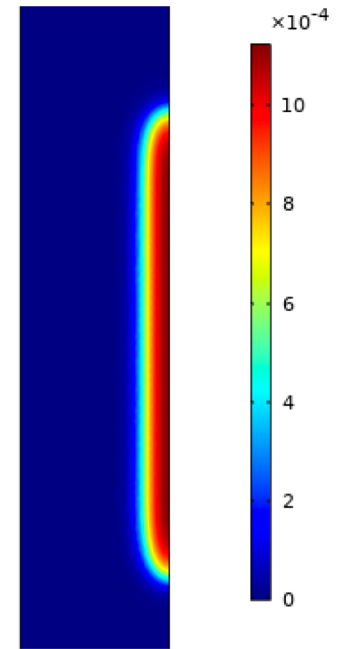
$t = 0.1$  s



$t = 0.8$  s

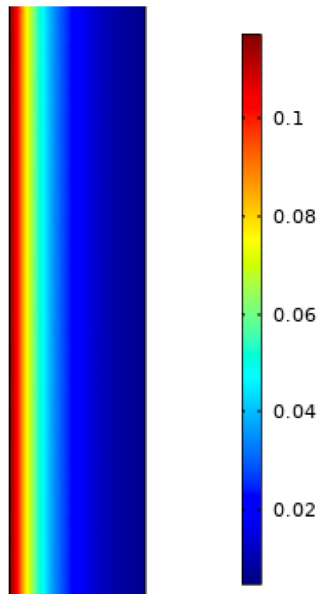


$t = 1.8$  s

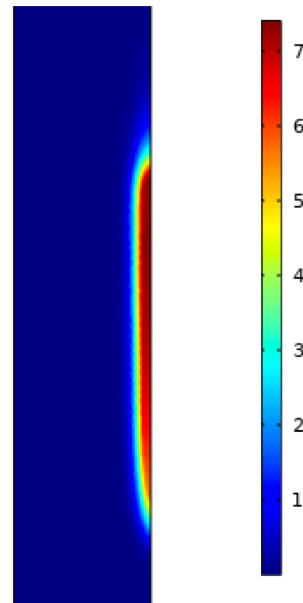


$t = 2.0$  s

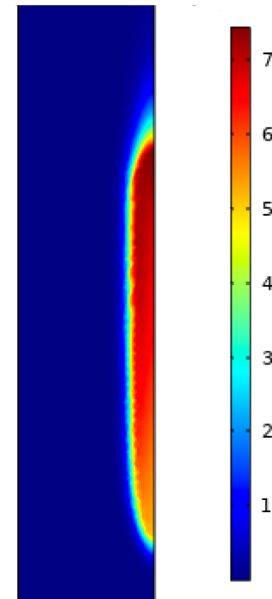
# Dynamic Viscosity (Pa\*s)



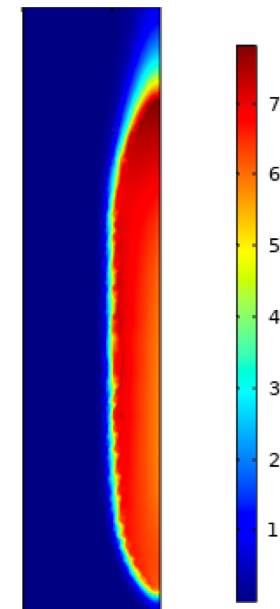
$t = 0.1$  s



$t = 1.2$  s



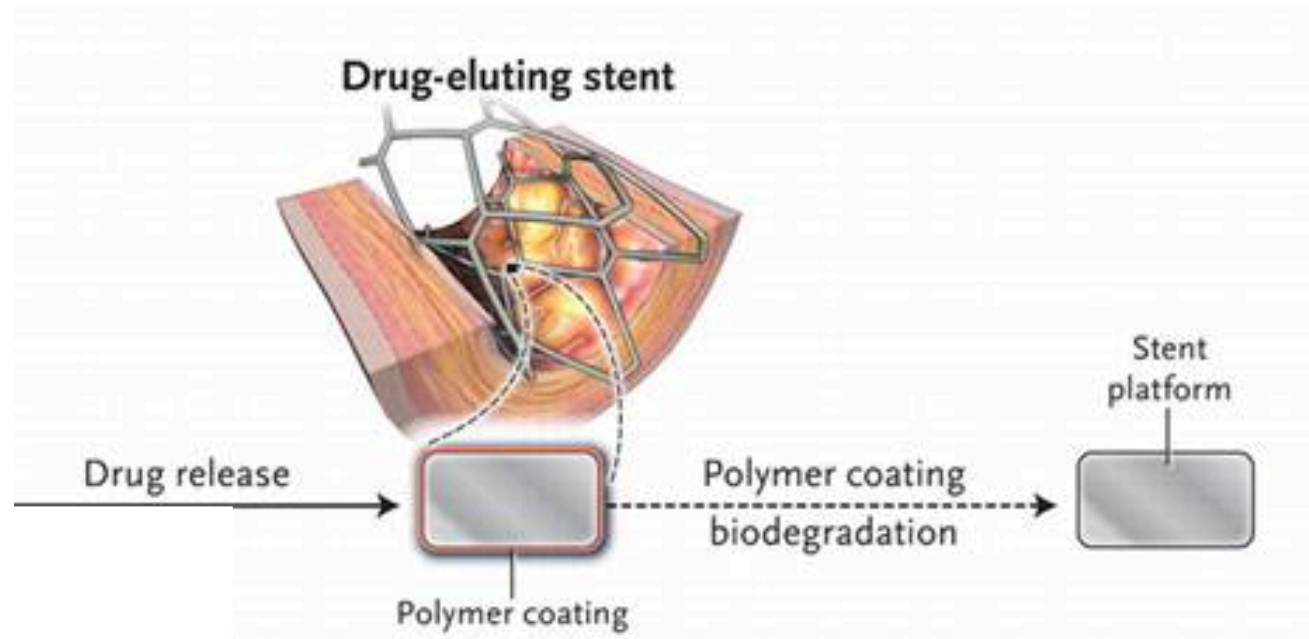
$t = 1.4$  s



$t = 2.0$  s

# Future Direction

- Investigate thrombosis on drug-eluting stent



<https://resident360.nejm.org/clinical-pearls/drug-eluting-coronary-stents>

# Acknowledgements and Questions

Larson Lab

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If you have any questions please reach out to [cerice@umich.edu](mailto:cerice@umich.edu)