



**COMSOL
CONFERENCE
2018 LAUSANNE**

**Numerical evaluation of the tuning,
pressure sensitivity and Lorentz force
detuning of RF superconducting crab
cavities**

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CERN



COMSOL CONFERENCE – LAUSSANE – 22/10/2018

Outline

- Introduction
- Numerical model
- Results
 - Overall results
 - Tunability
 - Pressure sensitivity
 - Lorentz force detuning
- Conclusions



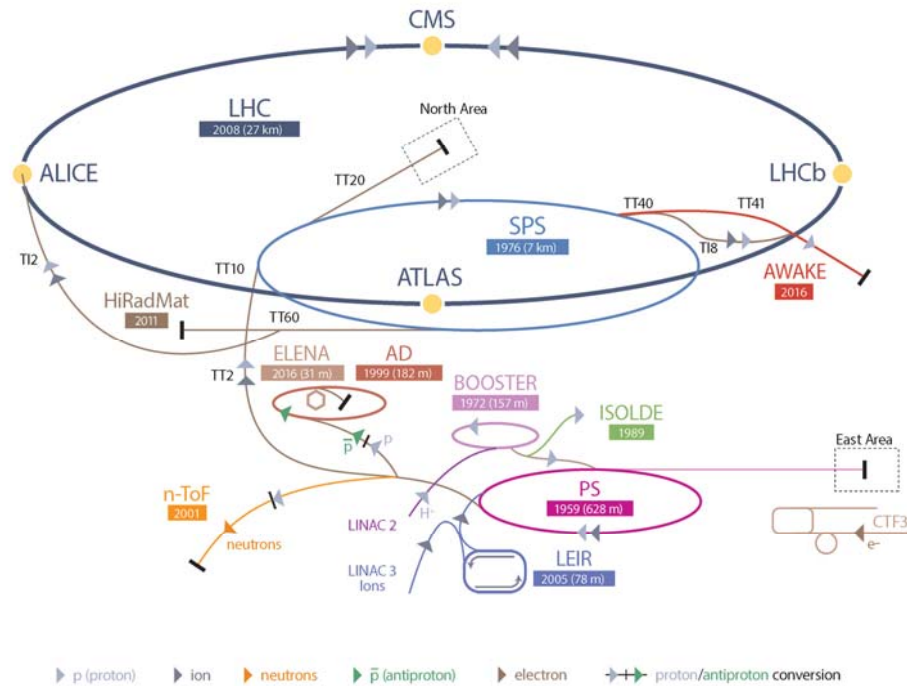
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Introduction - CERN

CERN's Accelerator Complex

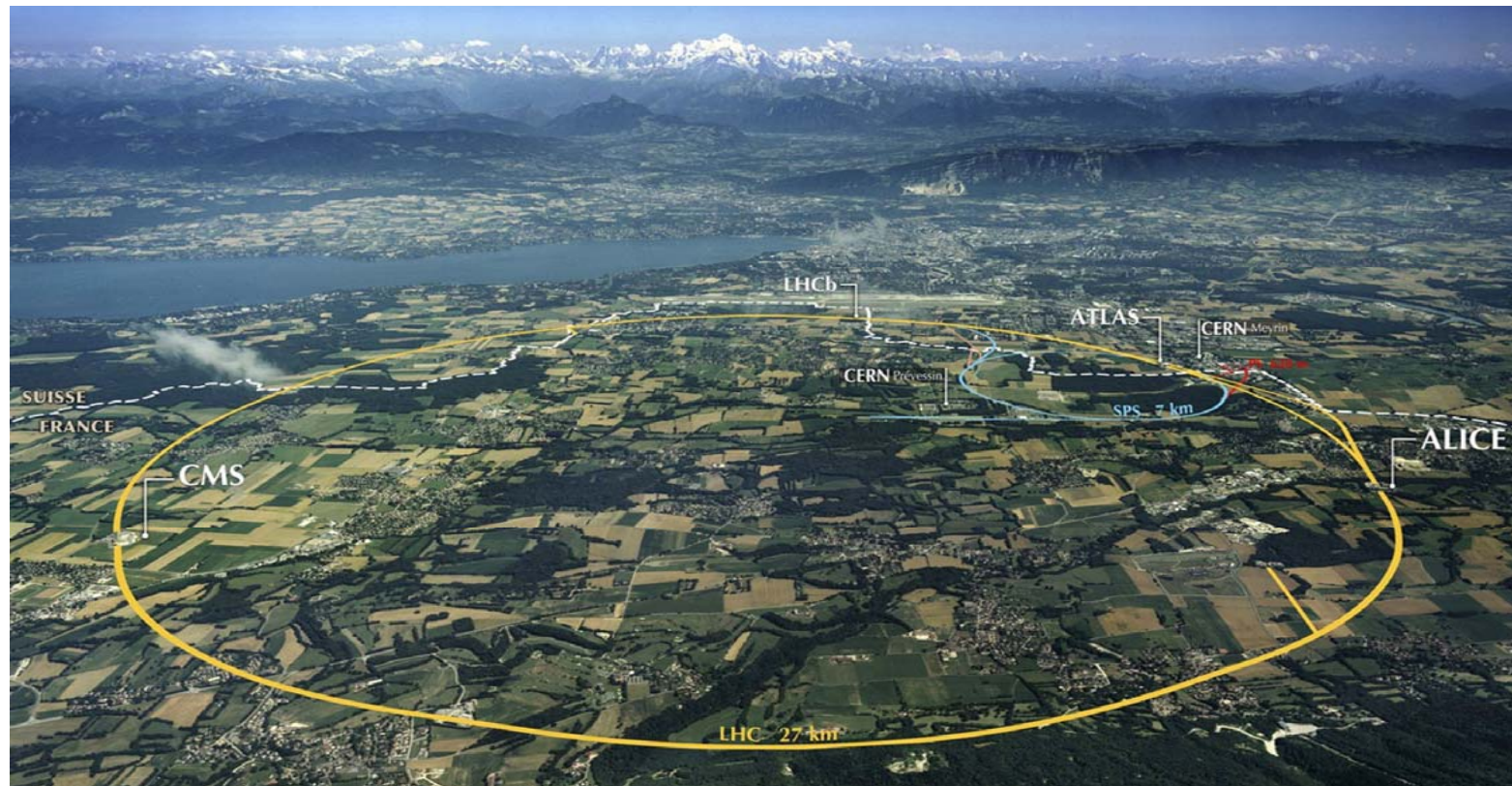


- CERN accelerator complex is the largest in the world
- LHC is the last stage and CERN's flagship
- **27 km** underground tunnel
- **2** counter-rotating **proton beams**
- **Collisions (experiment location)** which generate other particles

- **Radio Frequency System** (Acceleration)
- **Superconducting magnets** (bend trajectory)
- **2 Collimation Regions** (Beam Cleaning and Machine Protection)



Introduction - CERN

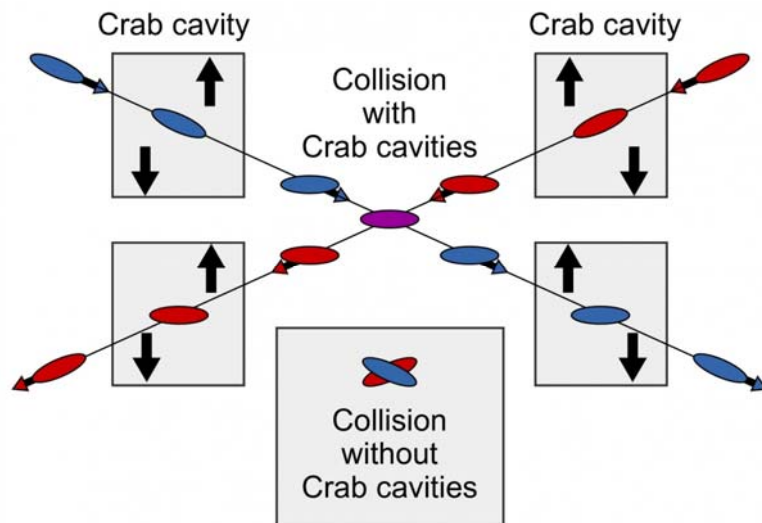


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Introduction - HL-LHC

- Peak luminosities a factor of five larger than LHC
- Update on **superconducting magnets**, **high-power superconducting links** with zero energy dissipation. New demands on **vacuum**, **cryogenics** and **machine protection**, and will require new concepts for **collimation** and **diagnostics**.
- **Crab cavities.** Transverse deflection of particle bunches.



Double Quarter Wave



RF Dipole



Introduction - Crab cavities

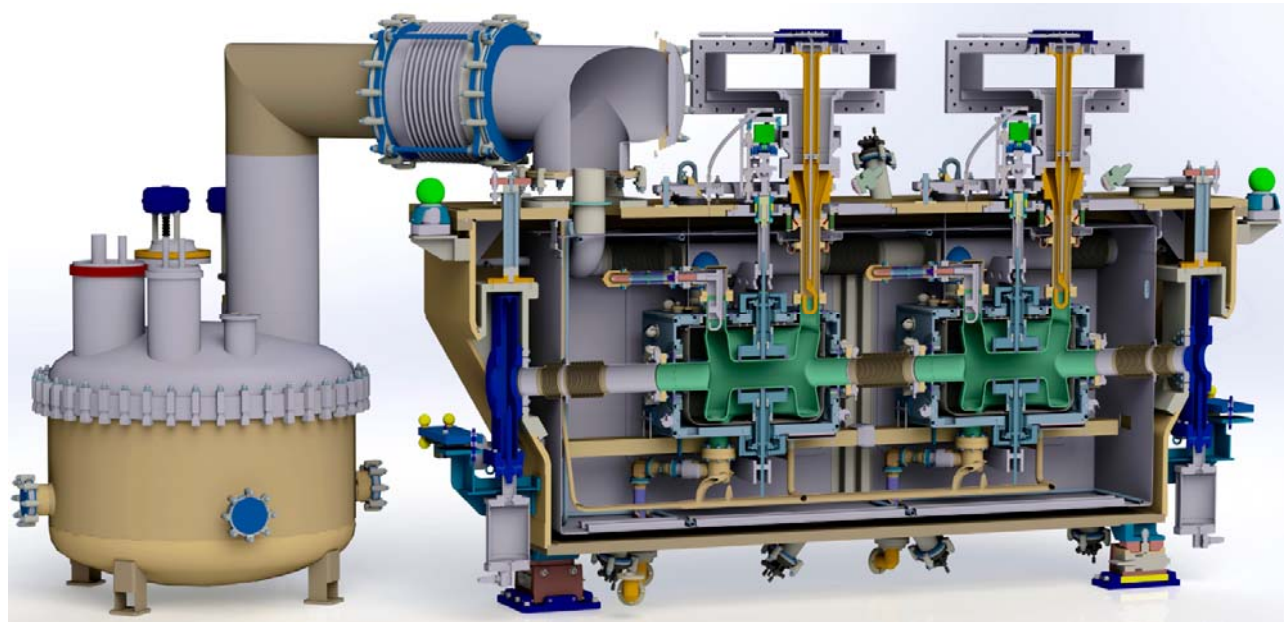
Double Quarter Wave (DQW)



RF Dipole (RFD)



- Operated at 2 K



Introduction - Crab cavities

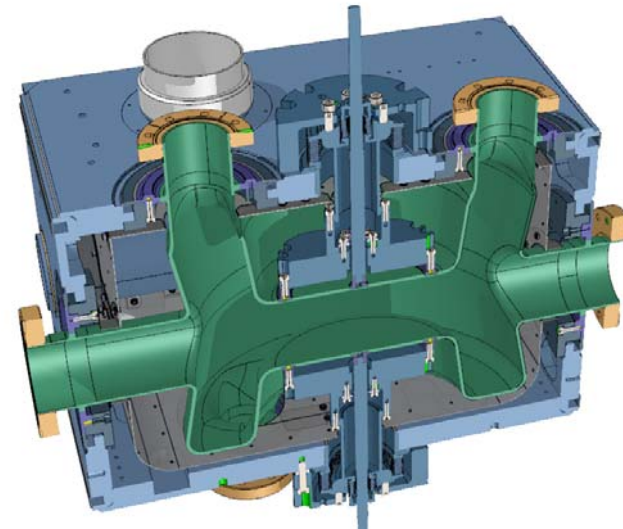
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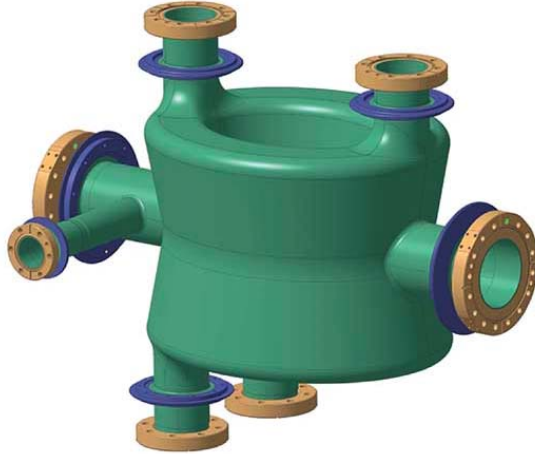


- Operated at **2 K**
- **3.4 MV** deflecting kick
- **400.79 MHz** fundamental frequency. **Tuning system**

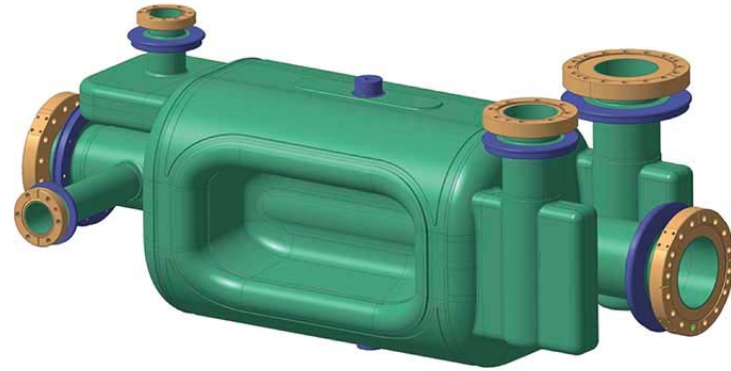


Introduction - Crab cavities

Double Quarter Wave (DQW)



RF Dipole (RFD)



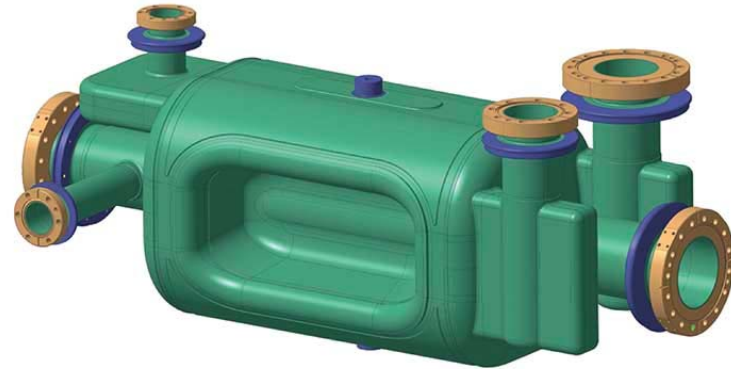
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- **400.79 MHz** fundamental frequency. **Tuning system.**
- **Pressure sensitivity** requirements. Changes of the cavity fundamental frequency due to pressure fluctuations of the cold He bath.
- **Lorentz force detuning** requirements. Change of the cavity fundamental frequency due to radiation forces.

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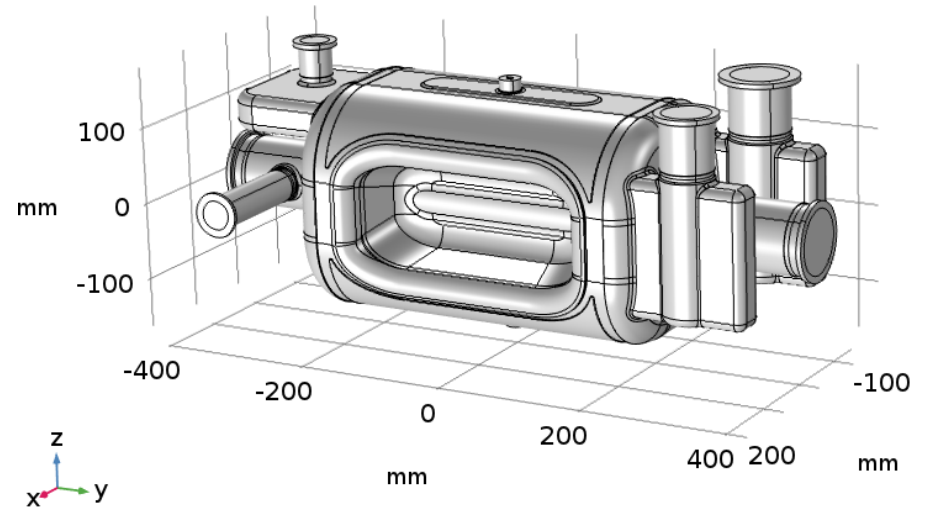
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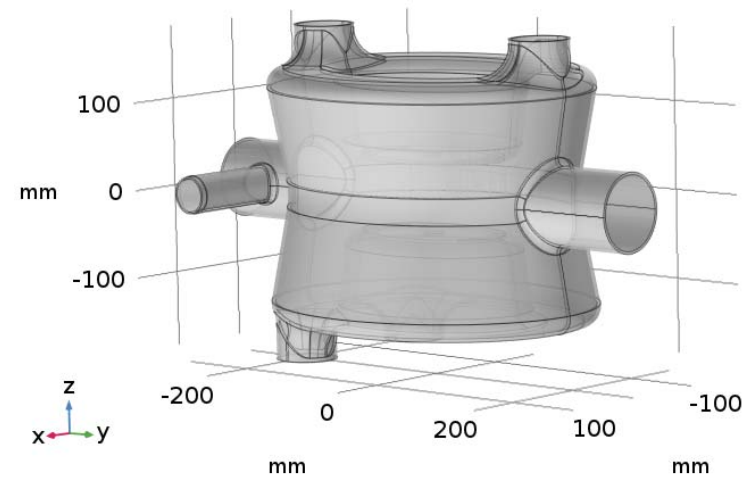
Numerical model

- Component 1 (*comp1*)
 - Definitions
 - Geometry 1
 - Materials
 - Electromagnetic Waves, Frequency Domain (*emw*)
 - Solid Mechanics (*solid*)
 - Moving Mesh (*ale*)
 - Electromagnetic Waves, Frequency Domain 1 (*emw1*)
 - Mesh 1
- Study 1
 - Cluster Computing
 - Step 1: Eigenfrequency 1
 - Step 2: Stationary
 - Step 3: Eigenfrequency 2
 - Solver Configurations
 - Job Configurations

RF Dipole



Double Quarter Wave

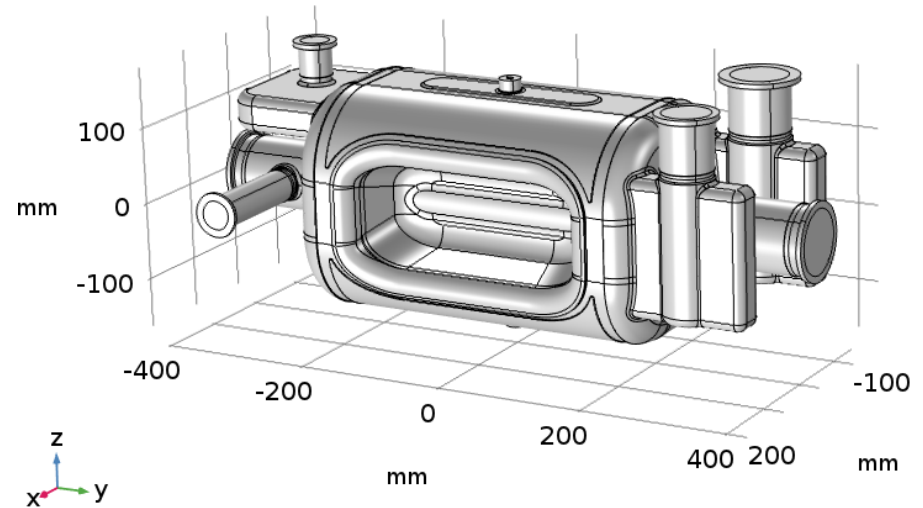


Numerical model

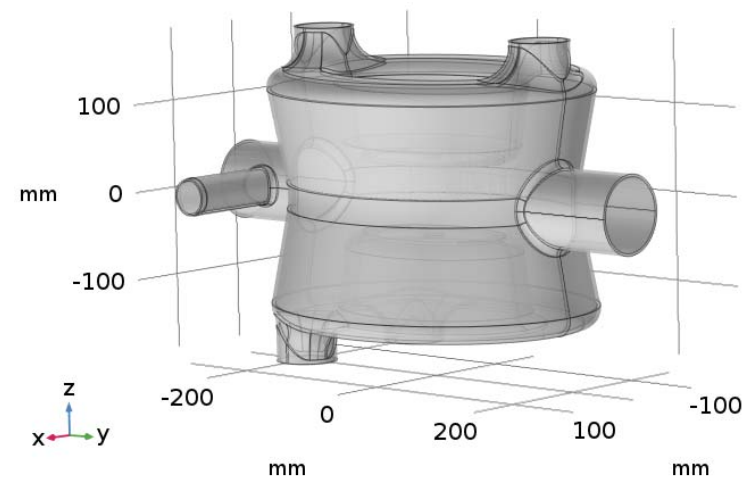
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- Two models:
- DQW for tunability, validation and mesh sensitivity
- RFD for pressure sensitivity (PS), Lorentz force detuning (LFD) and design optimization

RF Dipole



Double Quarter Wave

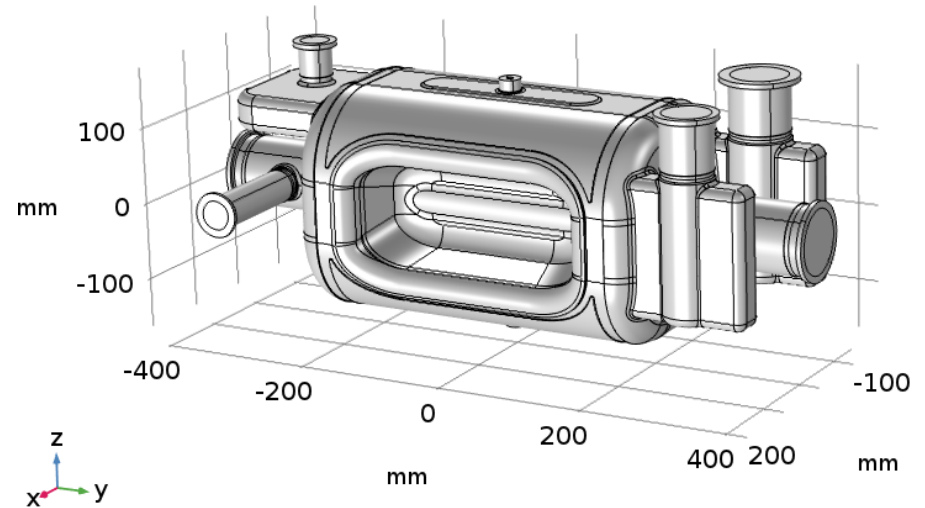


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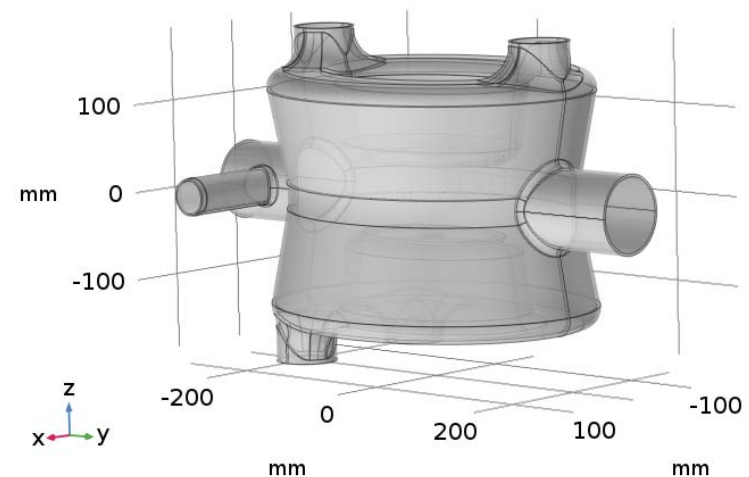
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- Niobium RRR300 for the cavities
- 55Ti45Nb for the tuning interfaces
- Vacuum volume inside the cavity

RF Dipole



Double Quarter Wave

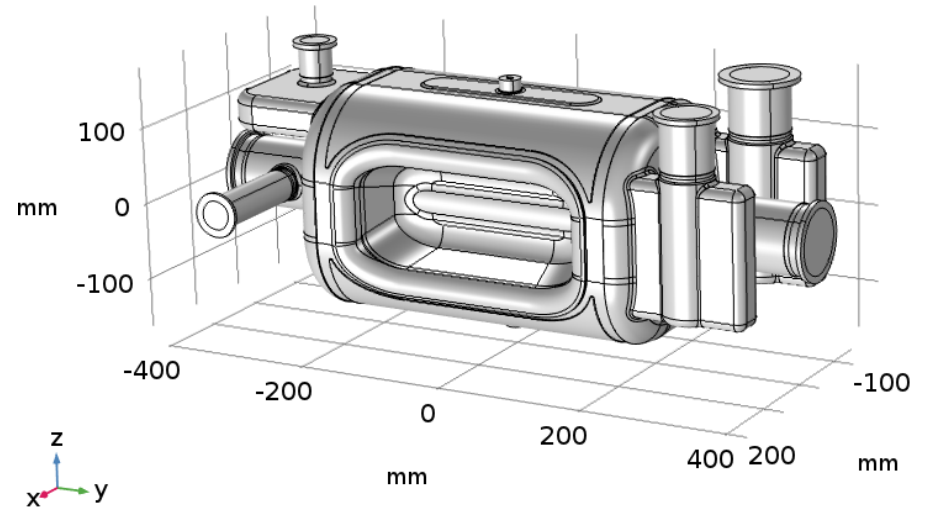


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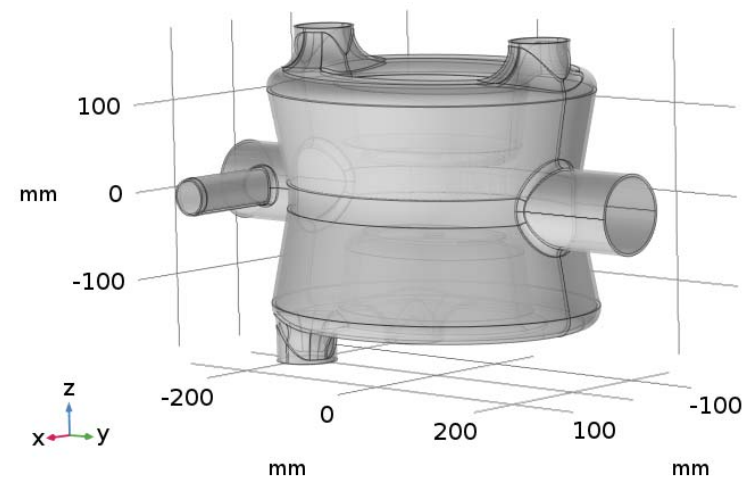
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- Fundamental frequency of the cavity without any imposed load

RF Dipole



Double Quarter Wave

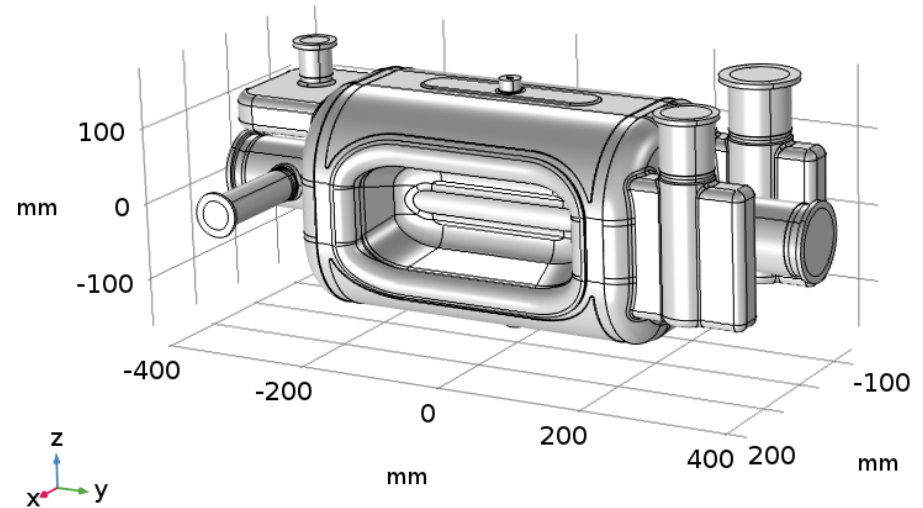


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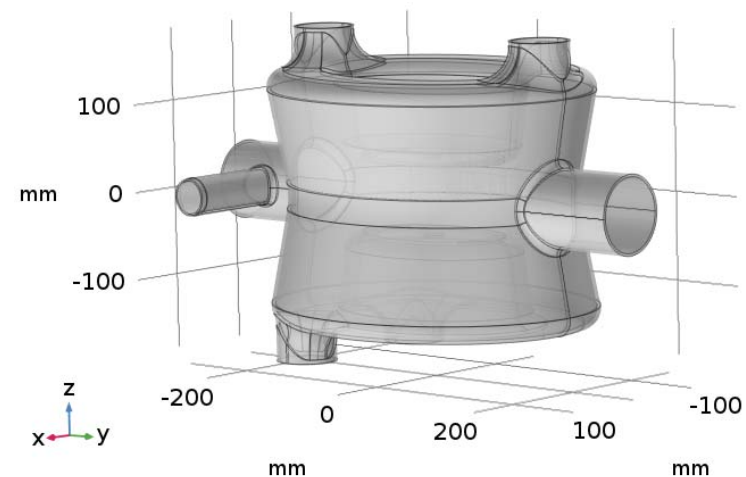
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- Structural & moving mesh coupled simulation to capture the cavity and vacuum volume deformation.

RF Dipole



Double Quarter Wave

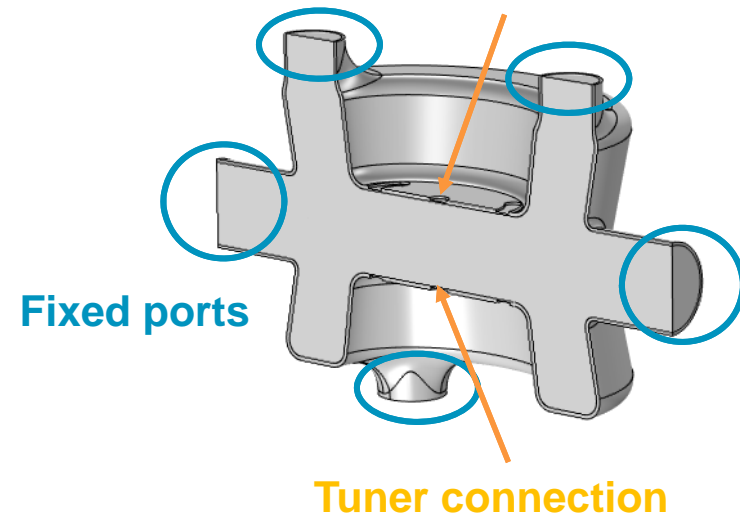


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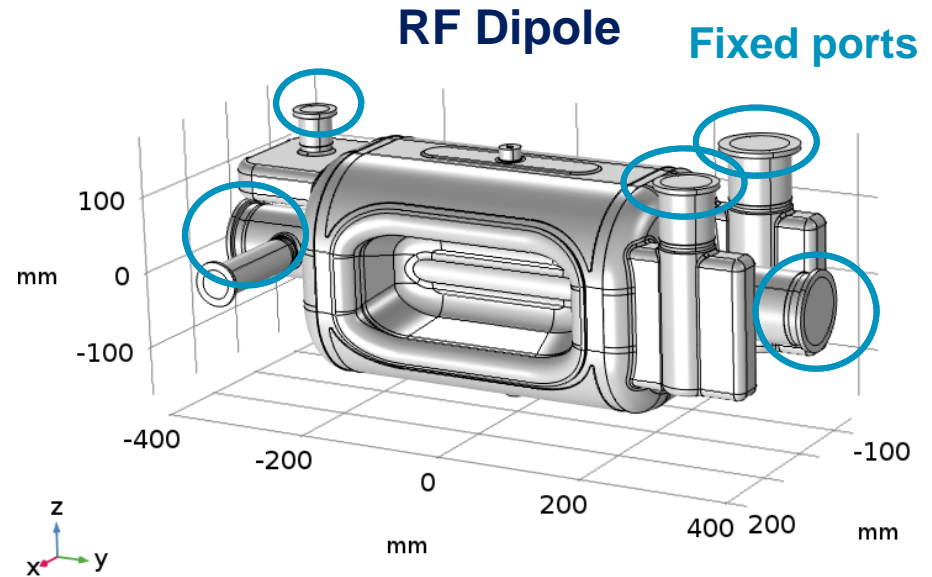
- Boundary conditions:
 - Symmetry
 - Fixed ports
 - DQW: **imposed displacement** in the tuners

Double Quarter Wave



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Pressure sensitivity

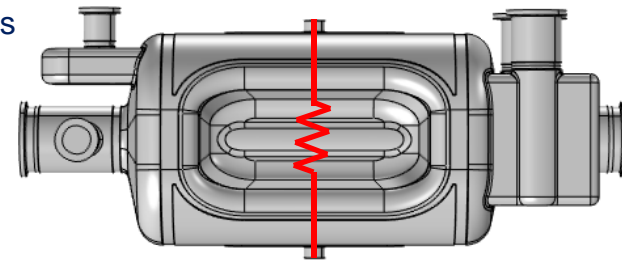
External pressure of 1 bar
(negative internal pressure)

- Boundary conditions:
 - Fixed ports
 - Internal pressure
 - Tuning interfaces

Spring between the tuning interfaces

$$F_{s1} = k_s(v_{s2} - v_{s1})$$

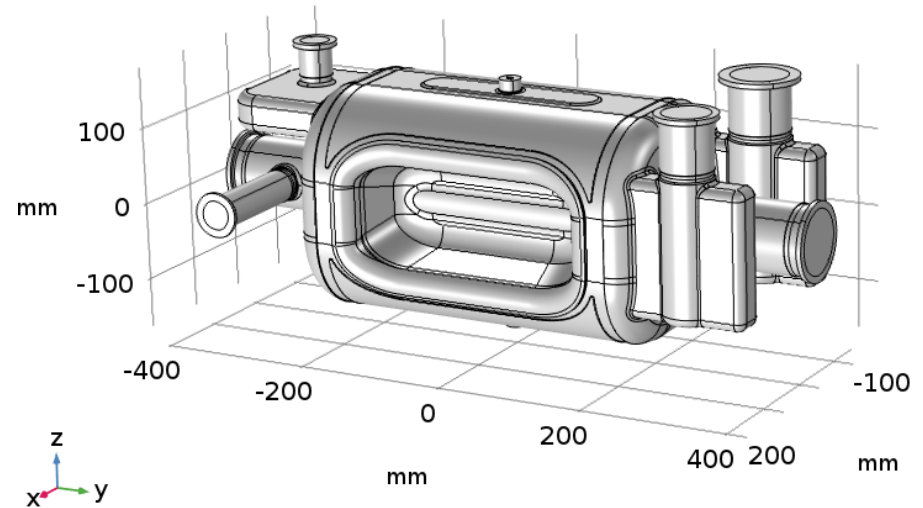
$$F_{s2} = k_s(v_{s1} - v_{s2})$$



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RF Dipole



- Boundary conditions:
 - Fixed ports
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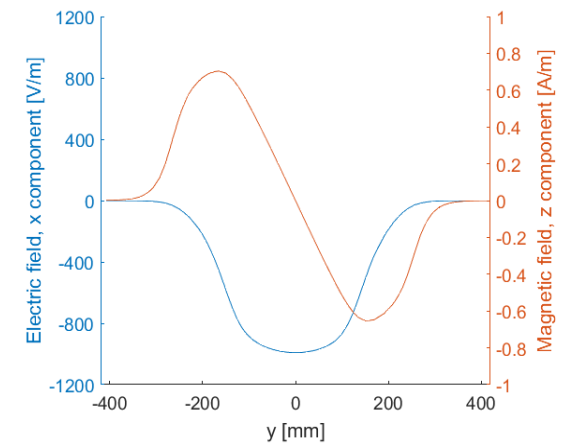
Lorentz force detuning

Radiation pressure

$$P = \frac{1}{4}(\mu_0 H^2 - \epsilon_0 E^2) \cdot SF$$

Integration of beam kick along the axis

$$SF = \left(\frac{V_{T,nominal}}{V_{T,COMSOL}} \right)^2$$

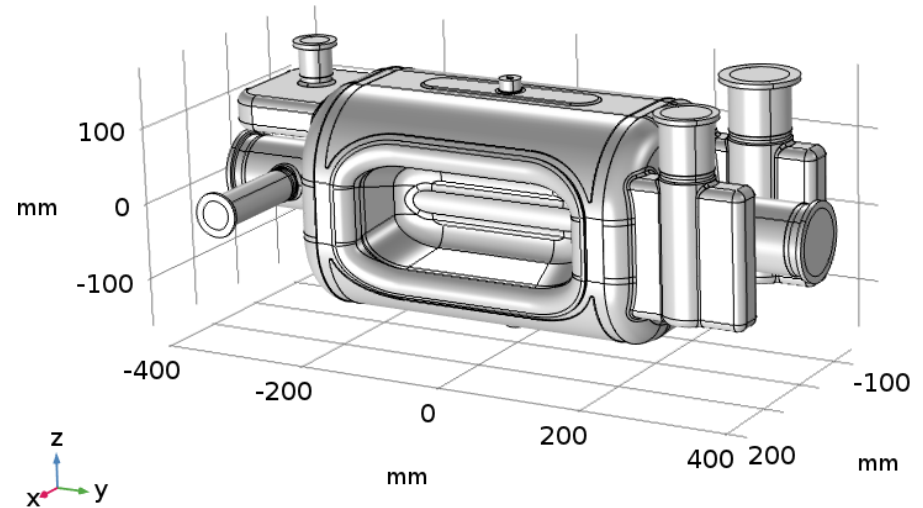


$$V_{T,COMSOL} = \left| \int E_x \cos\left(\frac{\omega y}{c}\right) dy + \int \mu_0 c \cdot H_z \cdot \sin\left(\frac{\omega y}{c}\right) dy \right|$$

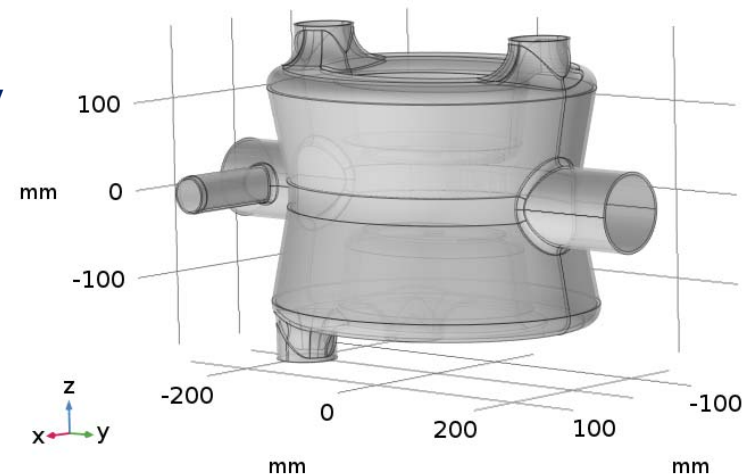
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RF Dipole



Double Quarter Wave



- Fundamental frequency of the deformed cavity

Tunability [kHz/mm]	PS [Hz/mbar]	LFD [Hz/MV ²]
$\frac{f_1 - f_0}{ v_{s2} + v_{s1} }$	$\frac{f_1 - f_0}{P_{PS}}$	$\frac{f_1 - f_0}{V_{T,nominal}^2}$

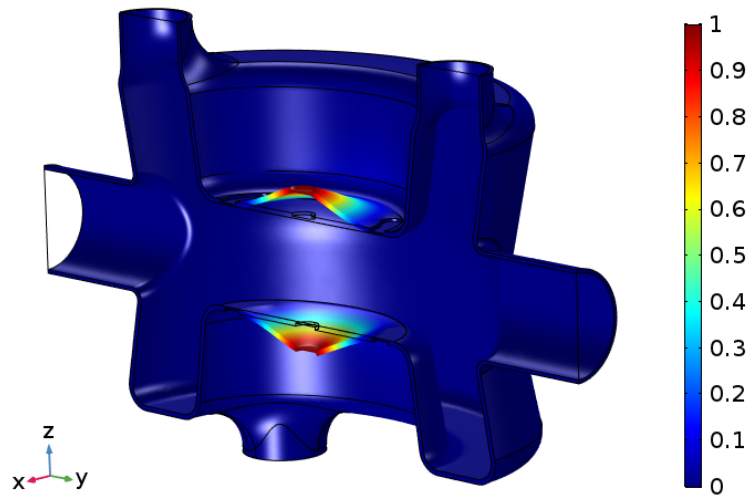
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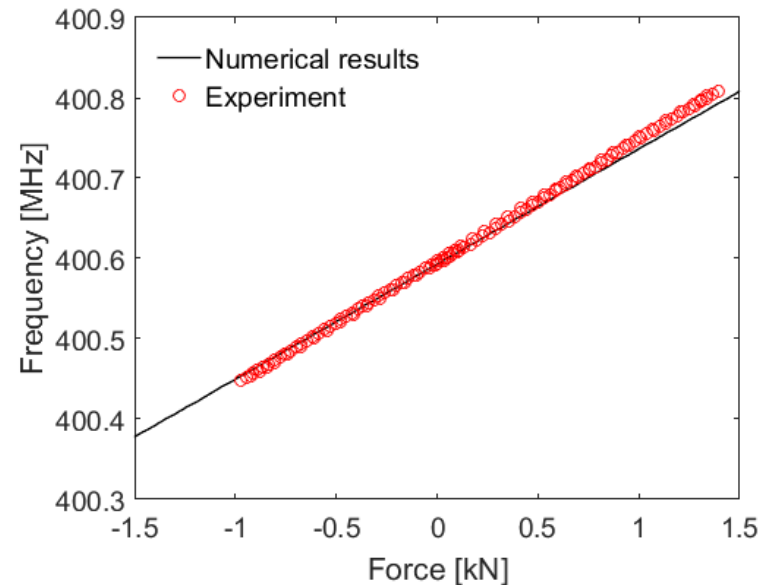
Results – DQW cavity

- Comparison with **experimental results** of the cavity cooldown at CERN at the end of 2017.
- **Very good agreement** between numerical and experimental results.
- Cavity tunability = $\frac{f_1 - f_0}{|v_{s2}| + |v_{s1}|} = 315.5 \text{ kHz/mm}$, well in line with expected values.
- **Incertitude** associated to COMSOL and the transformation from displacement to force in the tuning system.

Cavity displacement (mm)

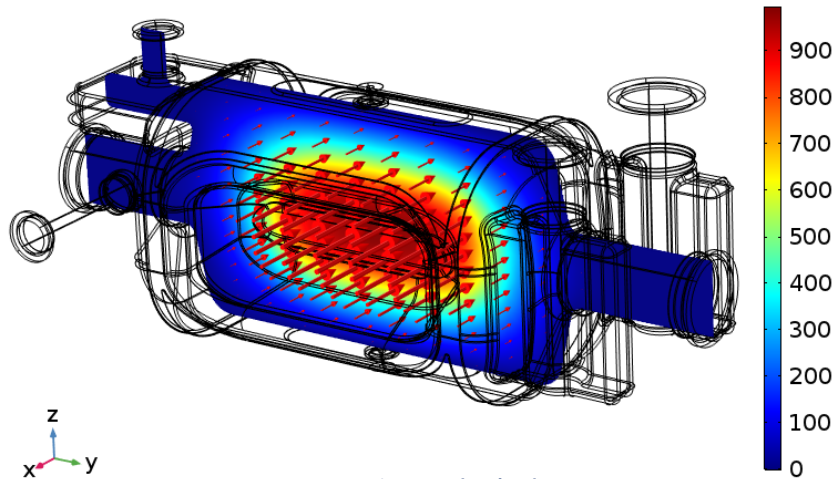


Cavity fundamental frequency vs. force on the tuning system

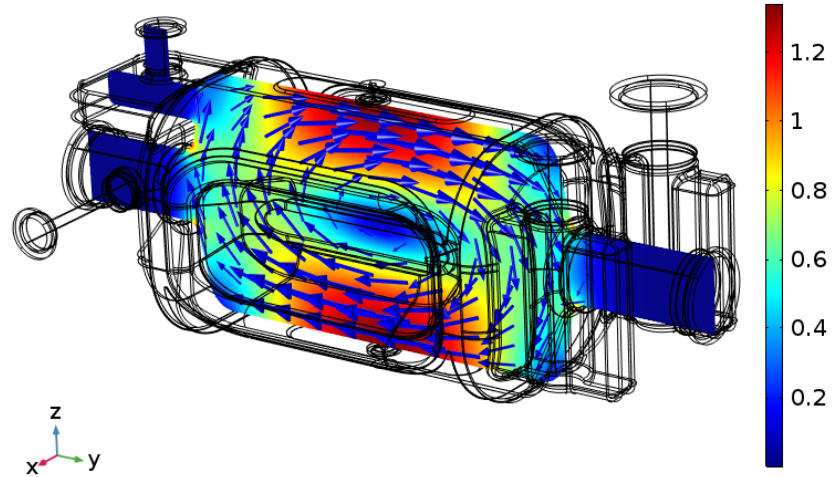


Results – RFD cavity

Electric field (V/m)



Magnetic field (A/m)



Overall results

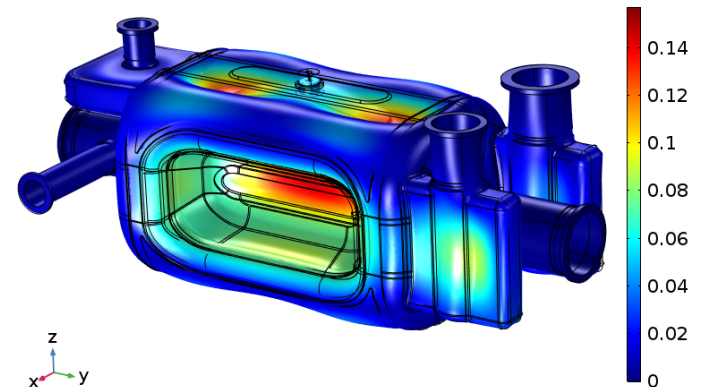
Energy stored in the cavity for 3.4 MV deflecting kick = **10.7 J**

Scaling Factor for radiation pressure, $SF=7.086 \cdot 10^8$

Pressure sensitivity

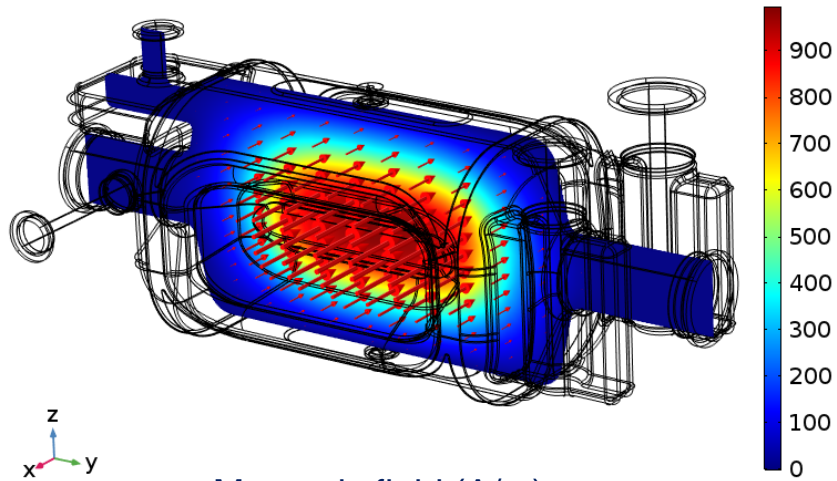
$$\frac{f_1 - f_0}{P_{PS}} = 244 \text{ Hz/mbar}$$

Cavity deformation (mm)

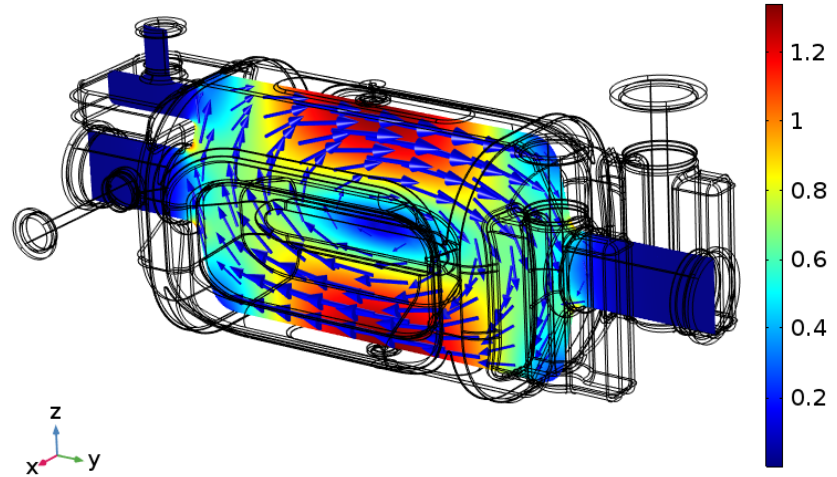


Results – RFD cavity

Electric field (V/m)

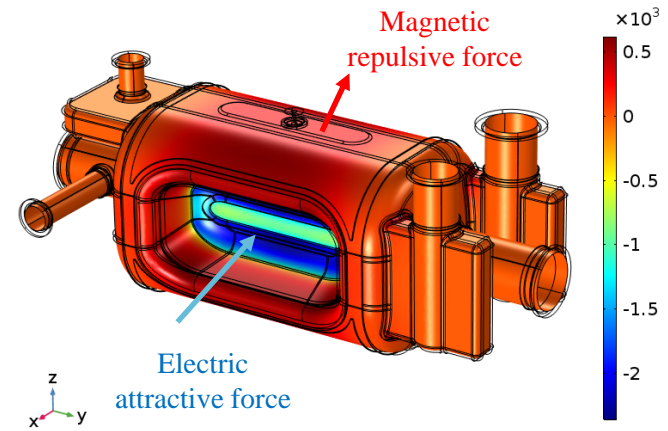


Magnetic field (A/m)



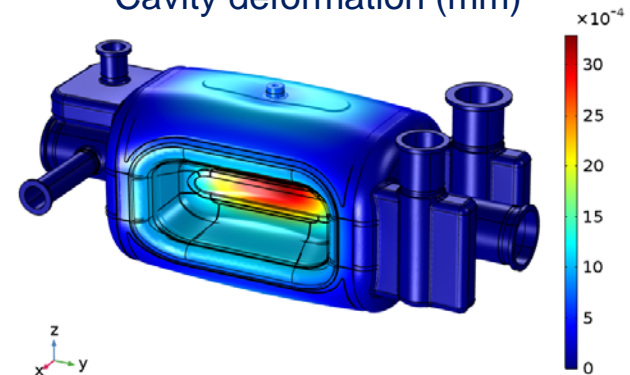
Lorentz force detuning

Radiation pressure (Pa)



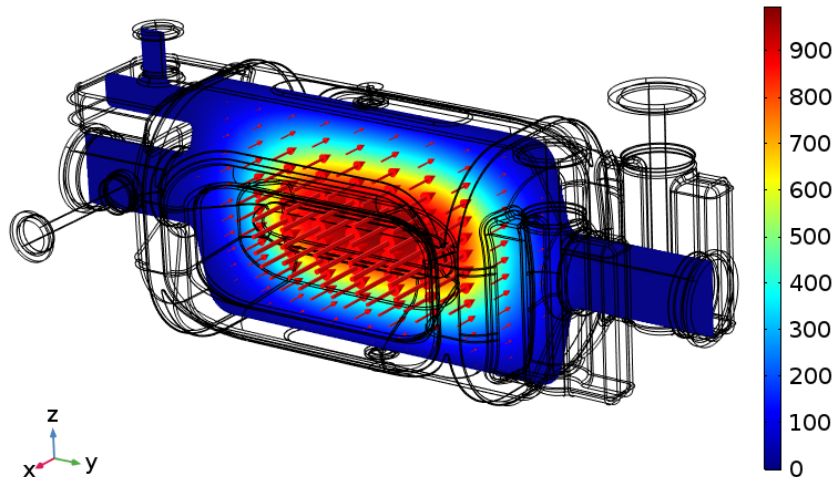
$$\frac{f_1 - f_0}{V_{T,nominal}^2} = 659 \text{ Hz/MV}^2$$

Cavity deformation (mm)

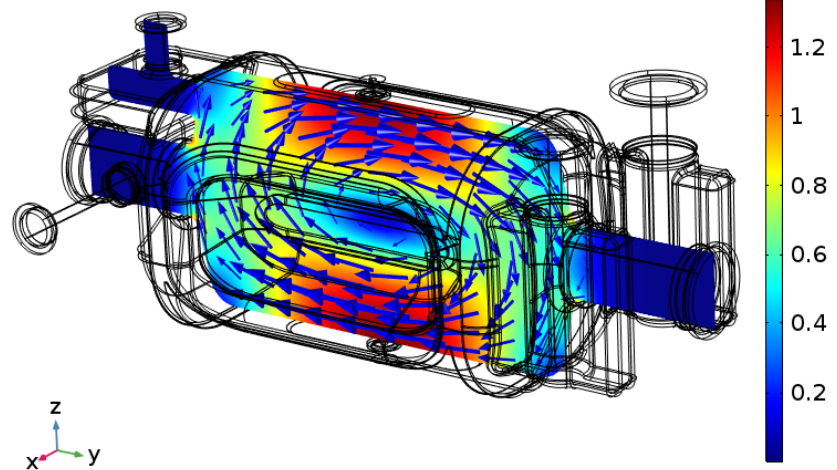


Results – RFD cavity

Electric field (V/m)

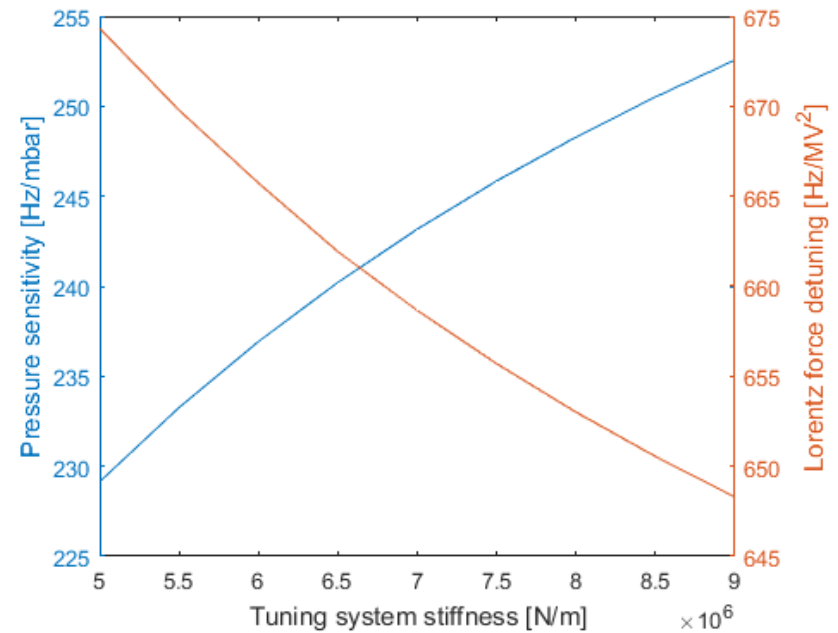


Magnetic field (A/m)



Tuning stiffness

- Tuning stiffness, k_s , parametric analysis.
- **Counteracting effects** of deformation in the pole and tuning regions.



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Conclusions

- **Tunability, pressure sensitivity** and **Lorentz force detuning** of SRF Crab cavities were numerically evaluated using COMSOL.
- The numerical predictions of the DQW cavity tunability **matched very well** the experimental results.
- Pressure sensitivity and Lorentz force detuning values were used **during the design** stage of the **RFD cavity body**.
- Parametric study on the tuning stiffness is used for the **design of the tuning system**.
- COMSOL is a **very powerful tool** for the RF-Structural evaluation of crab cavities during the validation and design stages.



Thank you for your attention!

