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Engineering

A Magneto hydrodynamic study of an inductive MHD generator

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OUTLINE OF THE PRESENTATION

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- INDUCTIVE MHD GENERATOR
- PHYSICAL MODEL
- MODELLING IN COMSOL
- SOLVER SETTING
- RESULTS
- CONCLUSION



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GOAL

- Typical drawbacks of MHD generators:
 - The use of the superconductive coils to generate the external magnetic field;
 - The deterioration of the electrodes;
 - The needed of high temperatures of the working fluid.
- Advantages of the proposed devices:
 - No external magnetic field;
 - No electrode is involved by the load current;
 - low temperatures.

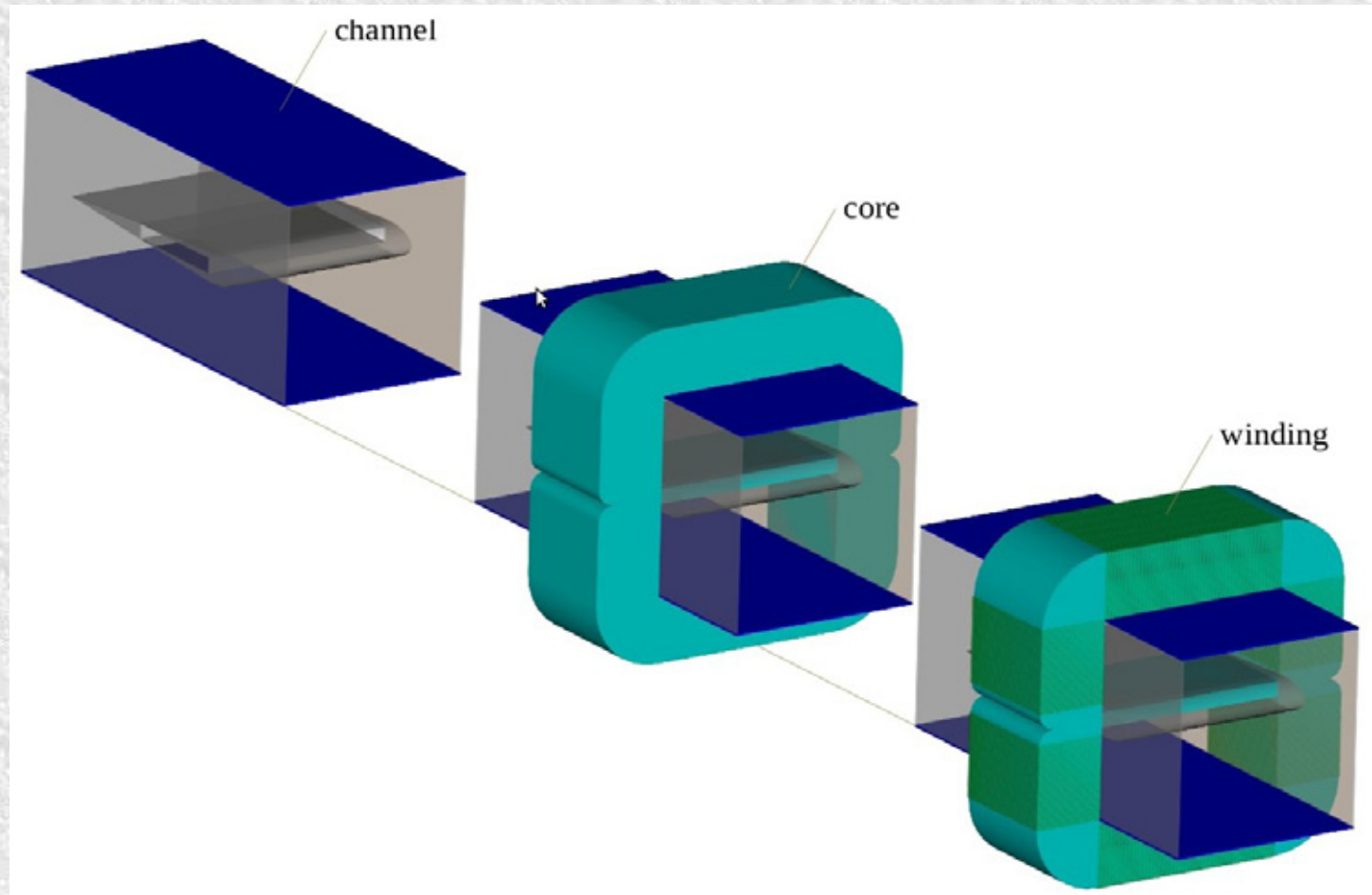


INDUCTIVE MHD MODEL

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Assembly of the Generator



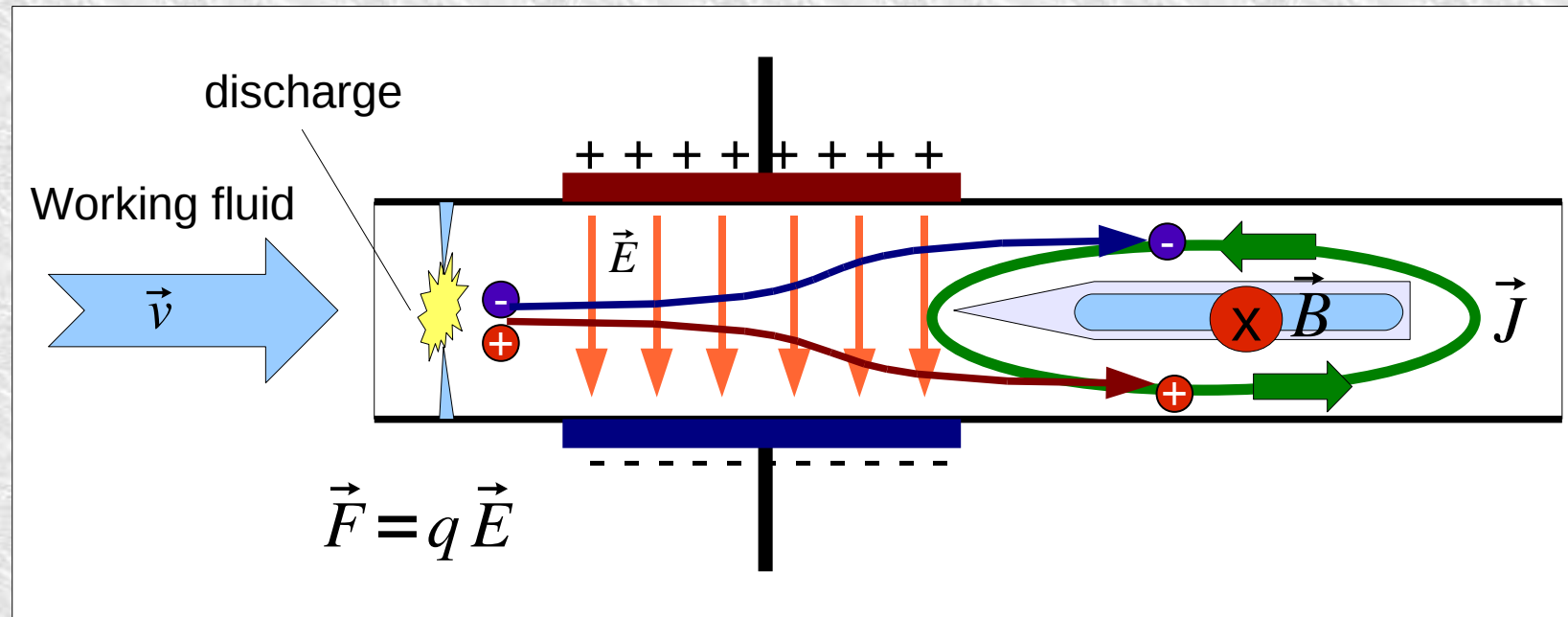


INDUCTIVE MHD MODEL

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Operating principle





THE APPLIED PHYSICAL MODEL

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- Electrostatic stationary;
- Fluid flow stationary (Navier-Stokes);
- Convection and diffusion transient.



AC/DC MODULE

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- Electrostatic model

$$\nabla^2 V = \frac{\rho}{\epsilon_0} \quad \text{Poisson equation}$$

where

$$E = -\nabla V$$

ρ space charge density

ϵ_0 dielectric permittivity



HEAT TRANSFER MODULE

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- Navier-Stokes k-ε model

Continuity equation

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$$

Momentum equation

x component

$$\rho u \frac{\partial u}{\partial x} + \rho v \frac{\partial u}{\partial y} = (\mu + \mu_t) \left[\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} \right] - \frac{\partial p}{\partial x} + F_x$$

y component

$$\rho u \frac{\partial v}{\partial x} + \rho v \frac{\partial v}{\partial y} = (\mu + \mu_t) \left[\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} \right] - \frac{\partial p}{\partial y} + F_y$$



MULTIPHYSICS MODULE

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- Convection and diffusion model

$$\frac{\partial c}{\partial t} = D \nabla^2 c - \vec{v} \cdot \nabla c$$

where

c concentration of charge

D diffusion coefficient

\vec{v} velocity vector



MODELING IN COMSOL

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- The convection and diffusion, electrostatic and Navier-Stokes equation are coupled;
- Velocity field from Navier's-Stokes equation and electric field from Poisson's equation used as source terms for convection's and diffusion's equation;
- The generation of the charge modeled setting the reaction rate parameter:

$$R = \frac{C_R}{\sqrt{2\pi \cdot \sigma^2}} \left[e^{-\frac{(t-t_1)^2}{2 \cdot \sigma^2}} + e^{-\frac{(t-t_2)^2}{2 \cdot \sigma^2}} \right]$$

Where

C_R = maximum charge concentration in the time;

σ = charge diffusion parameter.



BOUNDARY CONDITIONS

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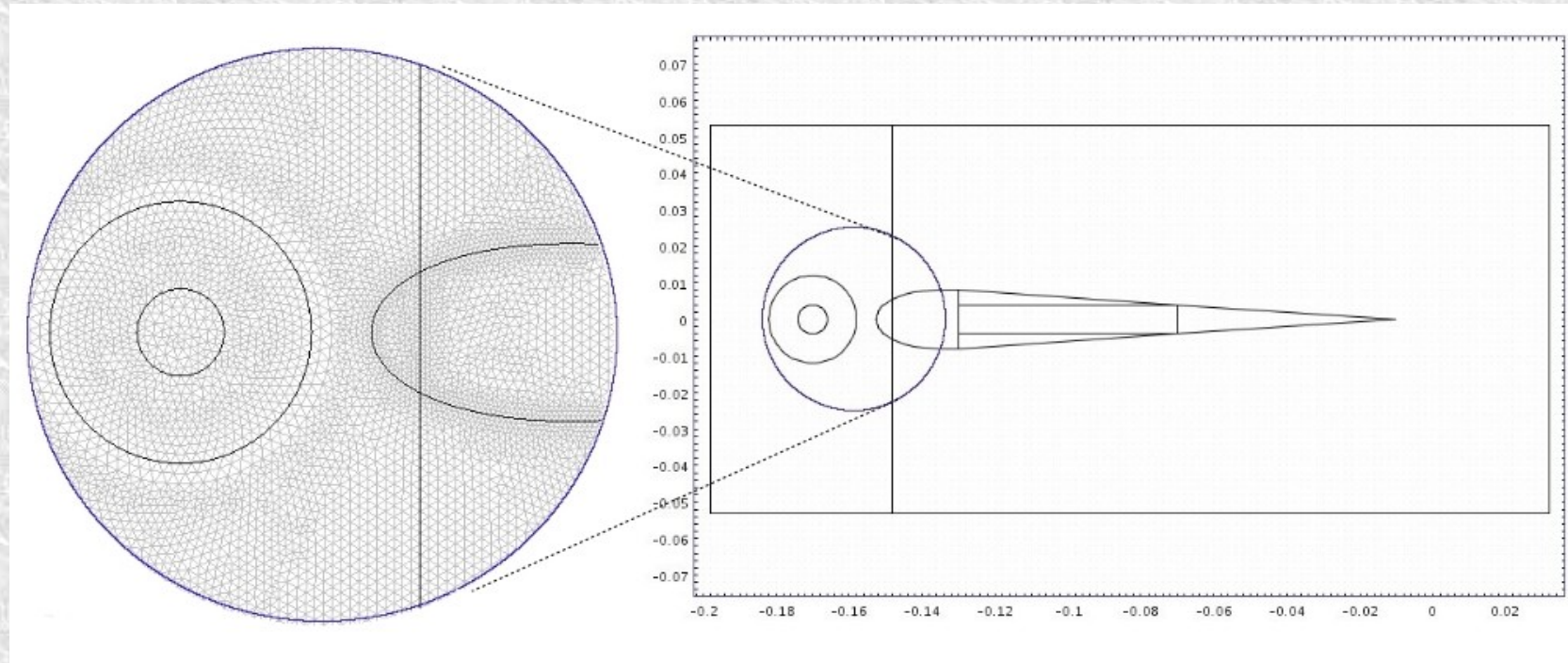
- For fluid dynamic
 - logarithmic wall function in the inner walls;
 - inlet velocity =200m/s;
 - outlet pressure= 101325 Pa.
- For Electrostatic
 - 50 kV DC voltage between capacitor plates;
 - Electric insulation in all inner walls.
- For convection and diffusion
 - Convective flux diffusion in the outlet section;
 - Zero diffusive flux condition in all the other boundaries.

MESH SETTINGS

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- 90752 elements
- Degree of freedom:
 - 904213 electrostatics and fluid dynamic model
 - 339236 convection and diffusion model





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SOLVER SETTINGS

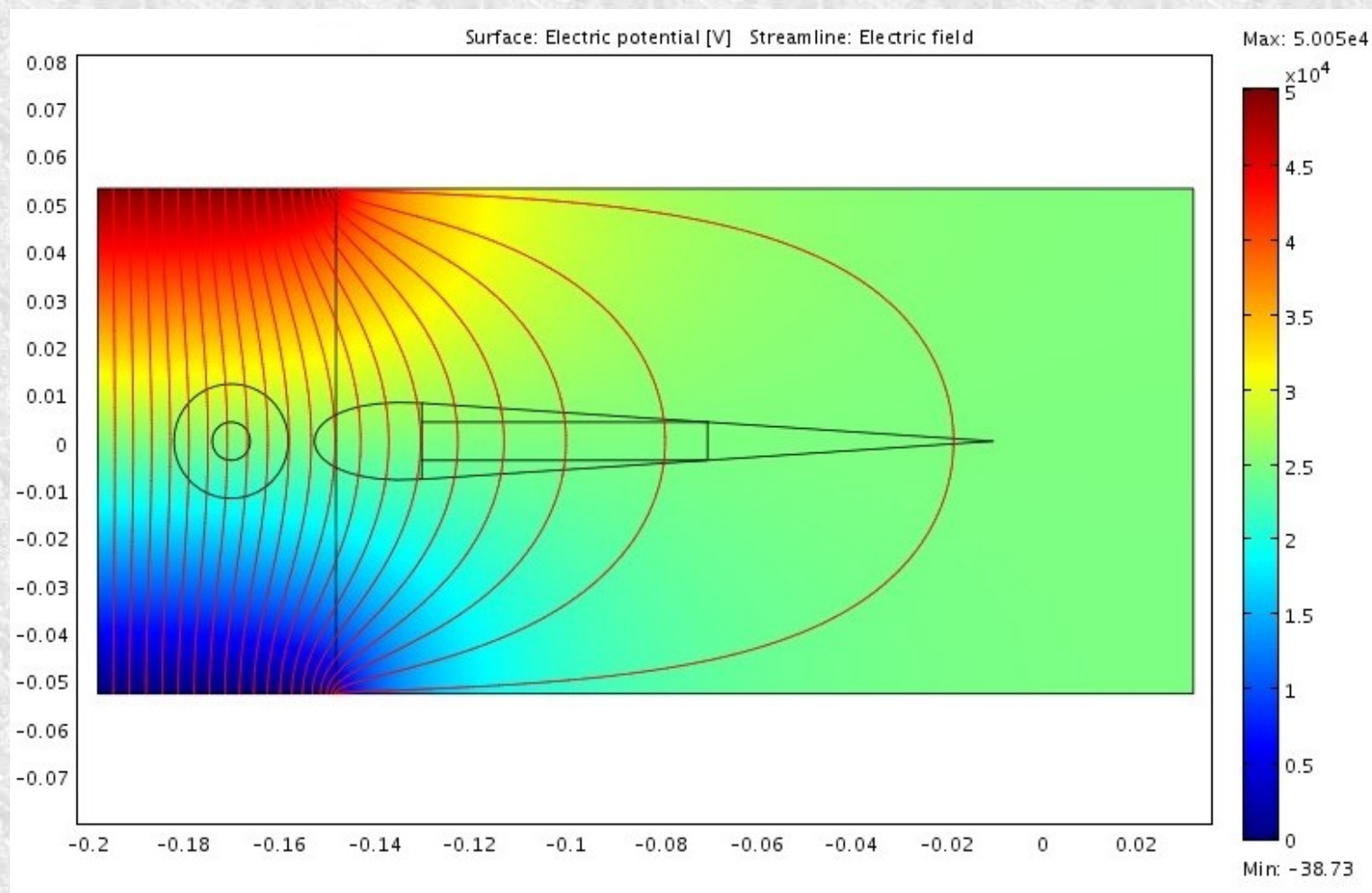
- Electrostatics and fluid dynamic modules are separated from a convection and diffusion module;
- Firstly the electrostatic and fluidodynamic module are solved by use of stationary solver.
- Then the velocity field and the electric field are used as source terms to solve the convection and diffusion equations by transient solver.

RESULTS

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- Surface electric potential and streamline electric field.

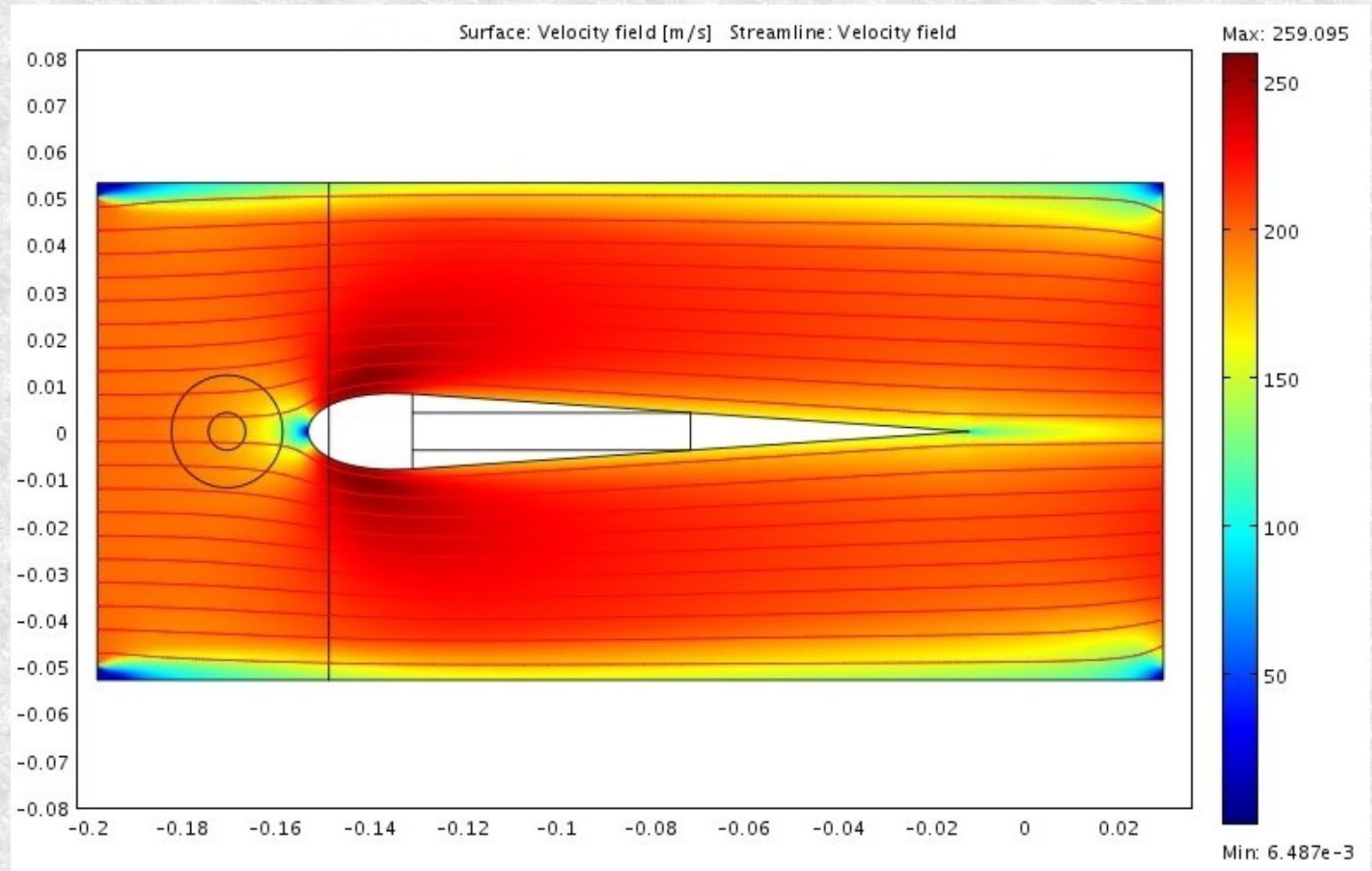


RESULTS

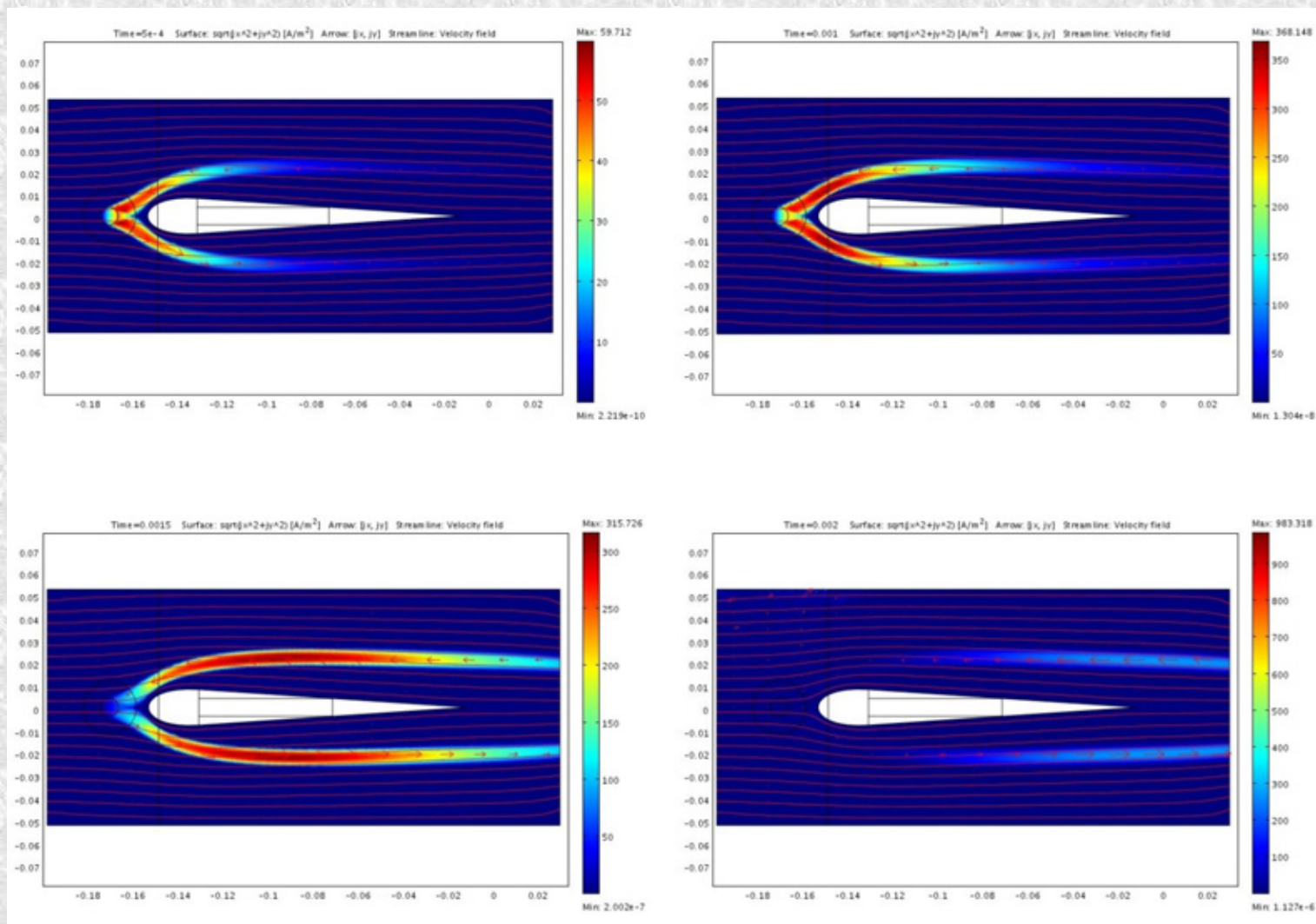
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- Surface and the streamline flow of the gas inside of the duct.



- Movement of the charge inside of the duct.



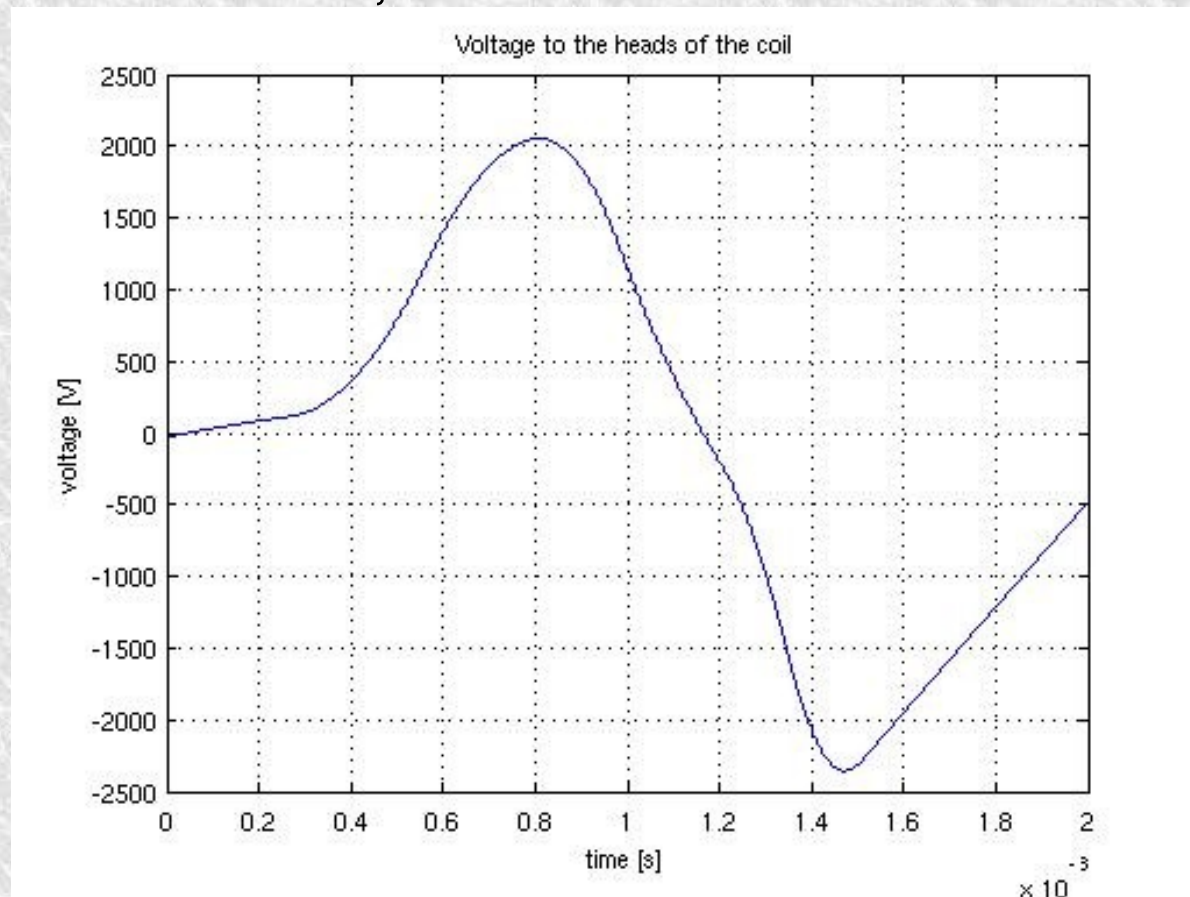


RESULTS

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- Trend of a voltage in the secondary winding left open circuited;



- Maximum Power (adapted load) 18kW.



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CONCLUSION

- The COMSOL 3.5a has been revealed as a suitable tool for a preliminary study to evaluate the physical feasibility of a inductive MHD generator;
- The proposed device does not need an external magnetic field to work but it performs the energy conversion by means of the inductive principle. This is possible thanks to a pulsed ionization of the fluid current, carried out with a electrode dipped;
- The possible future works can be represented by the coupling with the heat transfer model and solve the three - dimensional model.